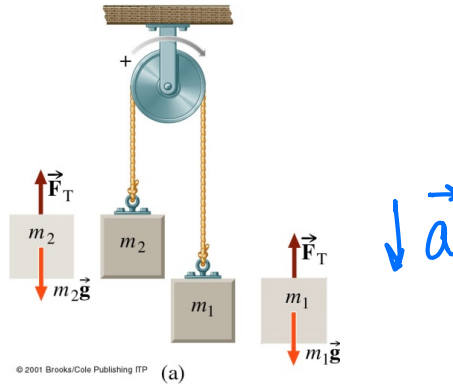
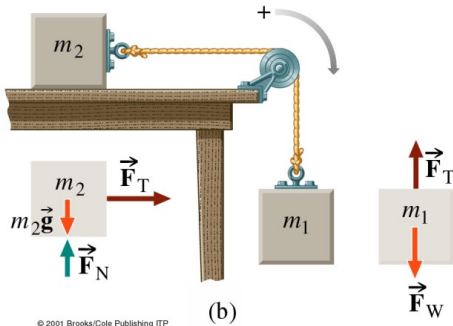


ÉQUILIBRE

PGC-04
(PGC-02)

RAPPEL – MOUVEMENT COUPLÉ



$$\vec{F}_W = \vec{F}_T$$

Au repos

$$m_1 > m_2$$

$$F_{W1} > F_T$$

$$a_1 = a_2$$

ÉQUILIBRE STATIQUE

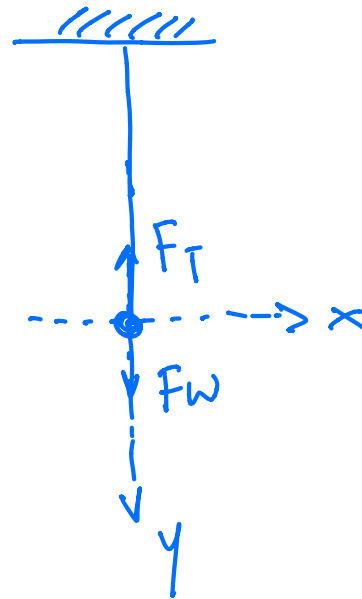
$$\sum \vec{F} = 0 \quad \Leftrightarrow \quad \vec{v} = \text{const}$$

$$\sum \vec{F}_x = 0$$

$$\sum \vec{F}_y = 0$$

$$F_T = F_W$$

Sans Rotation.

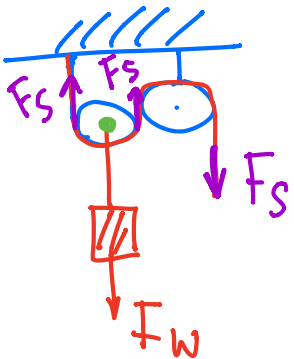
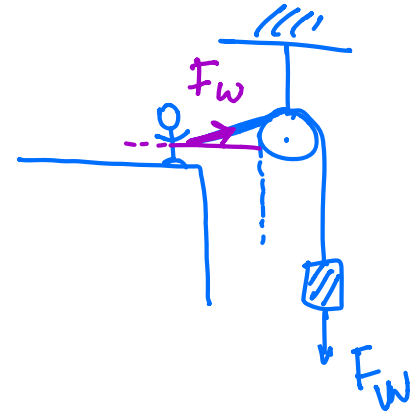


SYSTÈMES DE FORCES PARALLELES

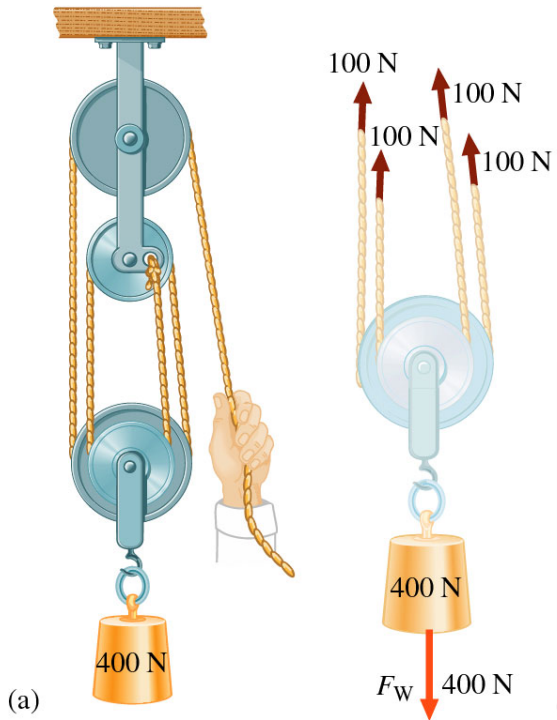
Poulies

- Reorienter forces

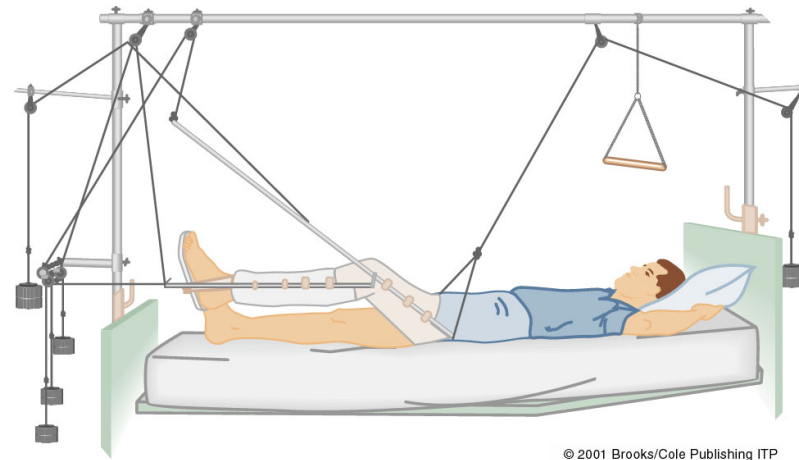
- Demultiplier forces



$$F_s = \frac{1}{2} F_w$$



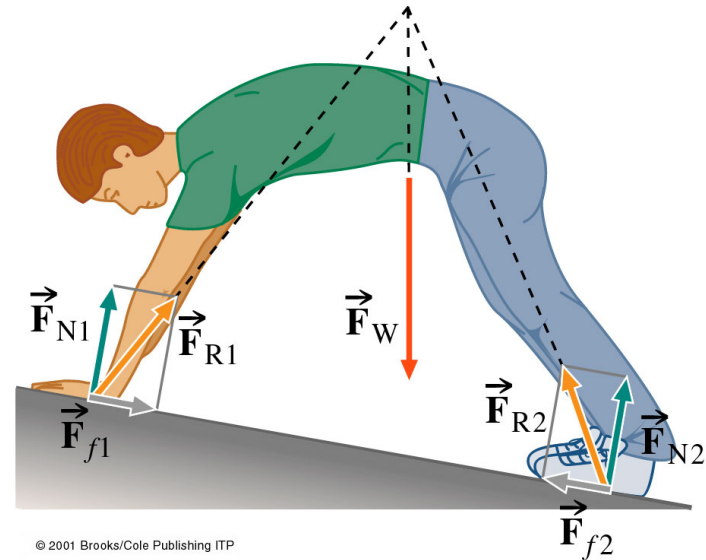
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FORCES CONCURRANTES

$$\Sigma \vec{F} = \vec{F}_w + \vec{F}_{R1} + \vec{F}_{R2} =$$

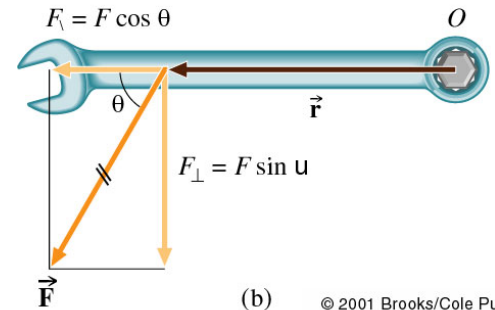
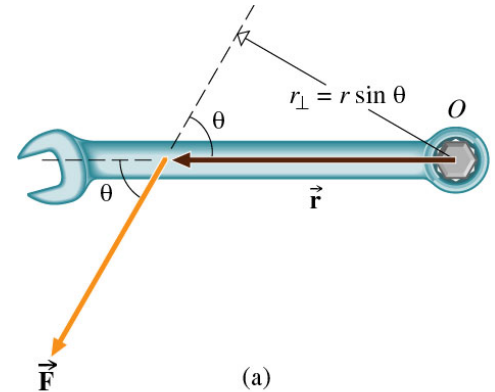


LE MOMENT DE FORCE

$$\begin{aligned}\tau_o &= r_{\perp} \cdot F = r \cdot \sin\theta \cdot F = \\ &= r \cdot F \cdot \sin\theta = \\ &= r \cdot F_{\perp}\end{aligned}$$

↙
bras de levier

$$[\tau] = [F] \cdot [r] = \text{N} \cdot \text{m}$$

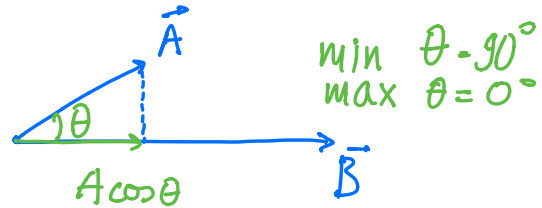


PRODUIT SCALAIRE

$$\vec{A} = \begin{pmatrix} A_x \\ A_y \end{pmatrix}$$

$$\vec{B} = \begin{pmatrix} B_x \\ B_y \end{pmatrix}$$

$$\begin{aligned} \vec{A} \cdot \vec{B} &= A_x B_x + A_y B_y = \\ &= |\vec{A}| \cdot |\vec{B}| \cdot \cos \theta \end{aligned}$$



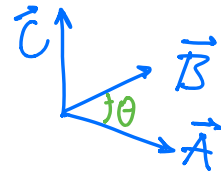
PRODUIT VECTORIEL

$$\vec{C} = \vec{A} \times \vec{B}$$

$$\begin{pmatrix} C_x \\ C_y \\ C_z \end{pmatrix} = \begin{pmatrix} A_x \\ A_y \\ A_z \end{pmatrix} \times \begin{pmatrix} B_x \\ B_y \\ B_z \end{pmatrix} = \begin{pmatrix} A_y B_z - A_z B_y \\ -(A_x B_z - A_z B_x) \\ A_x B_y - A_y B_x \end{pmatrix}$$

$$|\vec{C}| = |\vec{A}| \cdot |\vec{B}| \cdot \sin \theta$$

$$\begin{aligned} \text{min } \theta &= 0 \\ \text{max } \theta &= 90^\circ \end{aligned}$$



Si

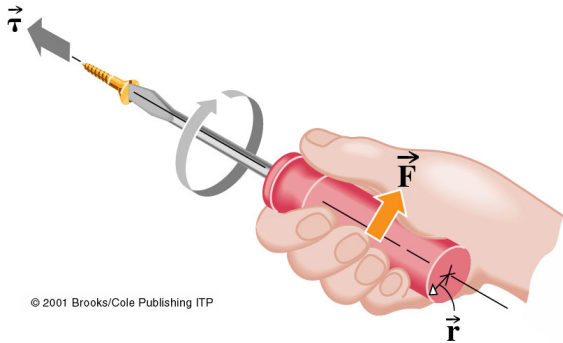
$$A = \begin{pmatrix} A_x \\ A_y \\ 0 \end{pmatrix} \quad B = \begin{pmatrix} B_x \\ B_y \\ 0 \end{pmatrix} \quad \rightarrow \quad C = \begin{pmatrix} 0 \\ 0 \\ C_z \end{pmatrix}$$

$A_z = 0$ $B_z = 0$

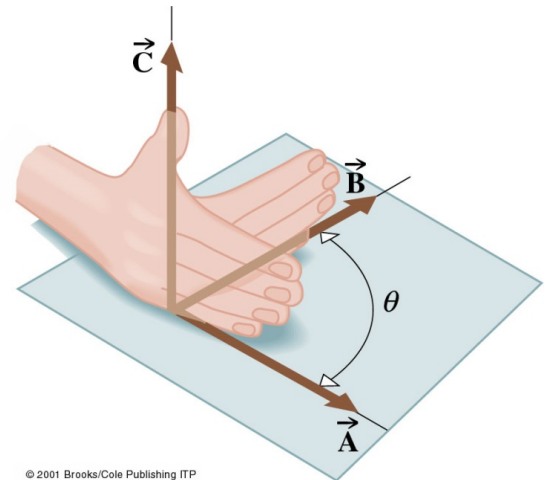
LE MOMENT DE FORCE

$$\tau_o = r F \sin \theta$$

$$\vec{\tau}_o = \vec{r} \times \vec{F}$$



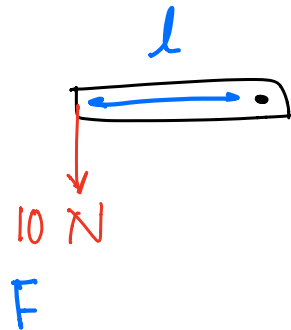
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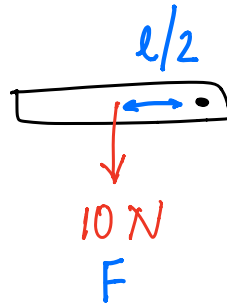
QUESTION

Dans quelle situation le moment de force est-il plus grand?



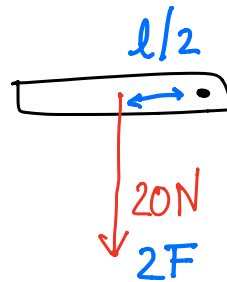
(a)

$$\tau = F \cdot l$$



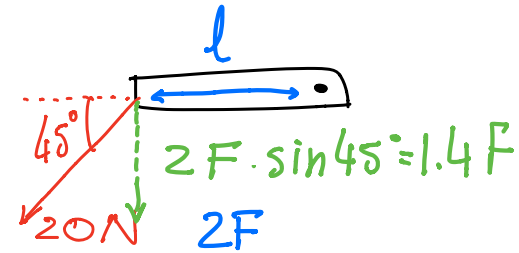
(b)

$$\tau = F \cdot \frac{l}{2}$$



(c)

$$\begin{aligned}\tau &= 2F \cdot \frac{l}{2} \\ &= F \cdot l\end{aligned}$$



(d)

$$\tau = 1.4 F \cdot l$$

$$\vec{\tau}_O = \vec{r} \times \vec{F}$$

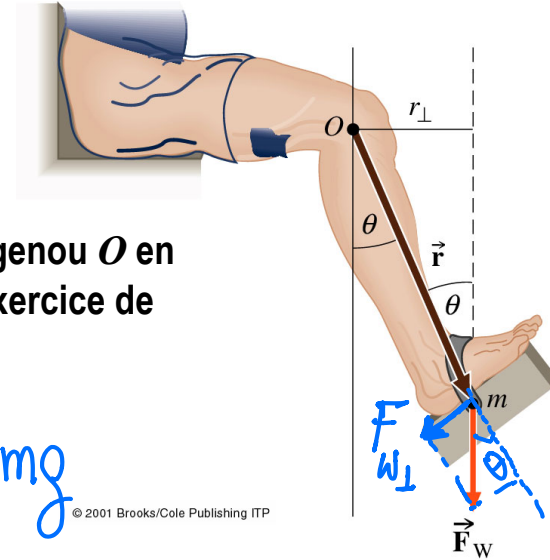
EXEMPLE

QUESTION: Exprimez le moment des forces par rapport au genou O en fonction de θ , m , et la distance r du genou au talon dans l'exercice de musculation ci-contre. Négligez la masse de la jambe.

$$\tau_O = r_{\perp} \cdot F_w = r_{\perp} \cdot mg = r \cdot \sin\theta \cdot mg$$

$$\tau_O \text{ min } \theta = 0$$

$$\tau_O \text{ max } \theta = 90^\circ$$



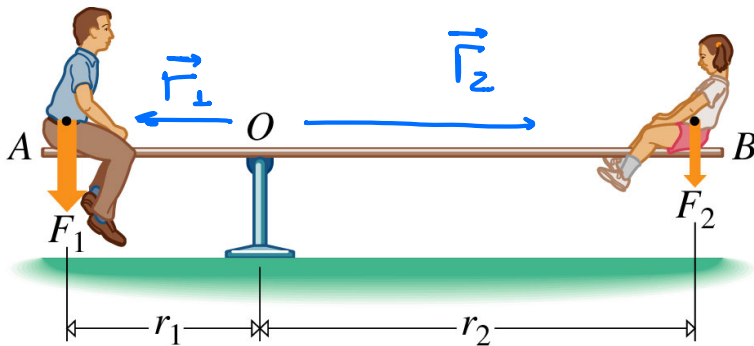
SECONDE CONDITION D'ÉQUILIBRE

$$\vec{\tau} = \vec{r} \times \vec{F} \quad \Sigma \vec{F} = 0 \Leftrightarrow \Delta \vec{v} = 0, \vec{v} = \text{const}$$

$$\Sigma \vec{\tau} = 0 \Leftrightarrow \Delta \vec{\omega} = 0$$

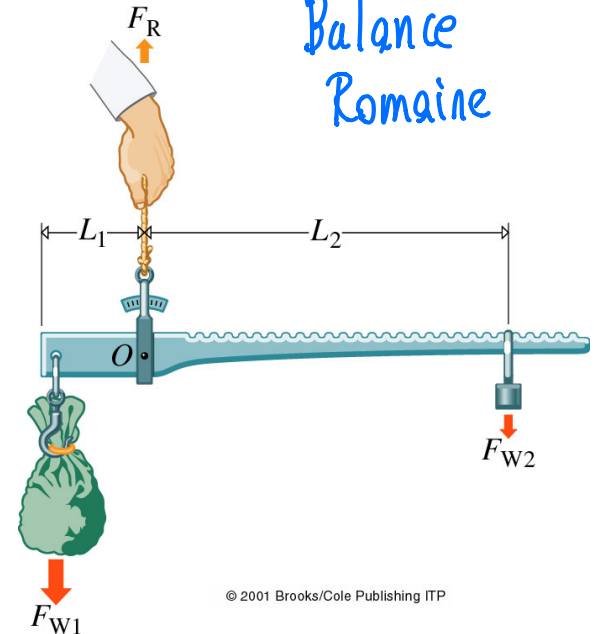
$$F_1 > F_2 \quad \Sigma \vec{F} = \vec{F}_1 + \vec{F}_2 \neq 0$$

$$F_1 \cdot r_1 = F_2 \cdot r_2$$



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Balance
Romaine



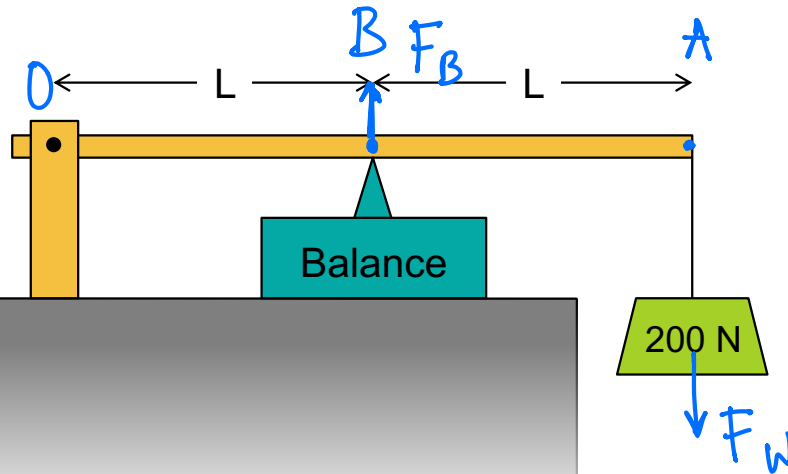
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QUESTION

Quelle est l'indication de la balance?

$F_B = ?$

- a) 200 N
- b) 400 N
- c) 100 N
- d) 0 N



$$\Sigma \vec{\tau} = 0$$

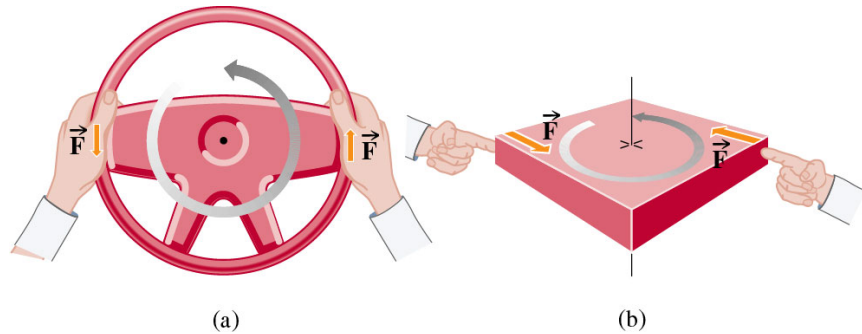
$$-\vec{\tau}_{AO} = \vec{\tau}_{BO}$$

$$F_W \cdot 2L = F_B \cdot L$$

$$\Rightarrow F_B = 2F_W$$

FORCES NON-CONCOURANTES

$$\Sigma \vec{F} = 0 \quad \underline{\underline{\text{MAIS}}} \quad \Sigma \vec{\tau} \neq 0$$

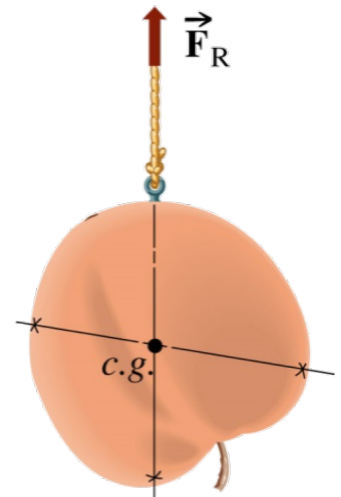
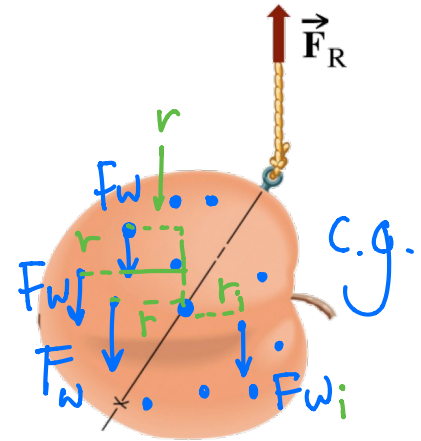


CENTRE DE MASSE

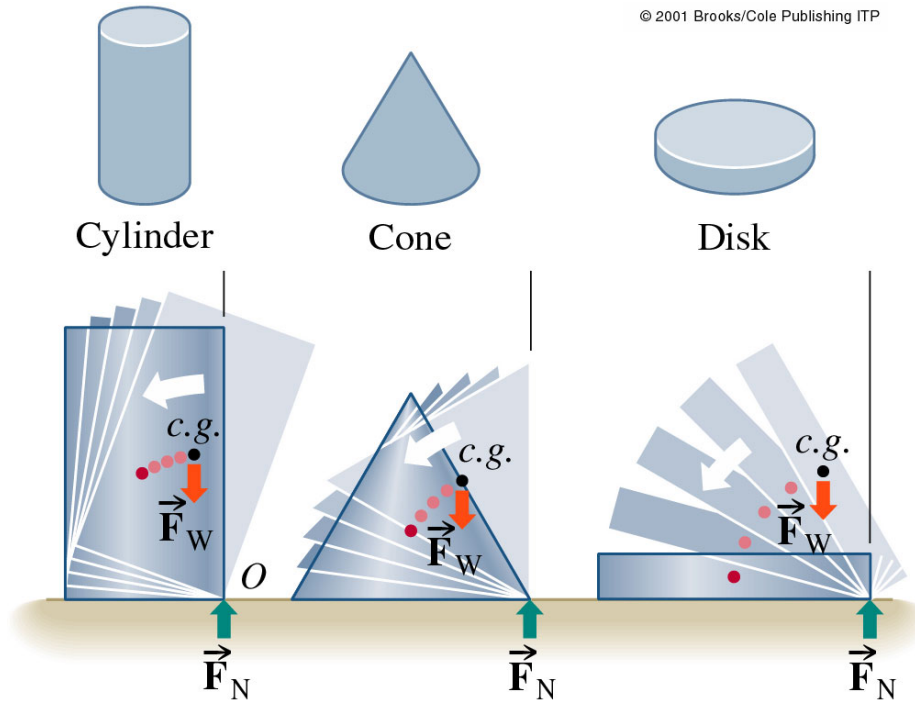
$$x_{cg.} = \frac{\sum_{i=1}^N F_{w_i} r_i}{\sum_{i=1}^N \bar{F}_{w_i}}$$

$$\sum F_{w_i} \cdot x_{cg} = \sum_{i=1}^N \bar{F}_{w_i} r_i$$

$$F_w \cdot x_{cg} = \sum_{i=1}^N \bar{F}_{w_i} r_i$$



STABILITÉ ET ÉQUILIBRE



LE CENTRE DE MASSE

Un haltère se compose d'un disque de 500 gr d'une coté et d'un disque de 2 kg de l'autre coté. On considère la barre qui les connecte sans masse et le longueur 50 cm. Calculer le centre de masse.

$$x_{CM} = \frac{\sum_i F_i x_i}{\sum F_i}$$

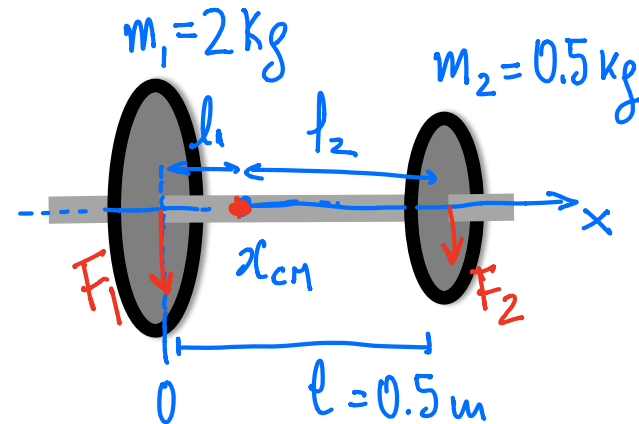
$$F_i = m_i g$$

$$F_1 \cdot l_1 = d_2 \cdot F_2$$

$$x_{CM} = \frac{F_1 \cdot x_1 + F_2 \cdot x_2}{F_1 + F_2} =$$

$$= \frac{m_1 \cdot x_1 + m_2 \cdot x_2}{m_1 + m_2} = \frac{m_2 \cdot l}{m_1 + m_2} \Rightarrow$$

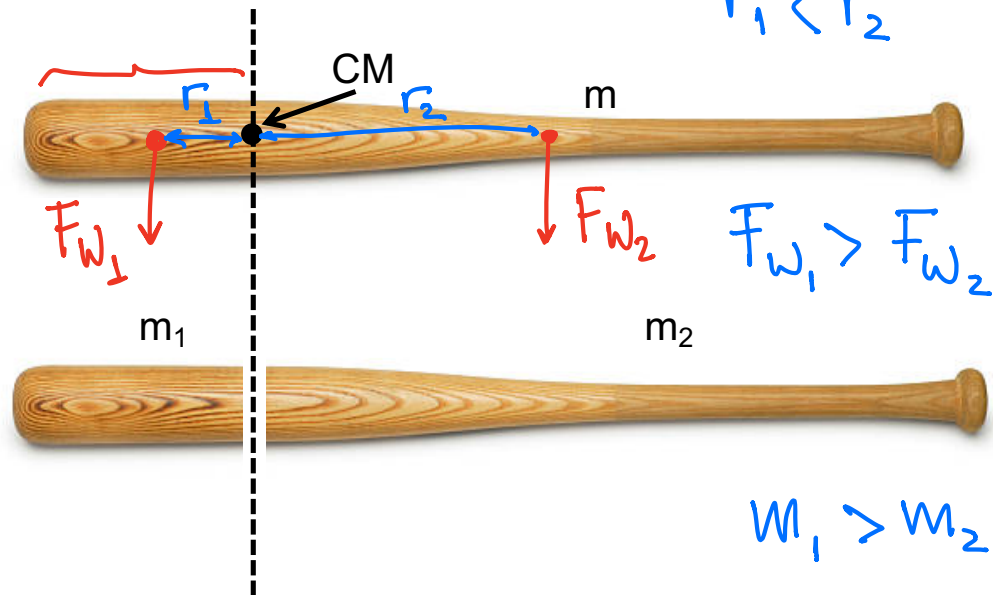
$$x_{CM} = \frac{m_2 l}{m_1 + m_2} = \dots 0,1 m$$



LE CENTRE DE MASSE - QUESTION

$$\sum \vec{\tau}_{CM} = 0 \Rightarrow F_{W_1} \cdot r_1 = F_{W_2} \cdot r_2$$

$$r_1 < r_2$$



(a) $m_1 > m_2$

(b) $m_1 = m_2$

(c) $m_1 < m_2$