Invisible Higgs & trigger challenges on ATLAS

A discussion on Dark sector,
Higgs boson,
Trigger, and
ML on FPGA





Université de Genève September 28, 2021

Outline

Motivation (10 min)

- Dark sector
- Higgs boson

Analyses (20 min)

- H₁₂₅ → Dark matter pair ATLAS Collab, ATLAS-CONF-2020-008 (2020)
- H₁₂₅ → Dark photon + Y ATLAS Collab, ATLAS-CONF-2021-004 (2021)

Trigger (30 min)

- E_Tmiss, VBF
- ML on FPGA

ATLAS, JHEP 08 (2020) 080

Hong et al., JINST 16 (2021) P08016



Motivation

Dark sector Higgs boson



Many evidence of dark matter

Here: colliding galaxy clusters

3 MLy (MACSJ0025, 2008)



Inferred distribution of matter by lensing

- _ X-rays from known matter
- Dark matter (Known unknown)

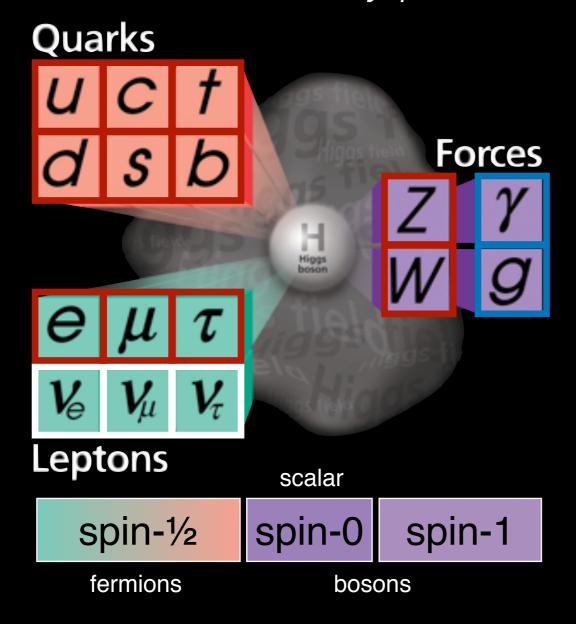
Source: https://apod.nasa.gov/apod/ap080917.html



Higgs boson couplings

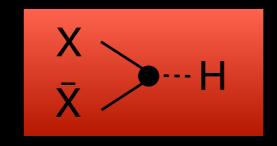
Higgs couples to everything

Table of elementary particles



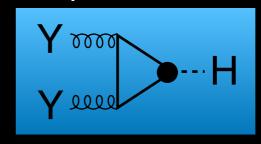
Feynman diagrams

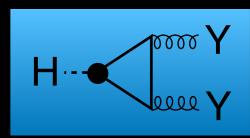
Tree relation for massive X





Loop relation for massless Y

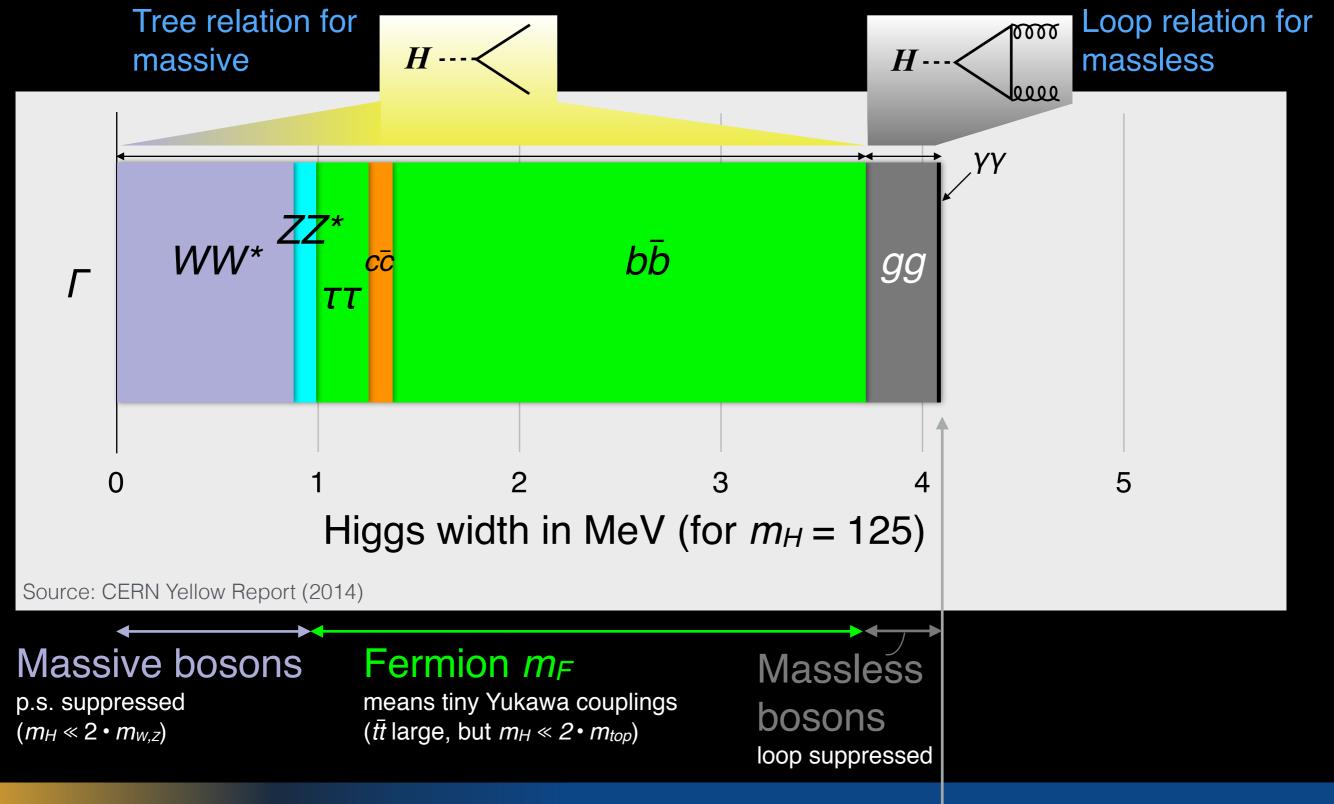




Source: Fermilab



Higgs is so narrow because 125 GeV

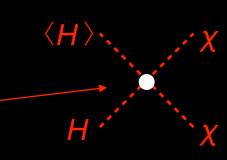


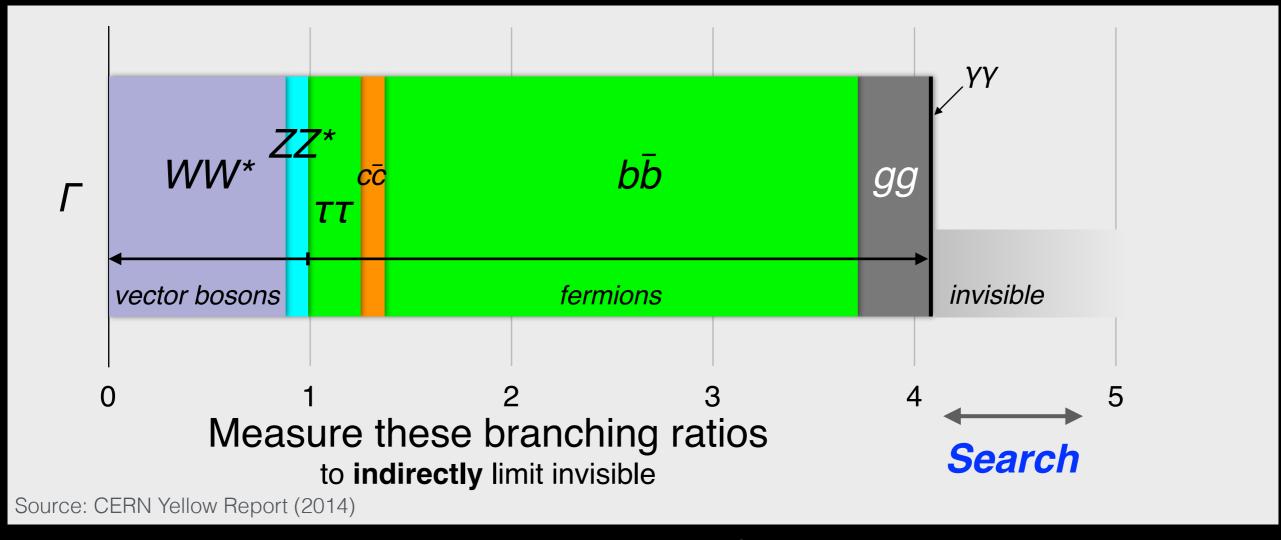


Everything is suppressed

O(MeV) is not unreasonable

Portals to NP can look like





Theory

Goncalves, Han, Mukhopadhyay, PRL 120, 11801 (2018)

Curtin, Essig, Zhong, 1412.4779 (2015)

Curtin +12 others, 1312.4992 (2014)

Chang +3 others, 0801.4554 (2008)

Silveira & Zee, PL B161,136 (1985)

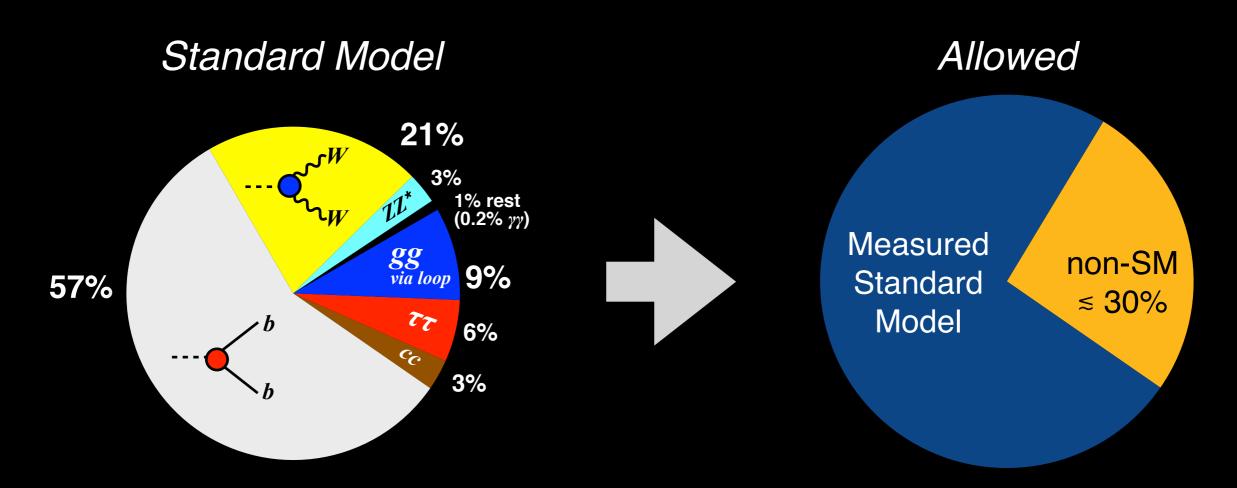
and many many more papers.



Fully renormalizable



What's allowed by individual measurements?



Measure each predicted slice

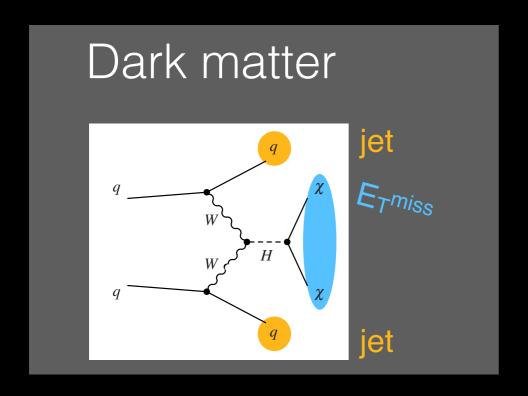
Constrains non-Standard Model (with caveats)

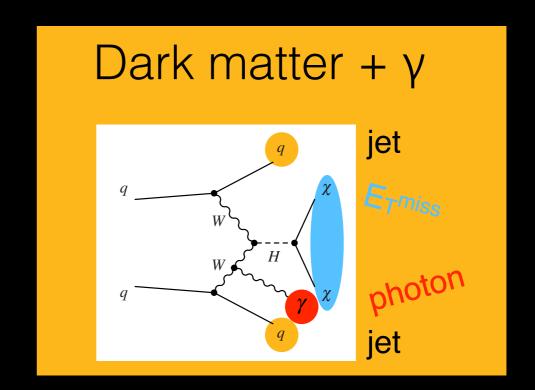
Source: http://cdsweb.cern.ch/record/2629412



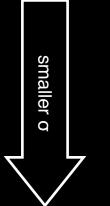
Dark matter (m>0)

Related production channels





Higgs production



- ggF No observable!
- ggF + 1 jet Overwhelming strong bkg'd
- VBF Depends on trigger threshold ——•
- ZH Suppressed by σ B
- WH and neutrino / hadronic W

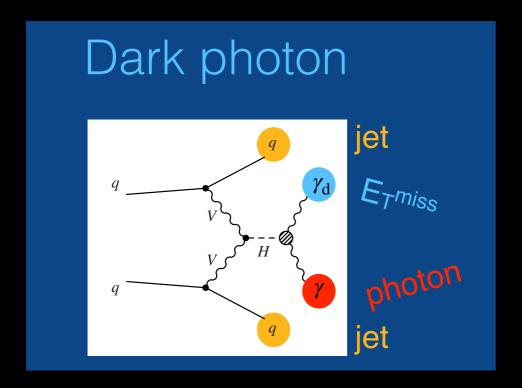
Comparison to without y

- Smaller signal size, but clean
- Adding γ reduces strong background
- Depends on trigger threshold
- Added bonus in interpretation (next slide)



Dark matter (m>0) → Dark photon (m=0)

Maybe there is a Dark sector



Dark matter + γ

jet

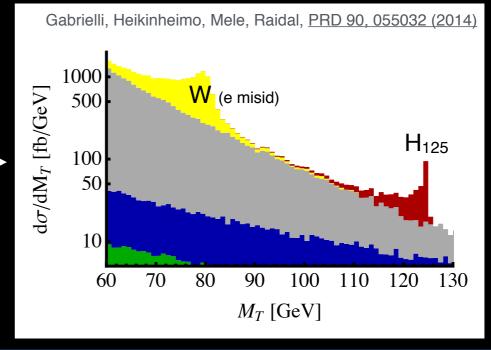
Frmiss

photon
jet

same final state

Theory

- Unbroken U(1)_{dark} with enhanced H $\rightarrow \gamma \gamma_{dark}$
- Signal peaks in the m_T of (E_T^{miss},γ) system —





Analyses

H₁₂₅ → Dark matter pair

 $H_{125} \rightarrow Dark photon + \gamma$



Physics of VBF *H* → *invisible*

VBF production of the Higgs is established

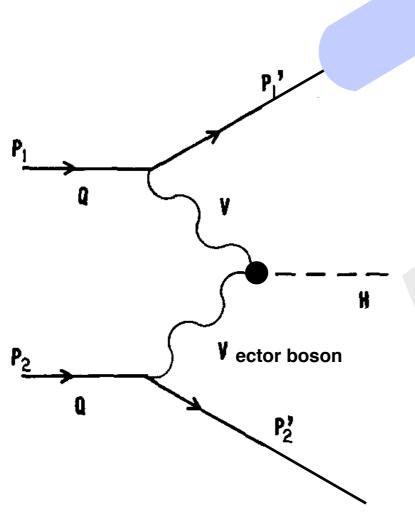
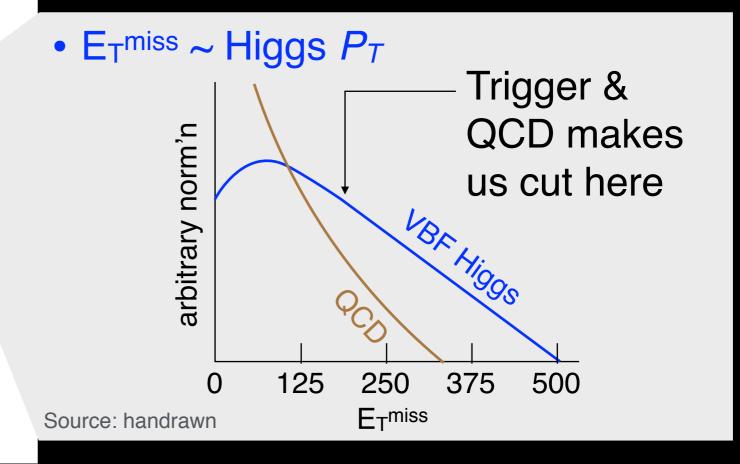


Fig. 1. Higgs boson production from virtual vector boson pairs (V = W or Z).

Source: Cahn, Dawson, PLB 136 (1984) 196

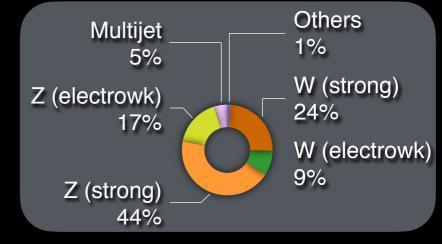
- Energetic jets with large η gap
- No hadronic activity
- m_{jj}, Δη_{jj}, N_{central jets}

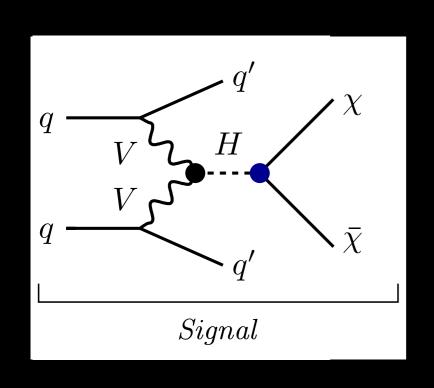


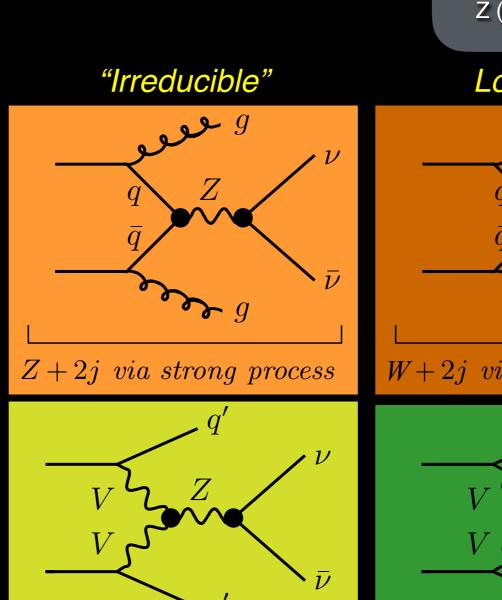


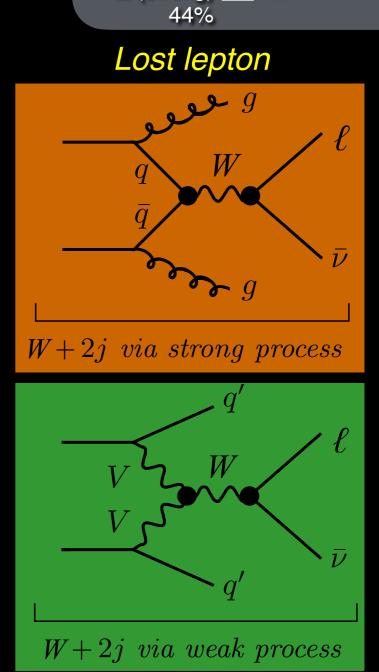
Signal & background

Z & W are largest







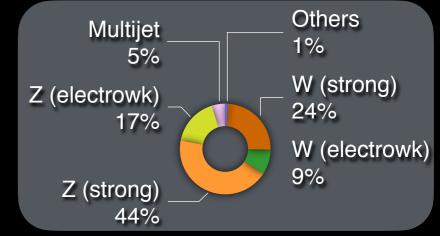


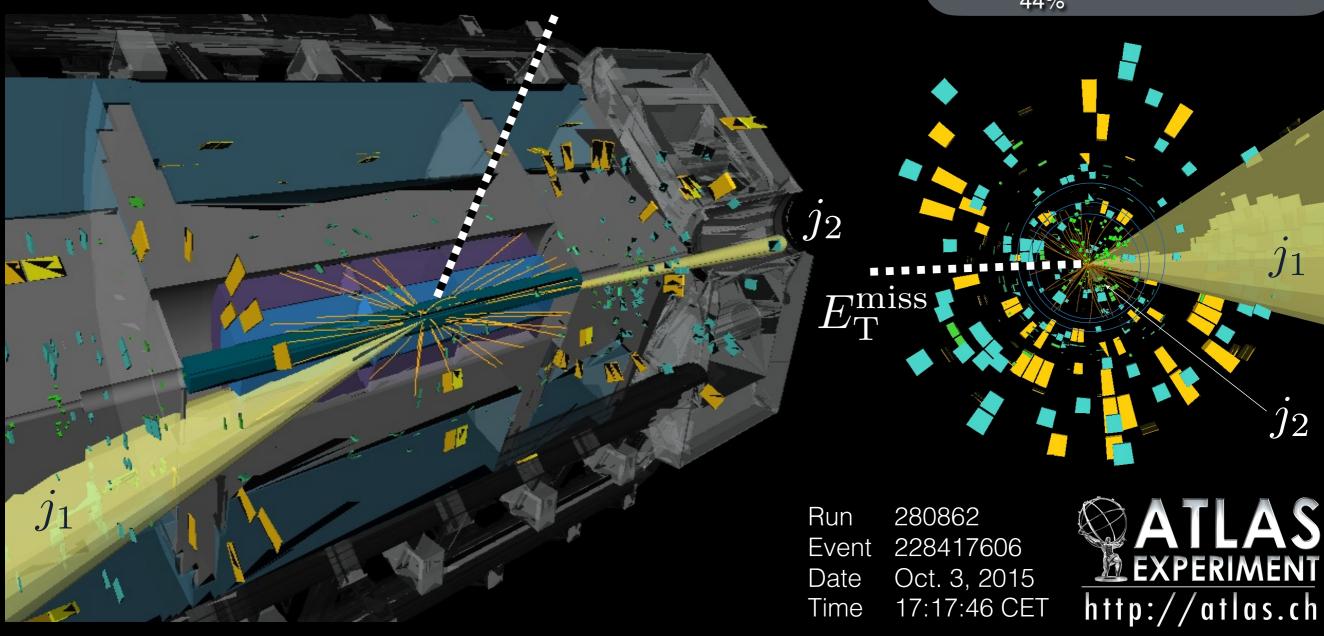


Z+2j via weak process

Event display

High E_Tmiss (564 GeV) + High m_{jj} (3.6 TeV)

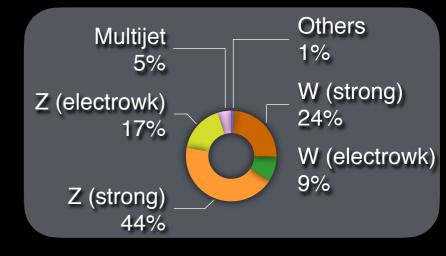


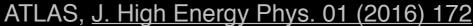


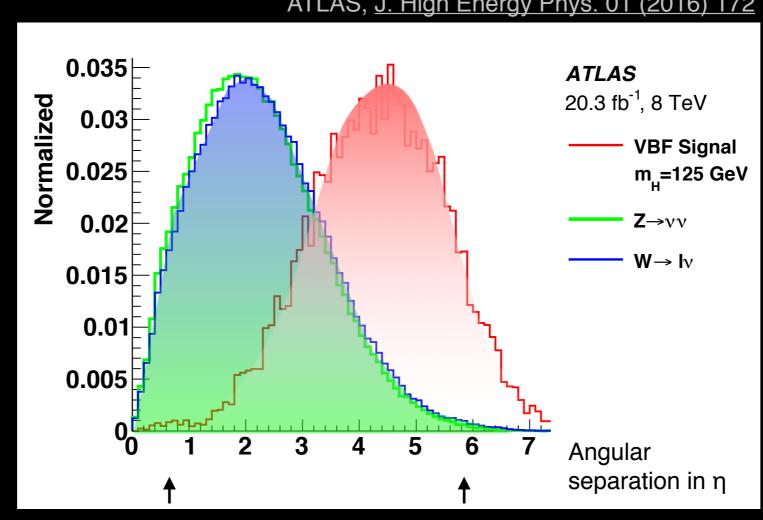


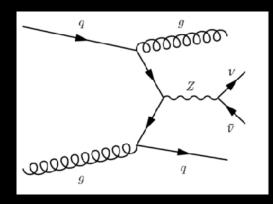
Angular characteristics

Data distribution of separation in η

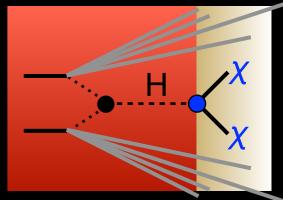








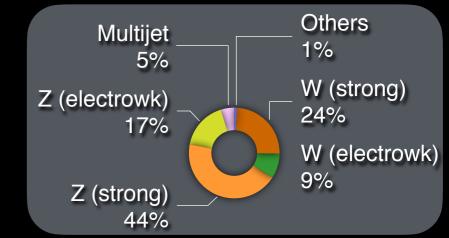






Selection

Signal region, control regions

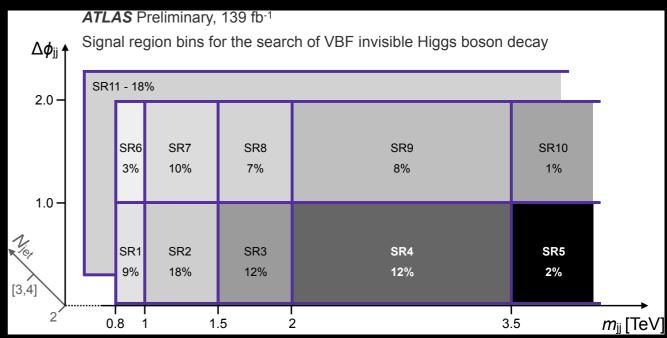


Cuts

- Two jets > 80 GeV, 50 GeV
- Centrality of additional jets
- E_T^{miss} > 200 GeV

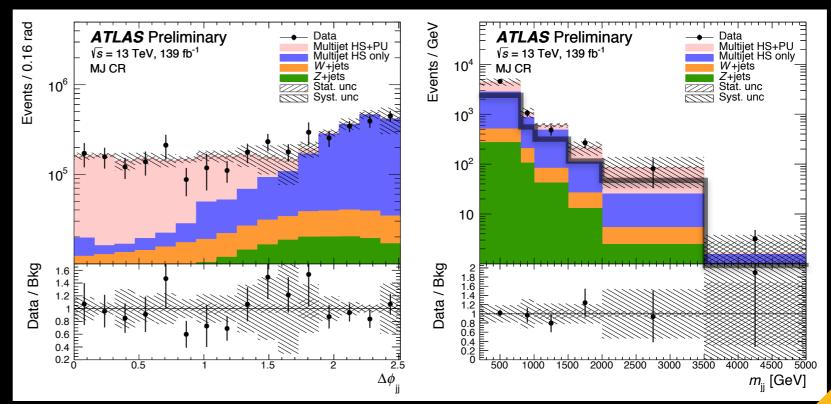
Signal region

• Bin in $m_{ij} \otimes N_{jet} \otimes \Delta \phi_{ij} = 5 \otimes 2 \otimes 2$



Control region

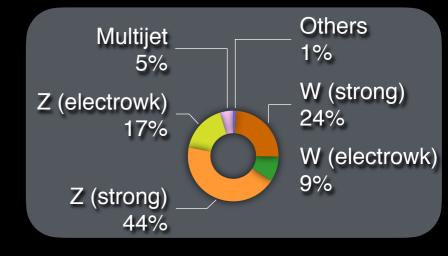
- $W \rightarrow \ell_V$
- \bullet $Z \rightarrow \ell \ell$
- Multijet by rebalance & smear ——

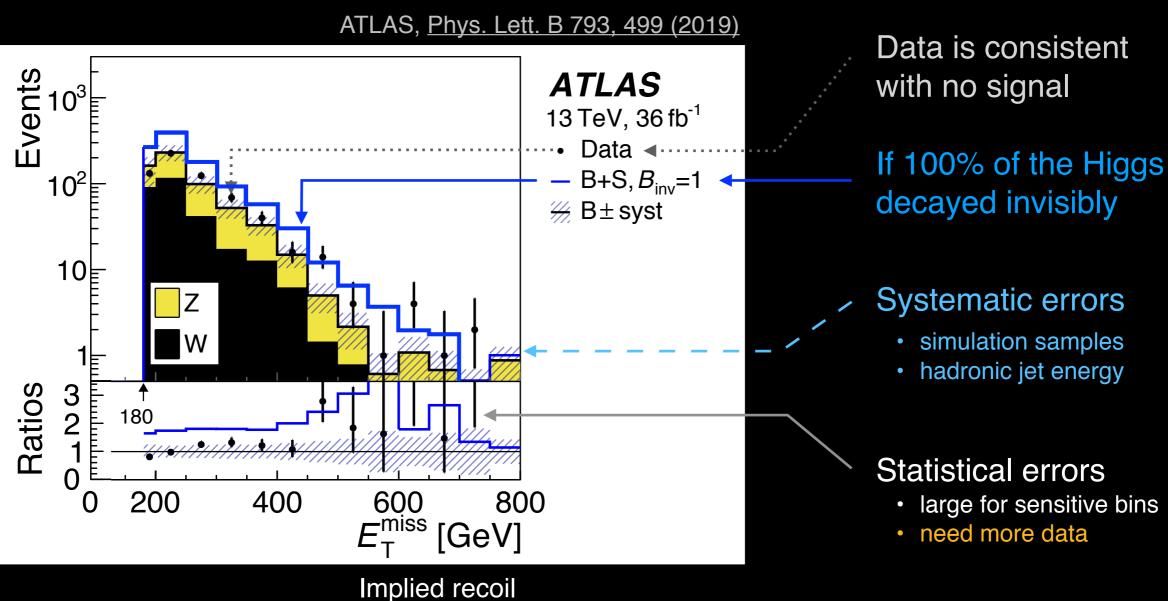




Results (2019)

Limits, systematics



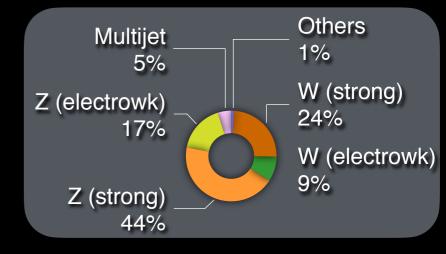


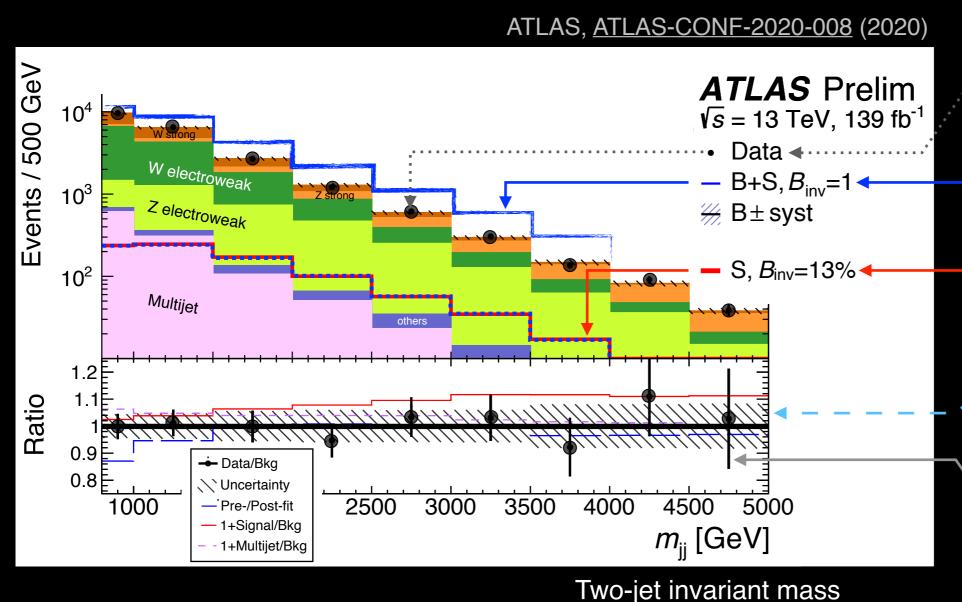


We can say that Higgs decays less than 37% to invisible final states

Update (2020)

Add 4x more data & improve methods





Data is consistent with no signal

If 100% of the Higgs decayed invisibly

If 13% of the Higgs decayed invisibly

Systematic errors

- simulation samples 8%
- multijet estimation 7%
- jet energy

Statistical errors

- · large for sensitive bins
- need more data 17%

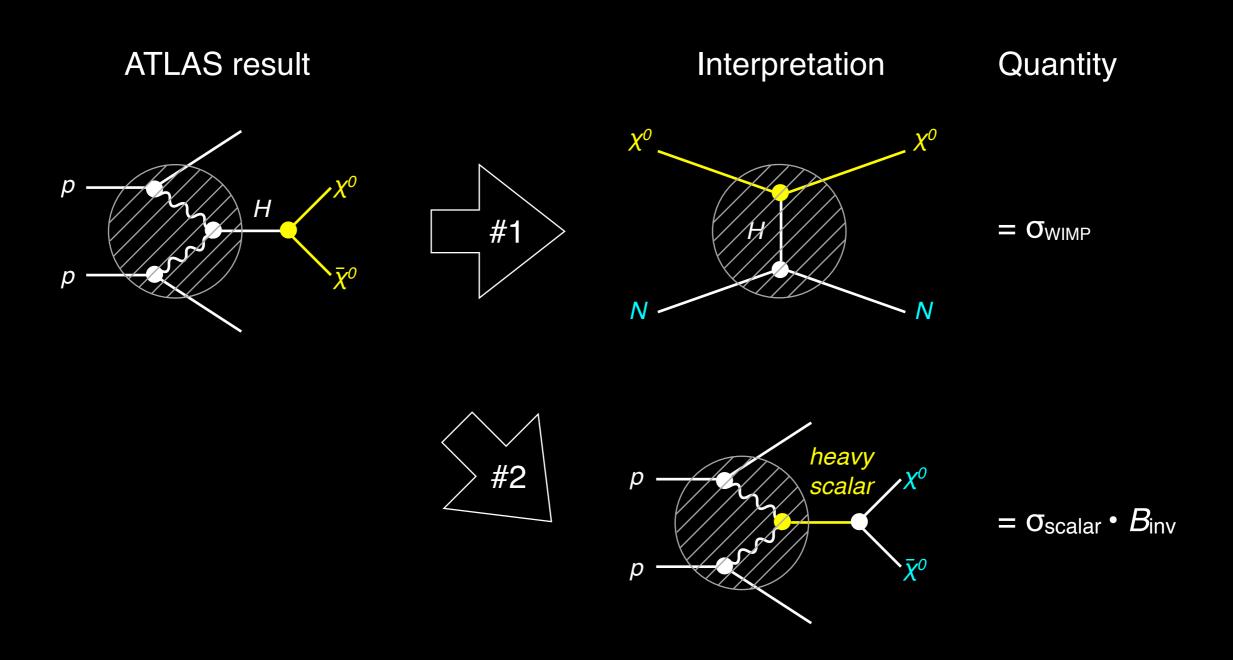


We can say that Higgs decays less than 13% to invisible final states

6%

Interpretations

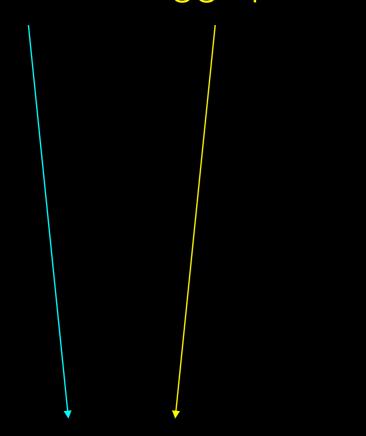
ATLAS result interpreted in #1, #2





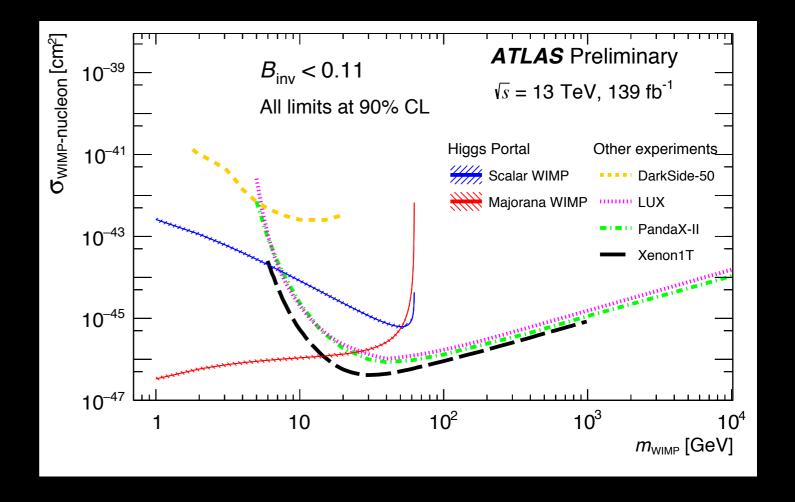
Interpretation #1

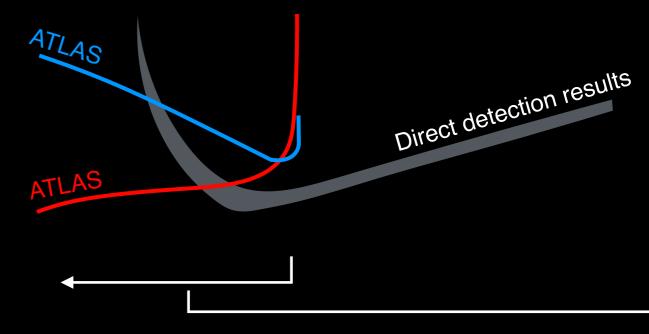
ATLAS result + Higgs portal



scalar: $\Gamma_{\text{inv}} \cdot (m_{\chi})^{-2} \sim \sigma_{\text{WIMP}}$

fermion: $\Gamma_{inv} \cdot const \sim \sigma_{WIMP}$

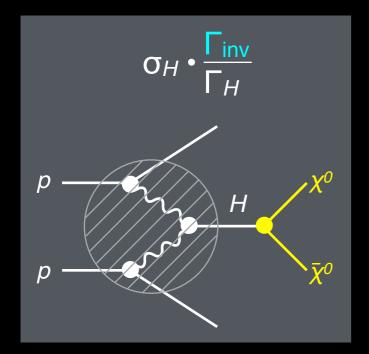


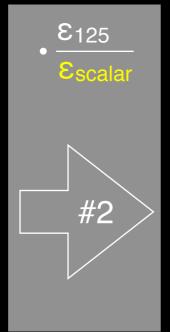


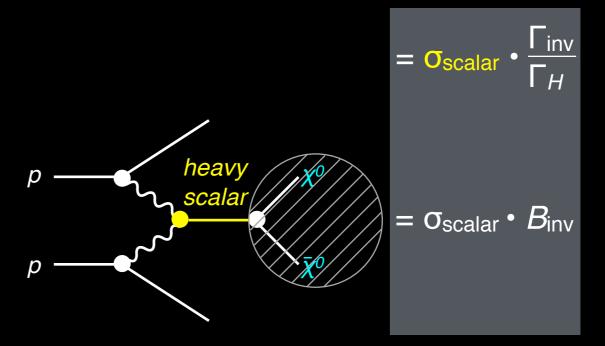


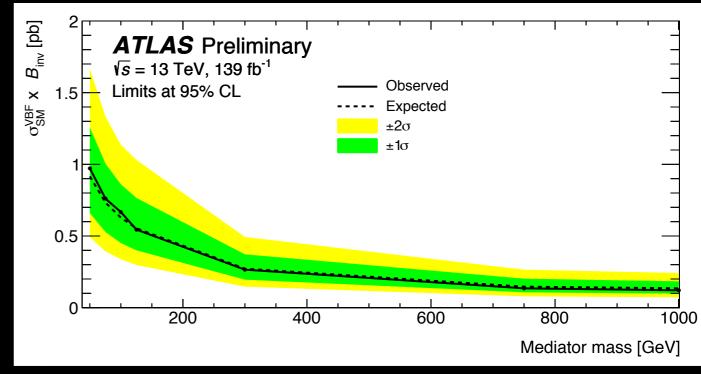
Interpretation #2

ATLAS result + "No model"



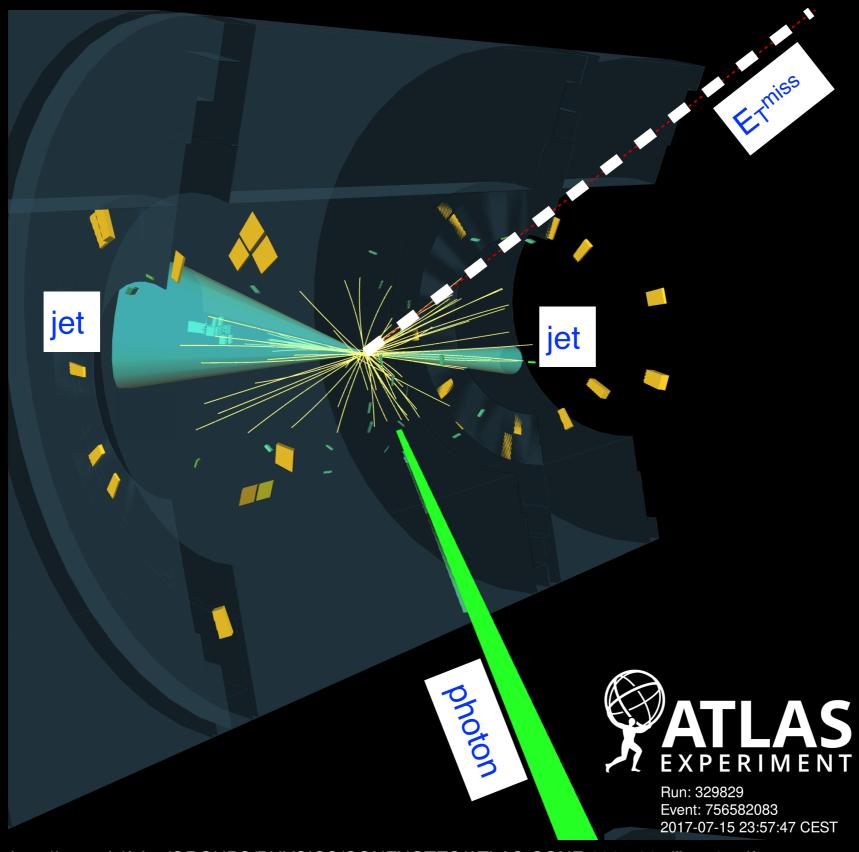








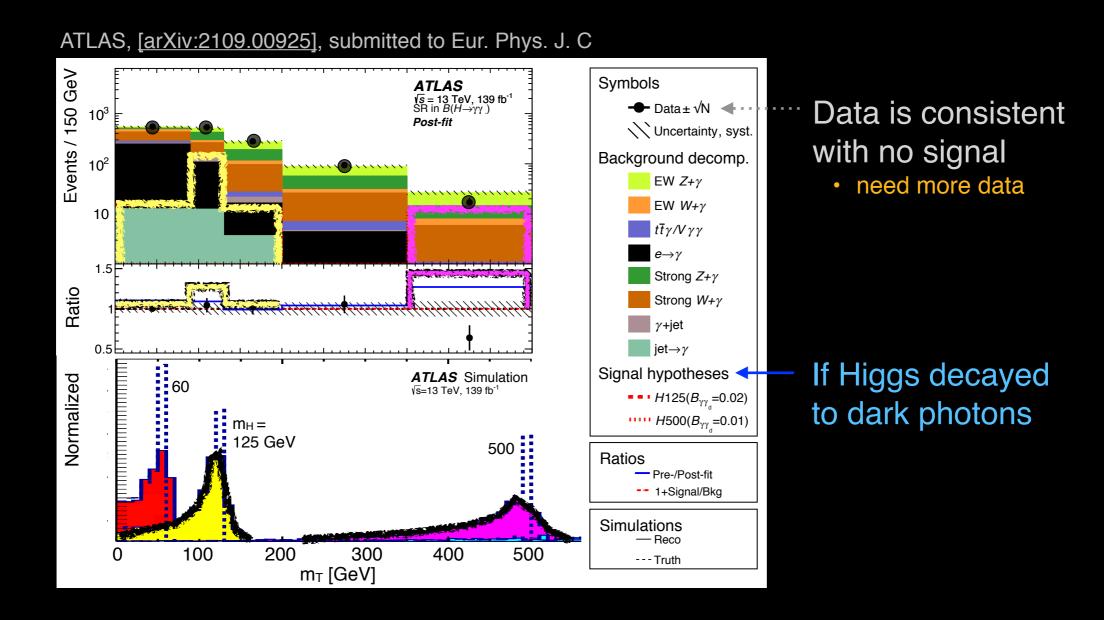
Add a photon to it





Interpretation

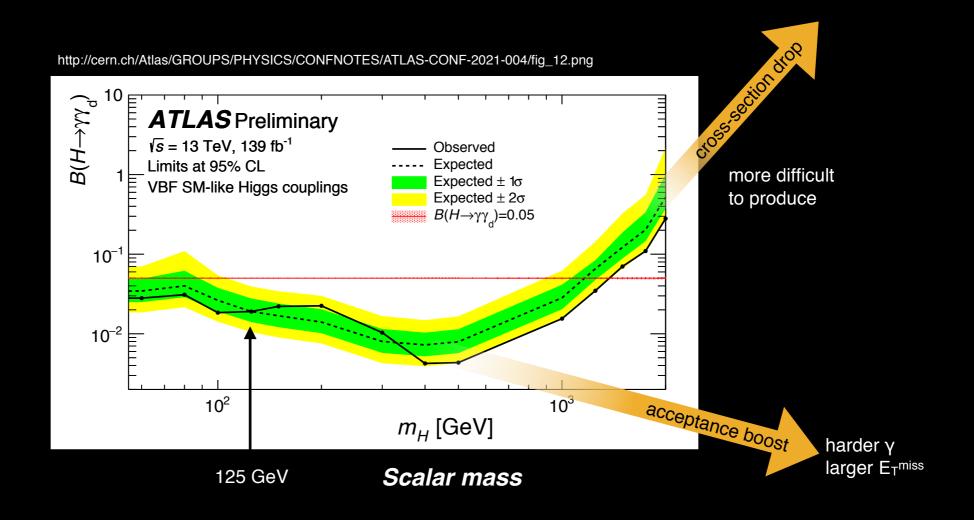
H₁₂₅ to γγ_{dark}





Interpretation

Scalar particle to γγ_{dark}





Trigger

E_Tmiss, VBF ML on FPGA



E_Tmiss trigger rate vs. (μ)

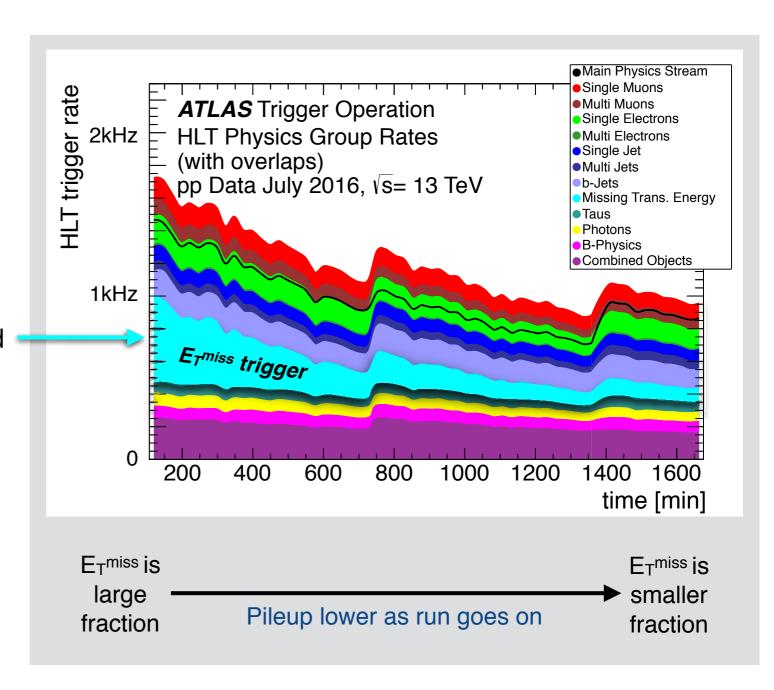
Rate blows-up with (µ), so very large at the beginning of runs

Physics

- Signal: Higgs p_T gives rise to E_T^{miss}
- Background: Combinatorics esp. vs. (μ)

Challenge

- Problem: E_Tmiss trigger is bandwidth limited
- Non-solution: Can't increase threshold to reduce the rate beyond ~150 GeV bec. signal peaks at low values
- Solution: Be smarter about reducing background while maintaining signal (sounds like physics analysis!)







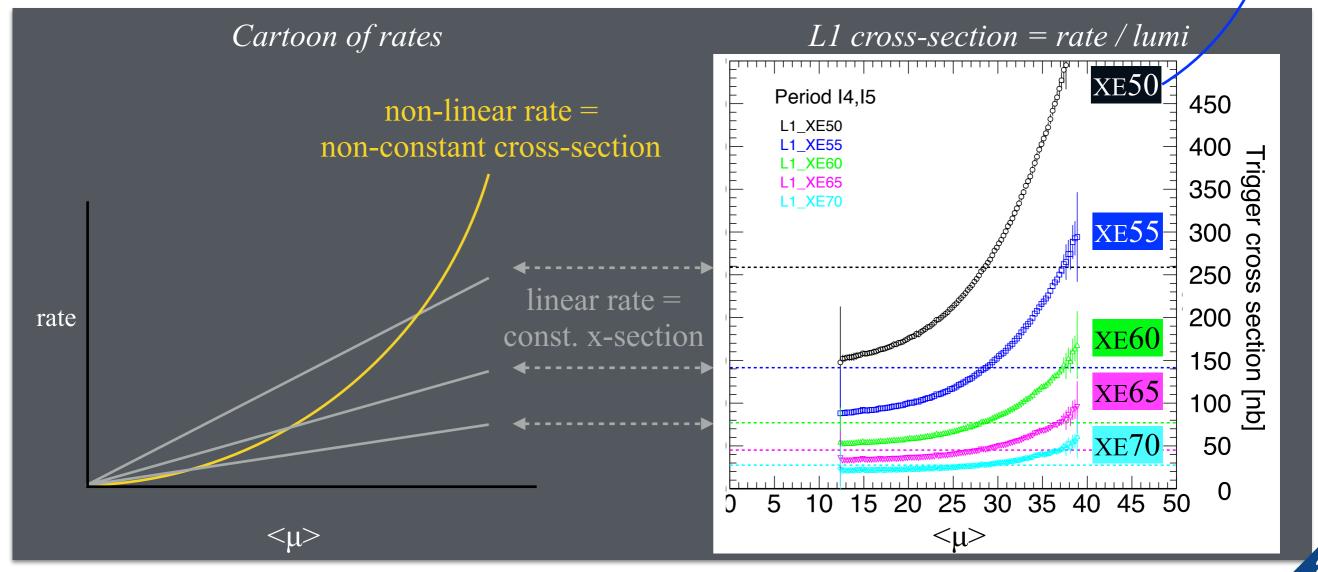
Lots of trouble with pileup driving up MET rates

- Conceptually, linear rate v. $<\mu>$ means "no pileup dependence," see left
- Rates show non-linear $<\mu>$ dependence, see right plot

Level-1 XE50 blowing up

Despite periods with very high L1 rates, we kept XE50

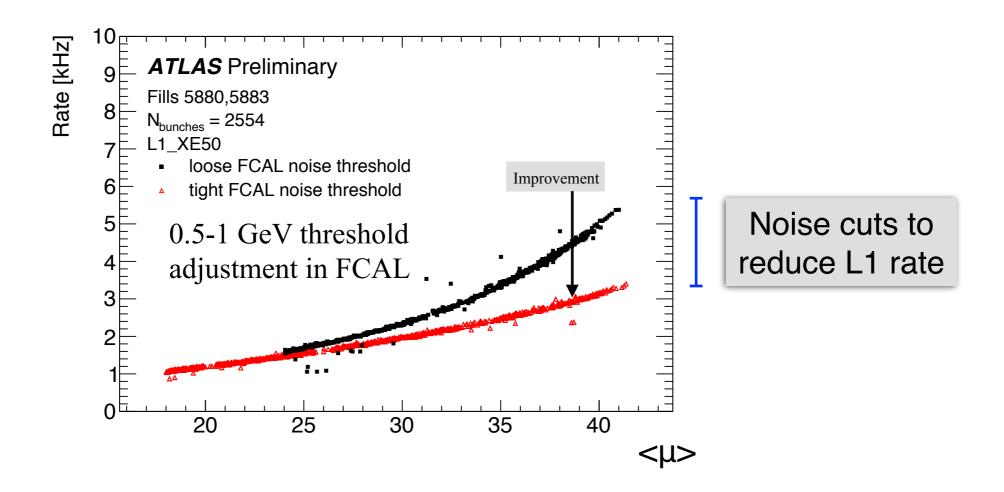
• The total rate did peak to almost 8 kHz a few times, but this was only at the start of





Frequent adjustments to noise cuts control the rate

- Adjusted as the pileup increases or the filling scheme changed (right)
- The noise cuts were adjusted three times in 2017 and once in 2018
- Plot on the left shows the impact of the first change





Try combo to

reduce rate

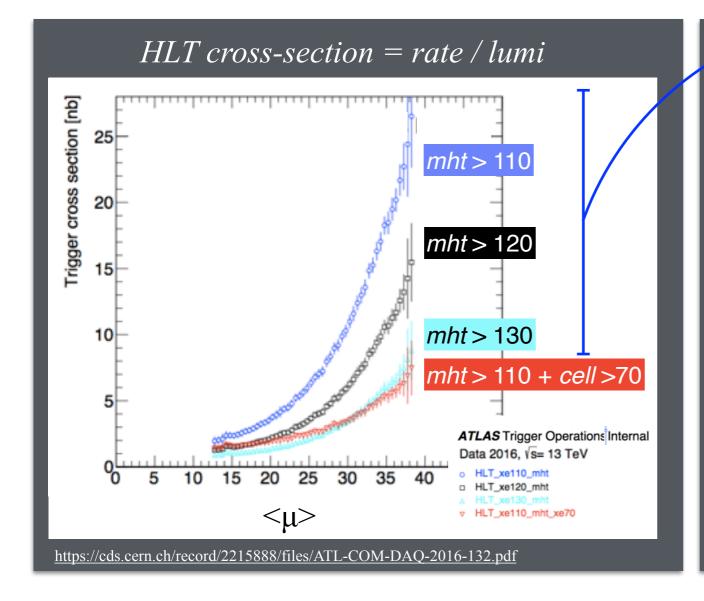
in 2016

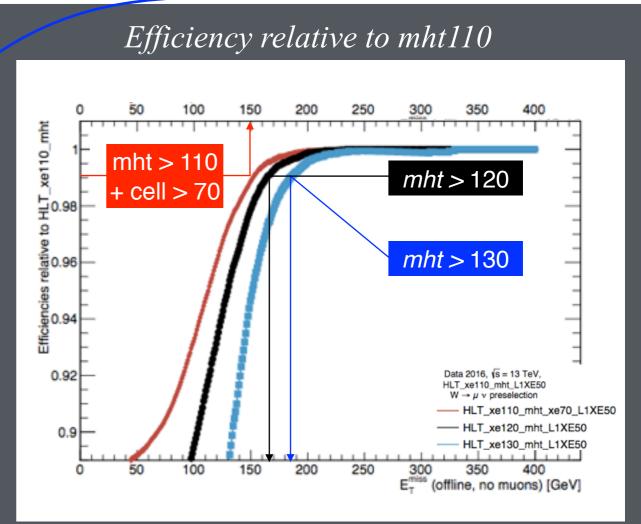
mht110 (default for post-CHEP 2016)

• Rate for $\mu > 45-50$ too high, see left plot

We found backup: $mht110 + cell70^*$, but kept mht110

- The performance is much better when mht is combined with cell MET
- Efficiency is better compared to *mht*130, see right plot[^]





At HLT: Smarter (2017)

χ² based "pileup fit" algorithm

Algorithm

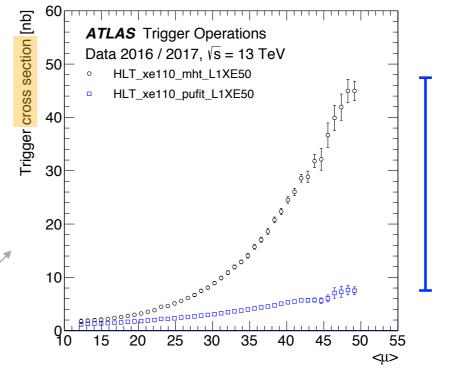
- Divide η-φ space in ~0.4² grid
- Assume uniform underlying pileup energy in η-φ, float magnitude given momentum conservation in xy

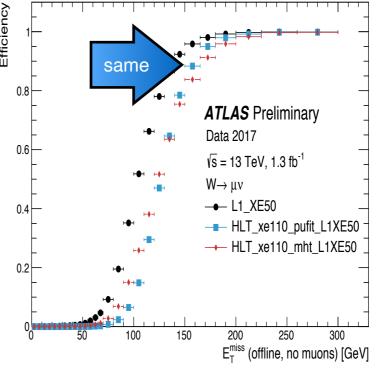
Result

- Trigger rate drastically reduced
- Signal efficiency is similar

Algorithm & threshold evolution

Rapid development





Year	Trigger name	HLT algorithm	L1 threshold	HLT threshold	$\int \mathcal{L} dt$
		[GeV]	[GeV]	[GeV]	$[fb^{-1}]$
2015	HLT_xe70_mht_L1XE50	mht	50	70	3.5
2016	HLT_xe90_mht_L1XE50	mht	50	90	12.7
2016	HLT_xe110_mht_L1XE50	mht	50	110	30.0
2017	HLT_xe90_pufit_L1XE50	pufit,cell	50	90, 50	21.8



At HLT: Combo (2018)

Use combinations of algorithms

Algorithm

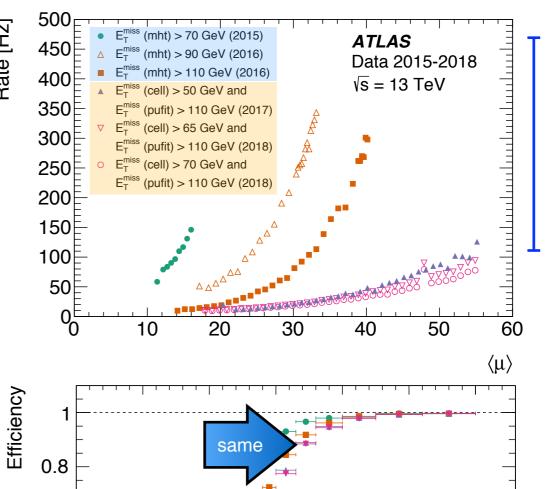
- χ^2 based algorithm from prev. slide
- Cell-based algorithm using ~200k LAr cells
- Use both algorithms!

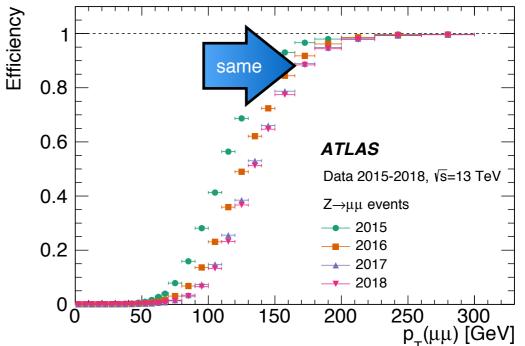
Result

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Algorithm & threshold evolution

Rapid development





Year	Trigger name	HLT algorithm	L1 threshold	HLT threshold	$\int \mathcal{L} dt$
		[GeV]	[GeV]	[GeV]	$[fb^{-1}]$
2017	HLT_xe100_pufit_L1XE50	pufit,cell	50	100,50	33.0
2017	HLT_xe110_pufit_L1XE50(55)	pufit,cell	50 (55)	110,50	47.7
2018	HLT_xe110_pufit_xe65_L1XE50	pufit,cell	50	110,65	57.0
2018	HLT_xe110_pufit_xe70_L1XE50	pufit,cell	50	110,70	62.6



E_Tmiss trigger

Summary of the Run 2 history & my outlook on Run 3

Approach

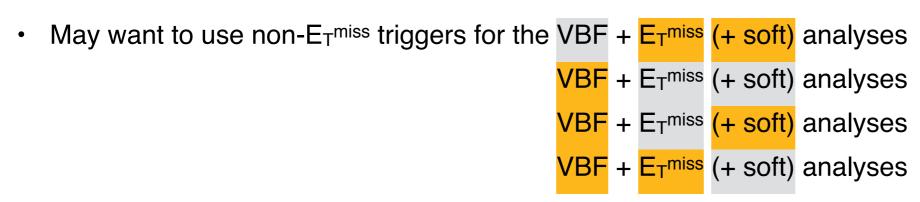
- Start data taking higher pileup than before ET^{miss} rates are too high threaten to raise thresholds Clever solutions
- Repeat every few months

Obvious question (& answer)

Why not pre-develop in advance? Rates are notoriously difficult to simulate

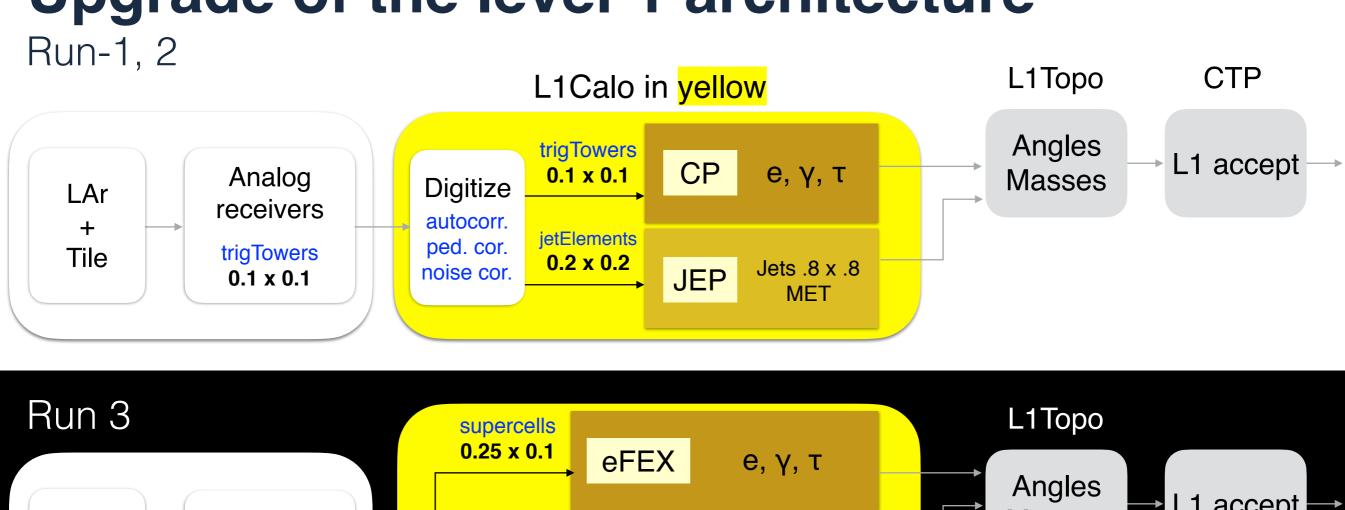
My view for Run 3

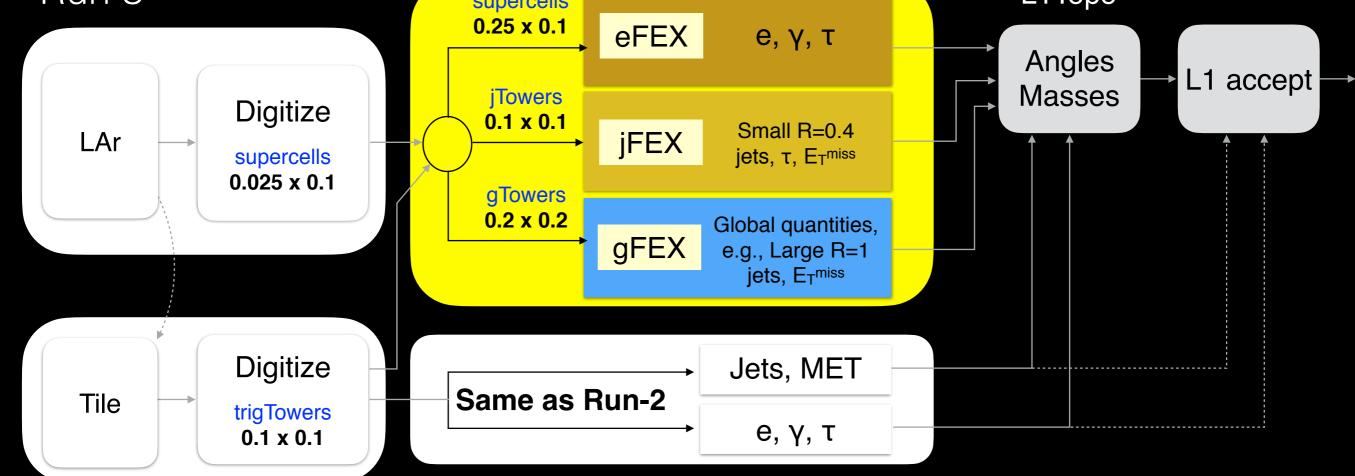
Keep a similar theme of innovating on algorithms, combining algorithms as we did in HLT





Upgrade of the level-1 architecture



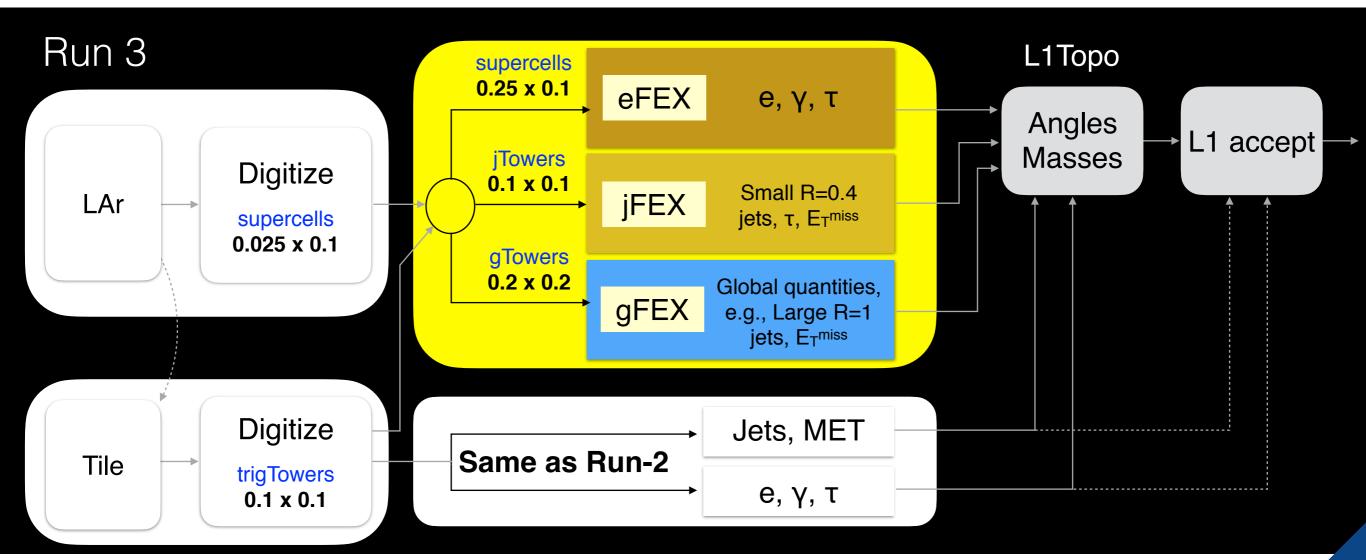


Run 3 architecture

My guess

More speculative

- We'll start with baseline E_Tmiss algorithms in jFEX-gFEX
- We'll take data and probably realize that we need to do better than baseline
- We'll probably improve & add jFEX-gFEX algorithms (like we did before in HLT)
- We'll combine jFEX-gFEX outputs (like we did before in HLT) → use ML?







Boosted decision trees



http://fwx.pitt.edu



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Nanosecond machine learning event classification with boosted decision trees in FPGA for high energy physics

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Department of Physics and Astronomy, University of Pittsburgh, 100 Allen Hall, 3941 O'Hara St., Pittsburgh, PA 15260, U.S.A.

E-mail: tmhong@pitt.edu

ABSTRACT: We present a novel implementation of classification using the machine learning/artificial intelligence method called boosted decision trees (BDT) on field programmable gate arrays (FPGA). The firmware implementation of binary classification requiring 100 training trees with a maximum depth of 4 using four input variables gives a latency value of about 10 ns, independent of the clock speed from 100 to 320 MHz in our setup. The low timing values are achieved by restructuring the BDT layout and reconfiguring its parameters. The FPGA resource utilization is also kept low at a range from 0.01% to 0.2% in our setup. A software package called fwxmachina achieves this implementation. Our intended user is an expert in custom electronics-based trigger systems in high energy physics experiments or anyone that needs decisions at the lowest latency values for real-time event classification. Two problems from high energy physics are considered, in the separation of electrons vs. photons and in the selection of vector boson fusion-produced Higgs bosons vs. the rejection of the multijet processes.

Keywords: Digital electronic circuits; Trigger algorithms; Trigger concepts and systems (hardware and software); Data reduction methods

ArXiv ePrint: 2104.03408

 $^* Corresponding \ author.$



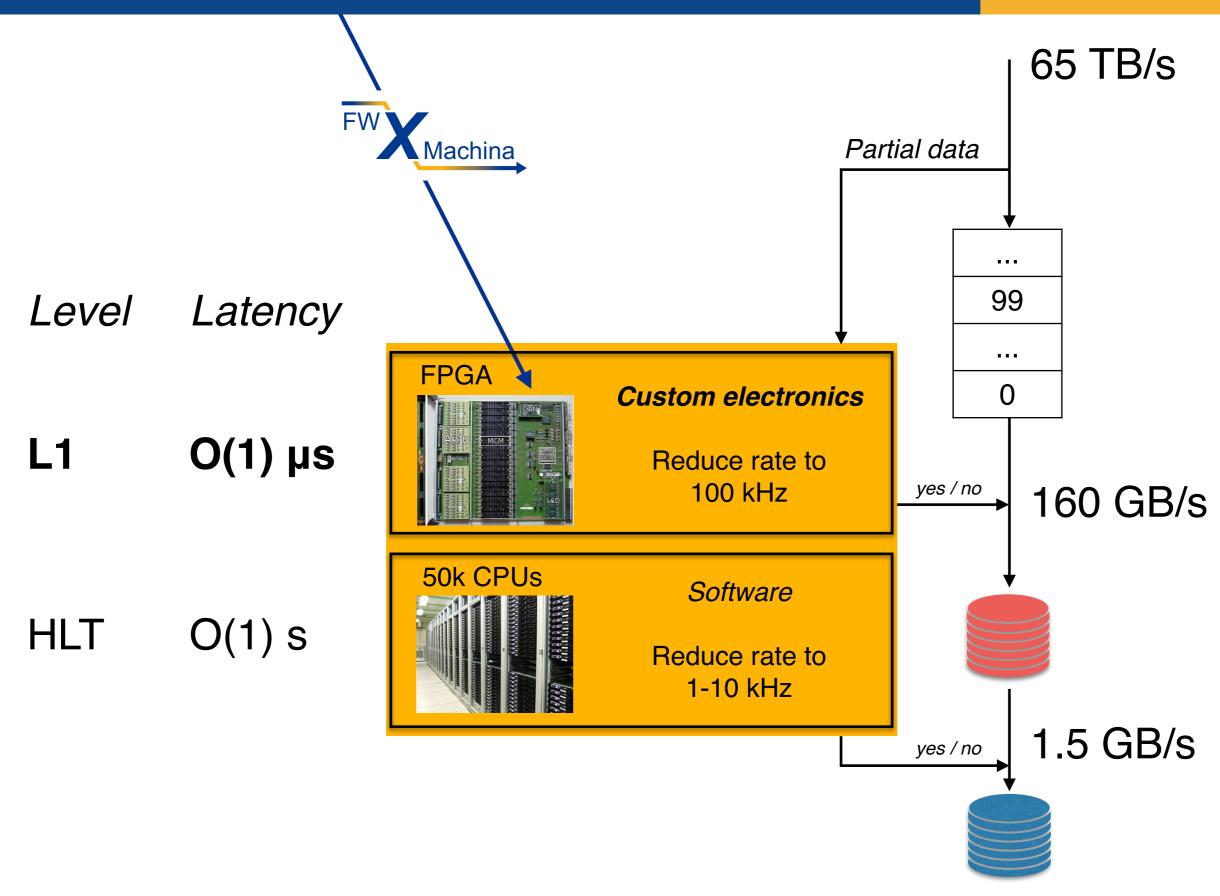
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https://doi.org/10.1088/1748-0221/16/08/P08016

Machine learning at L1 trigger









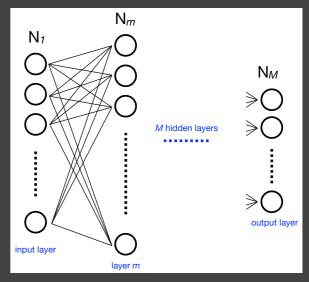
Deep Neural Network

- Popular method for signal vs. background
- But can't be very deep for FPGA, so ~3 "deep" in paper

•
$$y = \Theta(\mathbb{M} \cdot x + b)$$

Fancy Multiplication activation (limited resource on FPGA)

Duarte et al., <u>J. Instrum. 13, P07027 (2018)</u>



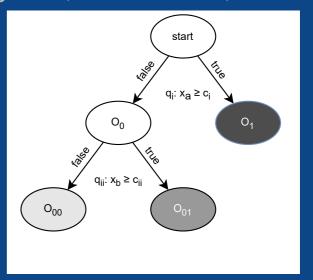
Standard Decision Tree

- Another popular classification
- $y = \Theta(x < \text{threshold})$ Boolean No multiplication

Decision Tree for FPGA

- Smart bit integer precision, bit shifting
- Flattened (also "deep")
- All variables processed in parallel
- One step algorithm, ns fast, tiny footprint

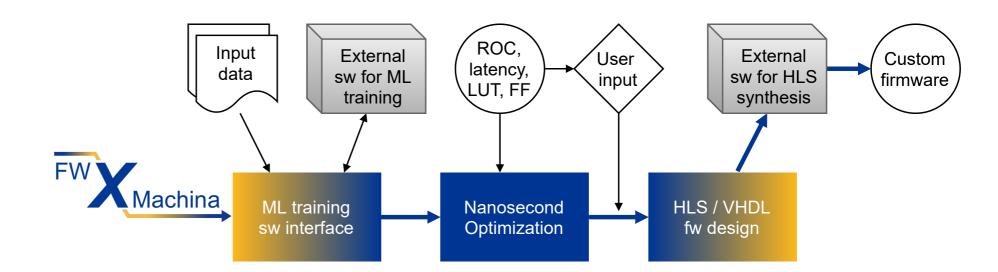
Hong et al., J. Instrum. 16, P08016 (2021)







Workflow



Optimization

Use bit integer precision



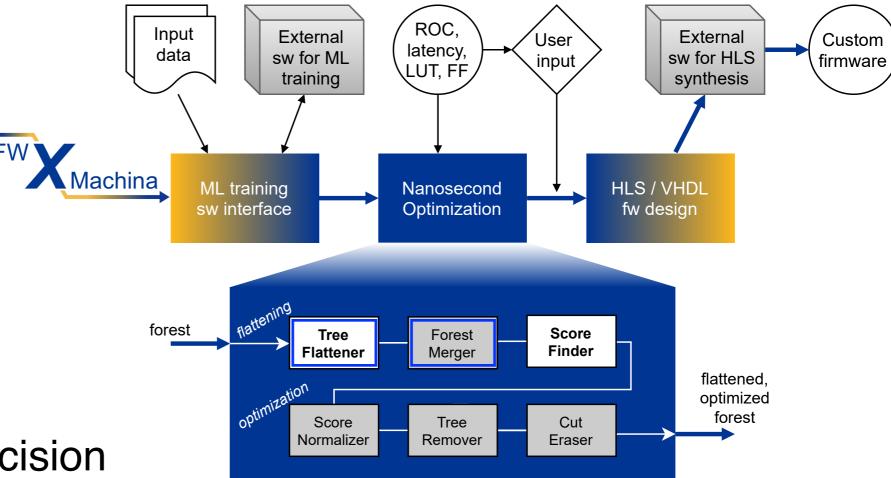
structure (2)



Workflow

Optimization

Use bit integer precision



Will discuss next:

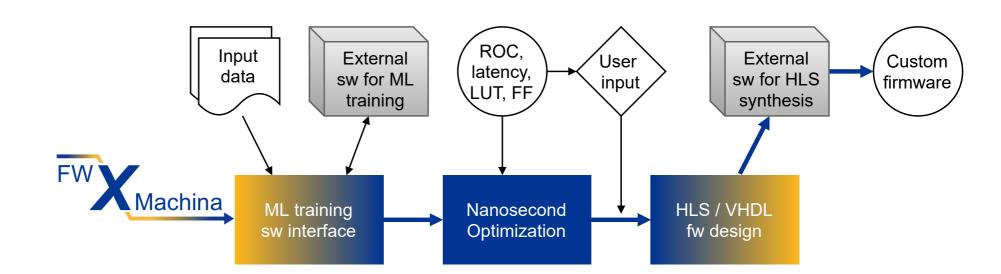
Tree Flattener

Forest Merger









Optimization

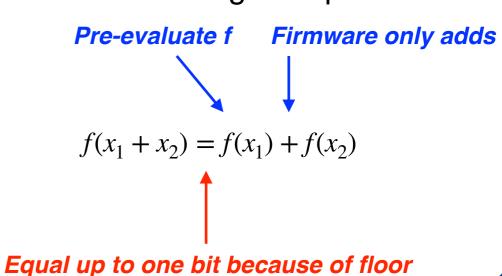
Use bit integer precision

E.g., ap_int(8) means the variable is represented by a range from 0 to 255.

Transformation
$$c_{\text{int}} = f(c_{\text{float}}) = \left[\frac{c_{\text{float}} - c_{\min}}{c_{\max} - c_{\min}} \cdot \left(2^N - 1\right)\right]$$
Floor operation

Advantages & subtleties

Bit integers represents a wide range without sacrificing float precision



Decision tree, 2 var example



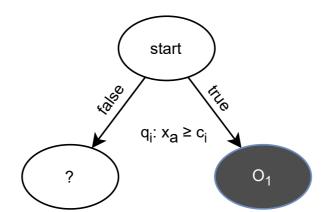




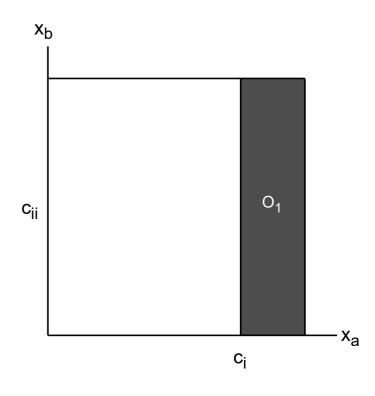


Root node

Depth i



2d plane: x_a vs. x_b



- Advantages & subtleties
 - Cut thresholds & weights determined during training
 - Danger of "memorizing" boundaries (overtraining), so must consider a forest

Decision tree, 2 var example (2)





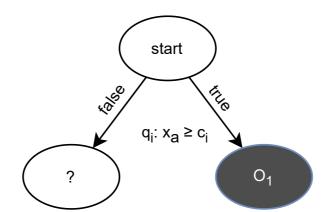
Conventional tree structure

IVI I IOI IG

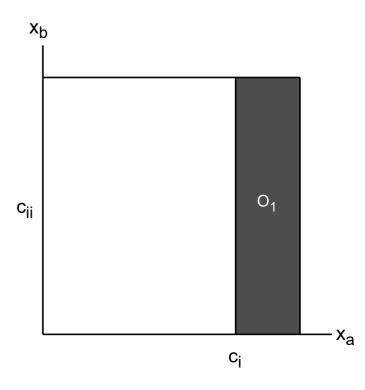
First step

Root node

Depth i

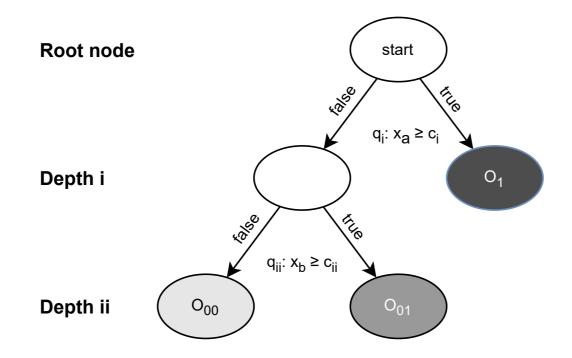


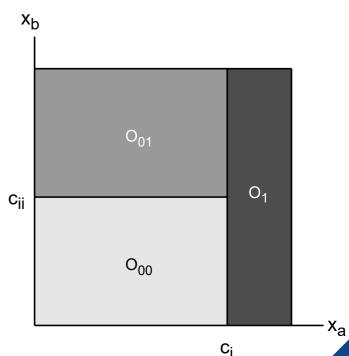
2d plane: x_a vs. x_b



- Advantages & subtleties
 - Deterministic, conventional style
 - · Cuts in each axis is not independent of each other, so recursive

Full tree



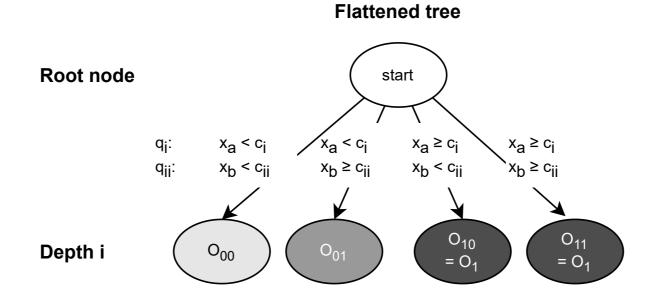


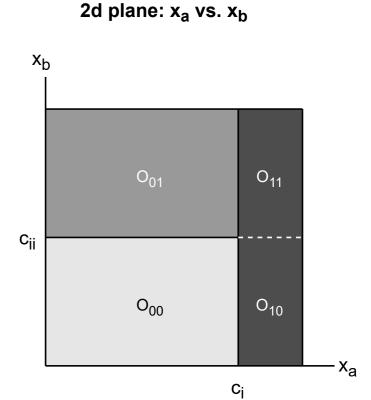
Decision tree, 2 var example (3)





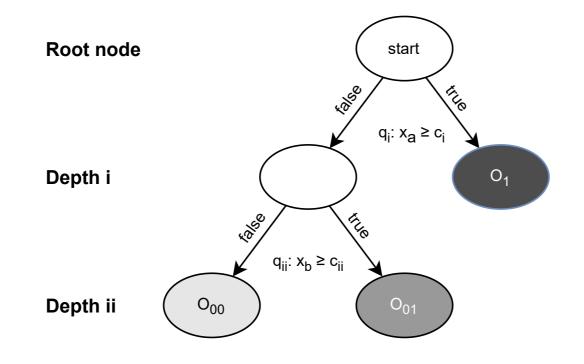


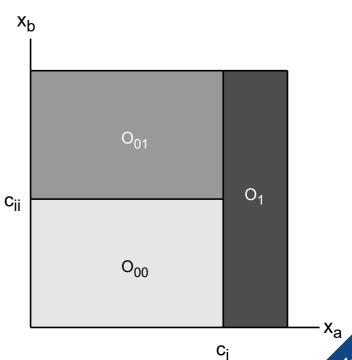




- Advantages & subtleties
 - Each axis is independent of each other → Bin search problem on a grid
 - Does not scale well for very deep trees (but do you really need it at L1?)







Forest of <u>boosted</u> decision trees



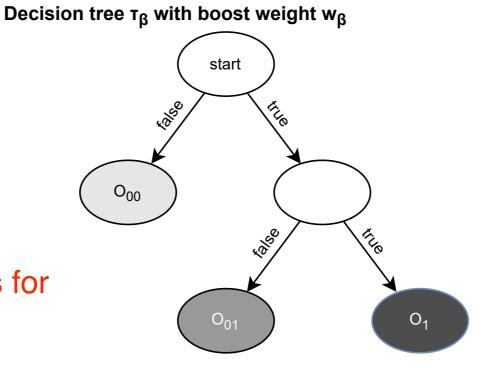


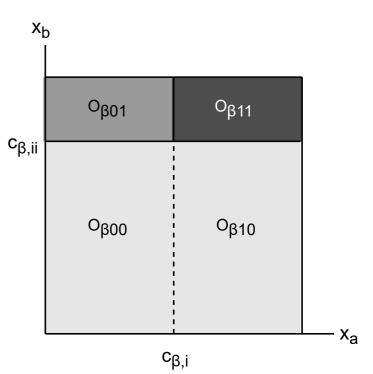
- Advantages & subtleties
 - Use TMVA software to train the BDT (support for other sw coming)

Our approach



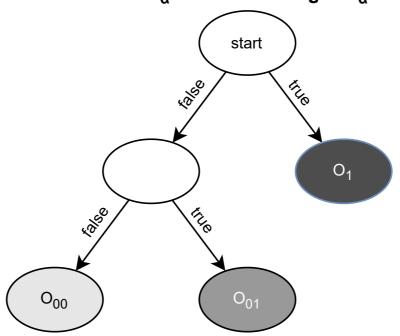
 Can we pre-merge the trees for firmware? Yes, next slide.

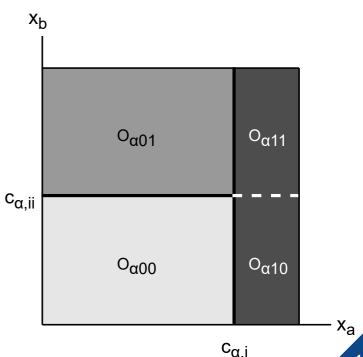




Decision tree τ_{α} with boost weight w_{α}

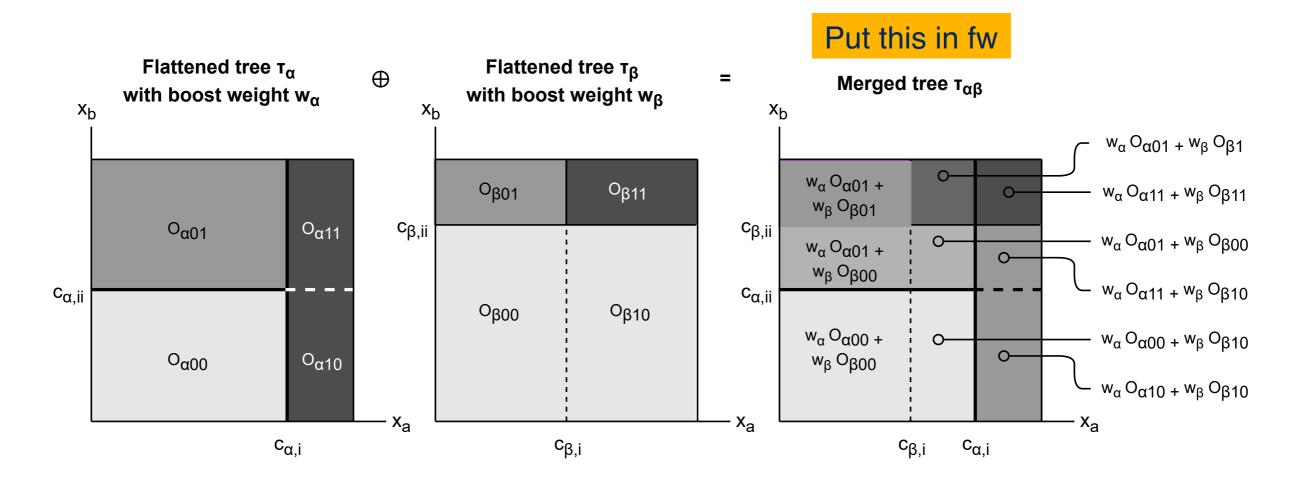






Merging of the forest





- Advantages & subtleties
 - Merging is pre-processed before implementation in firmware
 - This is using adaptive boosting. Gradient boosting cannot pre-merge, but we have approximations for that method to improve performance.
- Physics impact of flattening & merging
 - None, bec. encodes the entirety of conventional approach
 - Firmware is a giant look-up table problem

Physics: VBF Higgs vs. multijet





VBF Higgs vs. Multijet background

- $\sigma_{Higgs} = 4$ pb, two widely separated high-p_T jets
- $\sigma_{pp} = 80$ mb, dominant process at LHC
- Distributions given on the right

We consider two decays of the Higgs

- H → neutrinos, "invisible"
- H → bbbb, thru pseudoscalar decays

Strategy

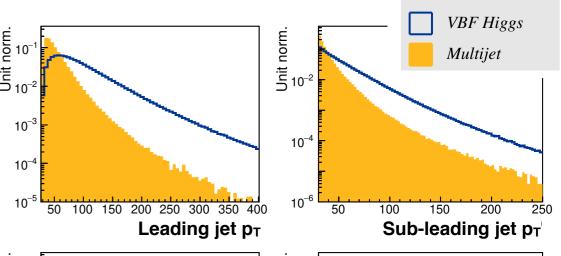
- Train BDT to identify VBF jet pair,
 i.e., train BDT on Multijet vs. VBF H → neutrinos 10-0 0.5
- Apply that BDT to Multijet vs. VBF H → bbbb

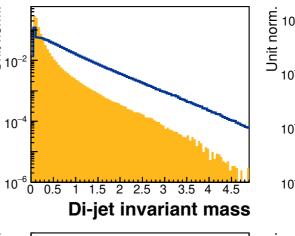
Why

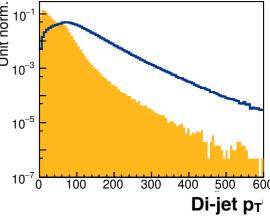
- If it works for VBF H → bbbb, then it can be a trigger for VBF independent of the Higgs decay
- Does it work? Next slide

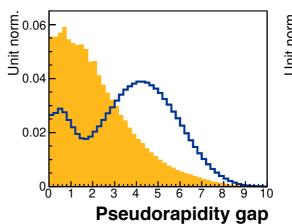


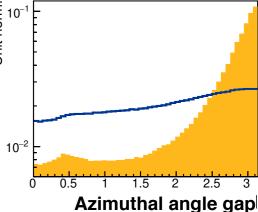
Samples













It works!

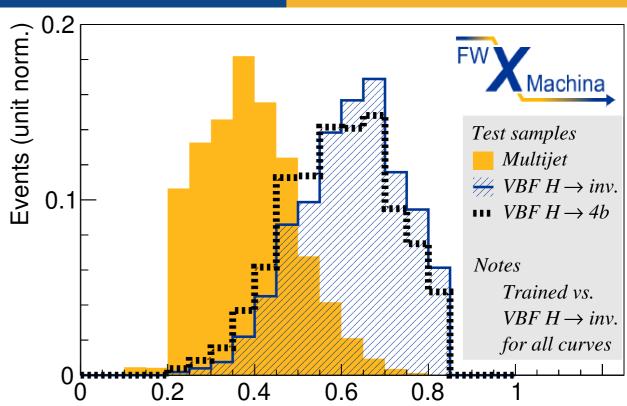
- Reminder. Did not train on VBF H → bbbb
- Subtlety re: jet selection (see paper)
- Distributions given on the right

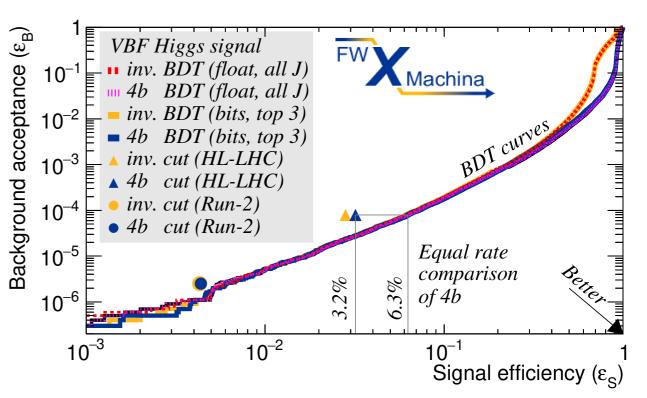
Performance comparison

- Try to mimic ATLAS HL-LHC cuts as best we can using Madgraph + Delphes
- Two-fold signal efficiency improvement from ATLAS-inspired → fwX results

Details

- We validated our setup to reproduce the signal efficiency in the ATLAS Run-2 paper
- Comparison using bit integers, not floats





Firmware: VBF Higgs vs. multijet





Ran two configurations

- Optimized version
- Non-optimized version (for comparison)
- Both using 100 trees, max depth of 4
- Results given on the right

Performance

- 5 clock ticks = 16 ns -
- Negligible resource usage

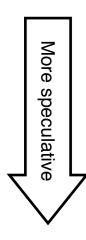
Benchmark using e+ vs. γ

- In the paper, we also define <u>one set</u> of parameters to scale up <u>one param. at a time</u>
- Uses 4 variables, 8 bits & same as above
- 3 clock ticks = 10 ns
- Negligible resource usage

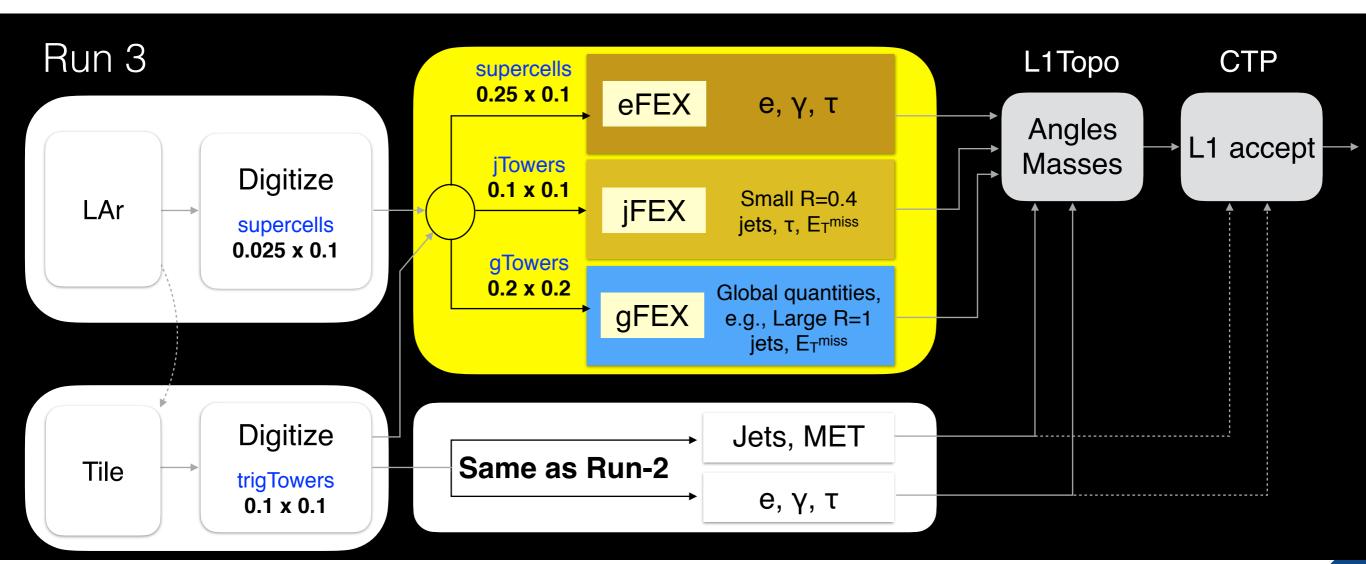
	VBF H Optimized	
N_{var}	5	7
N _{bit-var} N _{bit-score}	8 16	12 16
N_{bin}	40k	1M
Latency	5 ticks	6 ticks
LUT	1%	1.5%
Flip Flops	~0	~0
BRAM	2%	30%
DSP	0	~0



My guess



- L1Topo to do combo algorithms
- gFEX to develop new algorithms
- jFEX to develop new algorithms
- eFEX to develop new algorithms

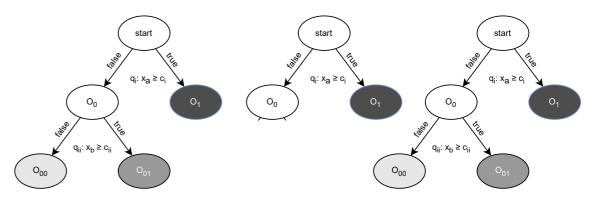


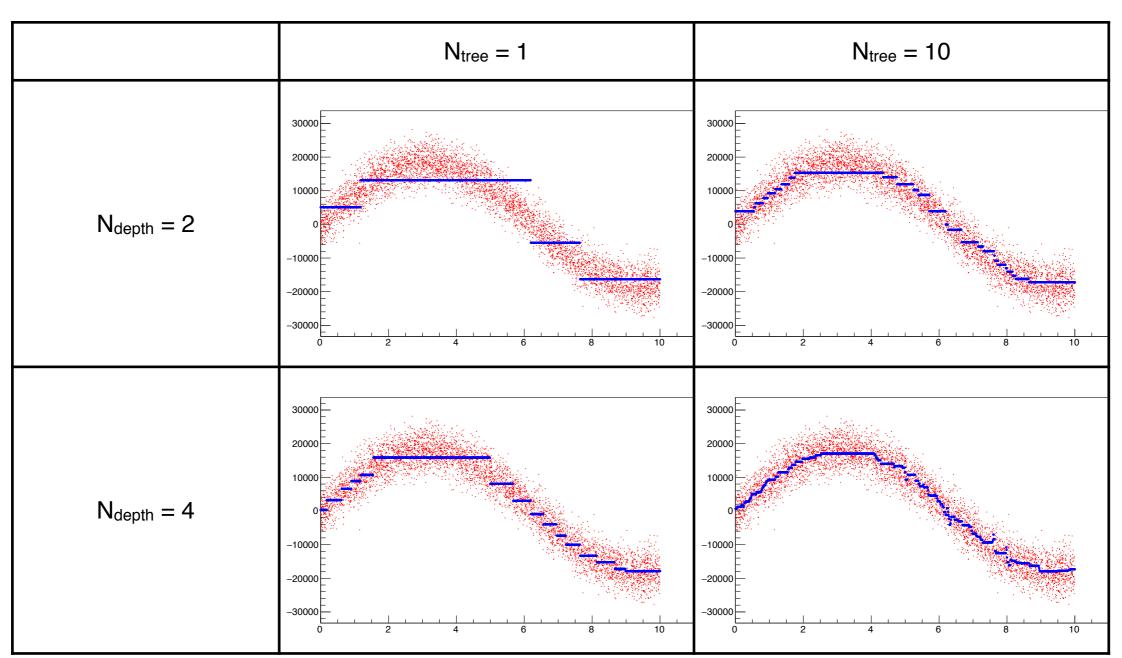
What about other ML? (we're working on it)

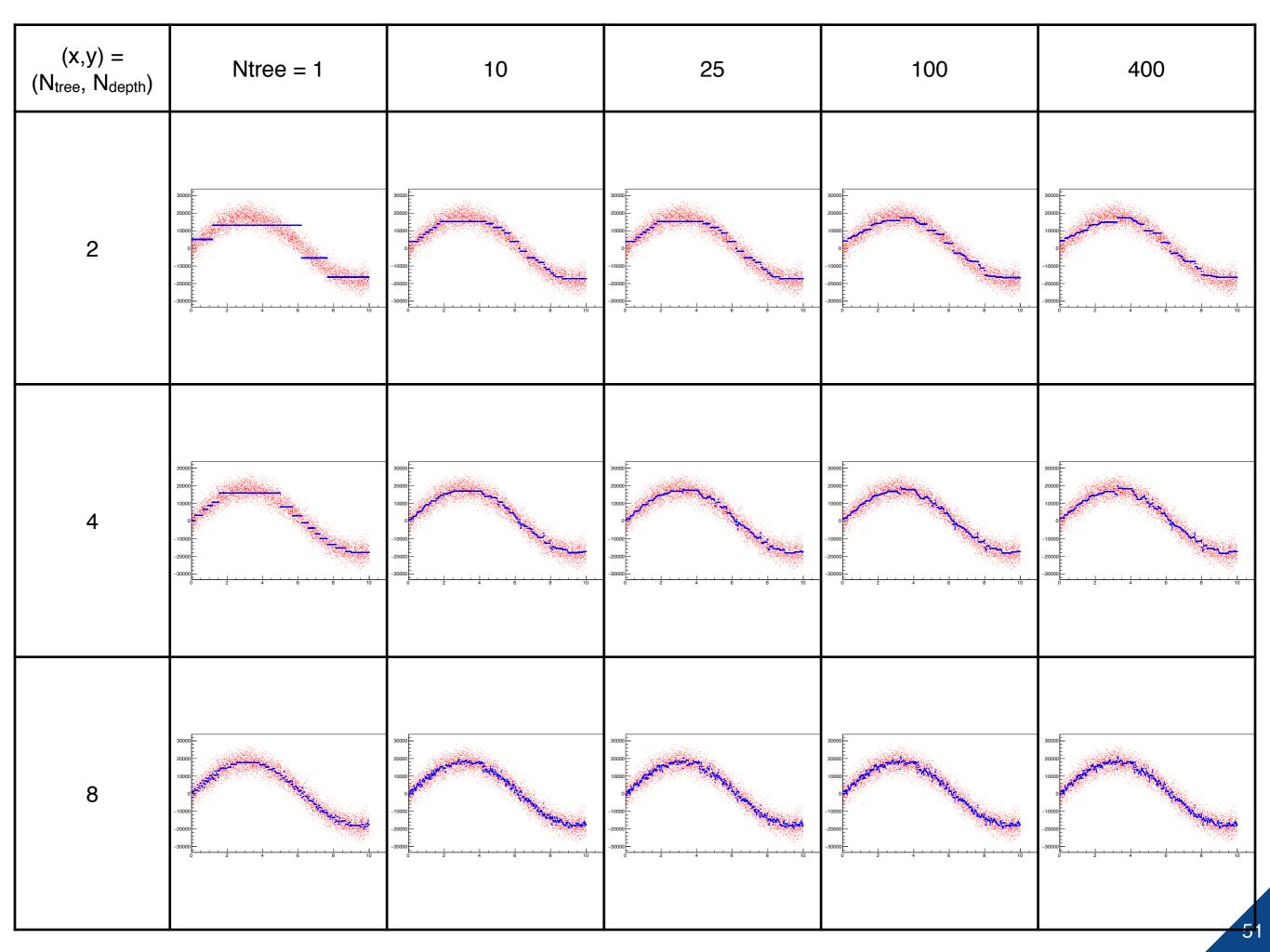


Regression (using BDT)

- Toy problem in 1-d
- Train / test on $f(x) = \sin(x) + Gaussian(x)$
- For sample of x: y = f(x) in 16 bits







Summary

Why (10 min)

- Higgs boson
- Dark sector

Method (20 min)

- H₁₂₅ → Dark matter pair B_{invisible} < 0.13
- H₁₂₅ → Dark photon + Y B_{dark photon} < 0.014

Trigger (30 min)

- E_Tmiss, VBF
- ML on FPGA

http://fwx.pitt.edu

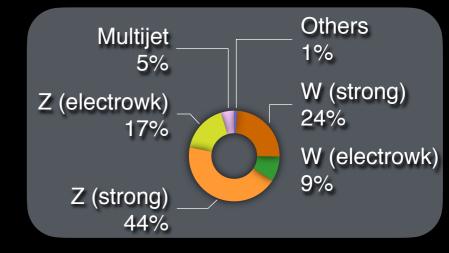


Abstract

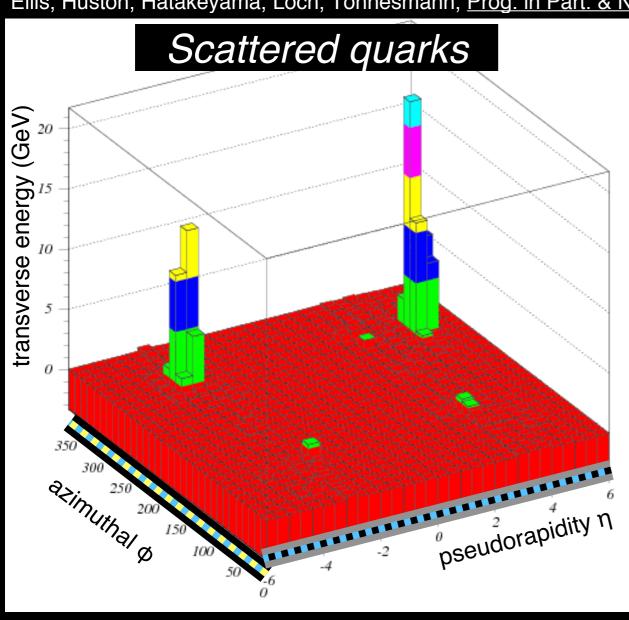
With more data coming from LHC collisions, detailed measurements of Higgs boson properties allow us to probe whether it communicates with the unknown and/or undiscovered sector beyond the Standard Model. One motivation is weakly interacting dark matter, which are invisible to the detecting apparatus, through a Higgs portal. I will discuss the latest ATLAS results of the search for Higgs bosons decaying to invisible particles. I will also describe the technical challenges of triggering on such events using missing energy from the Higgs boson decay and/or hadronic jets from the Higgs boson production, including the potential use of machine learning methods on FPGA boards in real-time level-1 trigger systems. will discuss how such interactions produce the recently discovered Higgs boson, and how it may serve as a portal to unknown sectors of elementary particles, such as dark matter. I will also describe the technical challenges of saving such minuscule fractions of weak force collisions, including the use of artificial intelligence in real-time trigger systems.

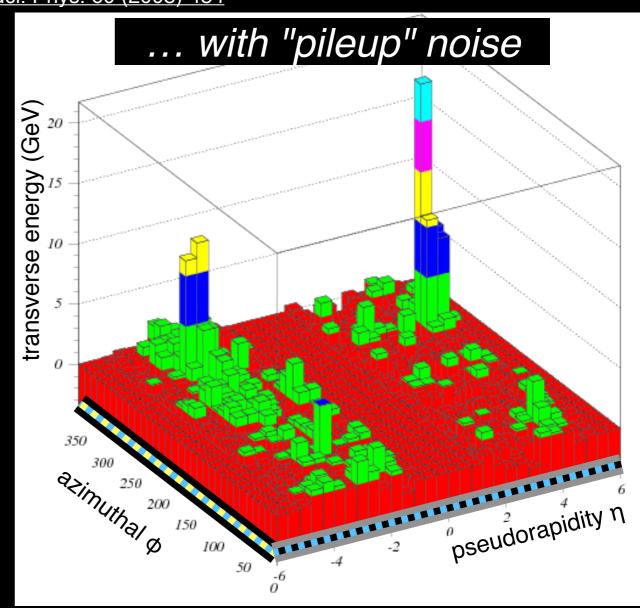
Distribution of energy

Simulation of the polar angle for one collision



Ellis, Huston, Hatakeyama, Loch, Tönnesmann, Prog. in Part. & Nucl. Phys. 60 (2008) 484







TM Hong

Detector signature



ATLAS geometry

- η along the beam direction
- ф azimuthal angle

VBF jet pair

- High p_T
- Wide gap in η
- Not back-to-back in φ
- Large m_{jet-jet}

2 TeV →

Low hadronic activity in between

• E_Tmiss

p_T imbalance

840 GeV →

• For +γ

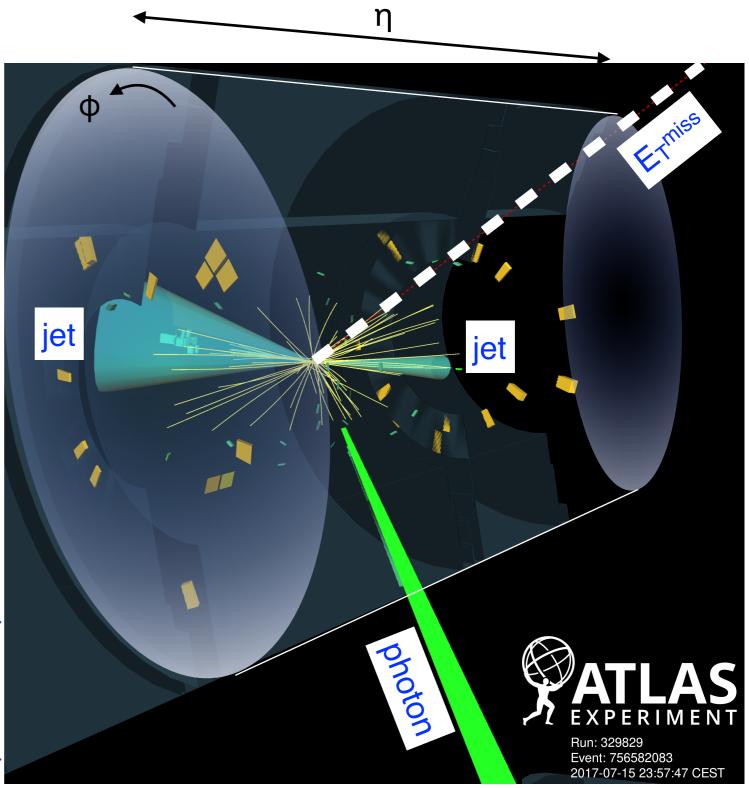
High-p_T photon

540 GeV -

• $m_T(E_T^{miss}, \gamma)$

1.1 TeV →

http://cern.ch/Atlas/GROUPS/PHYSICS/CONFNOTES/ATLAS-CONF-2021-004/fig_19.pdf



Signal models



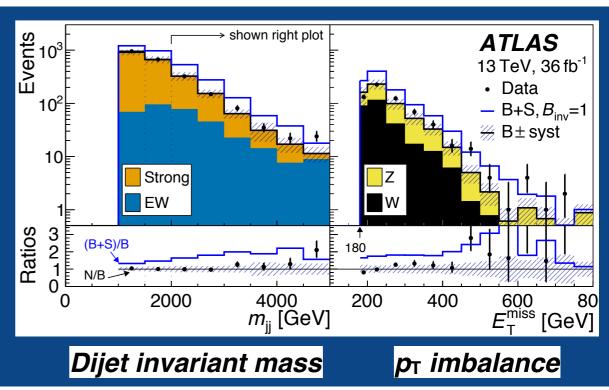


H portal to χ

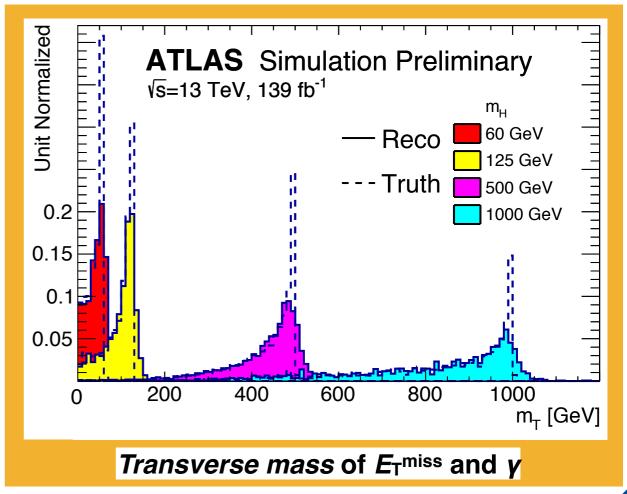
- VBF H₁₂₅
 w/ POWHEG NLO
- VBF H_{125} + γ_{ISR} w/ MG5_aMC@NLO
- S-to-B is higher with m_{jj}, E_T^{miss}, see →

H portal to γ_d

- VBF $H_{125} \rightarrow \gamma \gamma_{dark}$ w/ POWHEG v2
- m_T(E_T^{miss}, y) as proxy for m_H, see →



http://cern.ch/Atlas/GROUPS/PHYSICS/PAPERS/EXOT-2016-37/fig_05.pdf



Backgrounds, for +v





Weak boson bkg'd

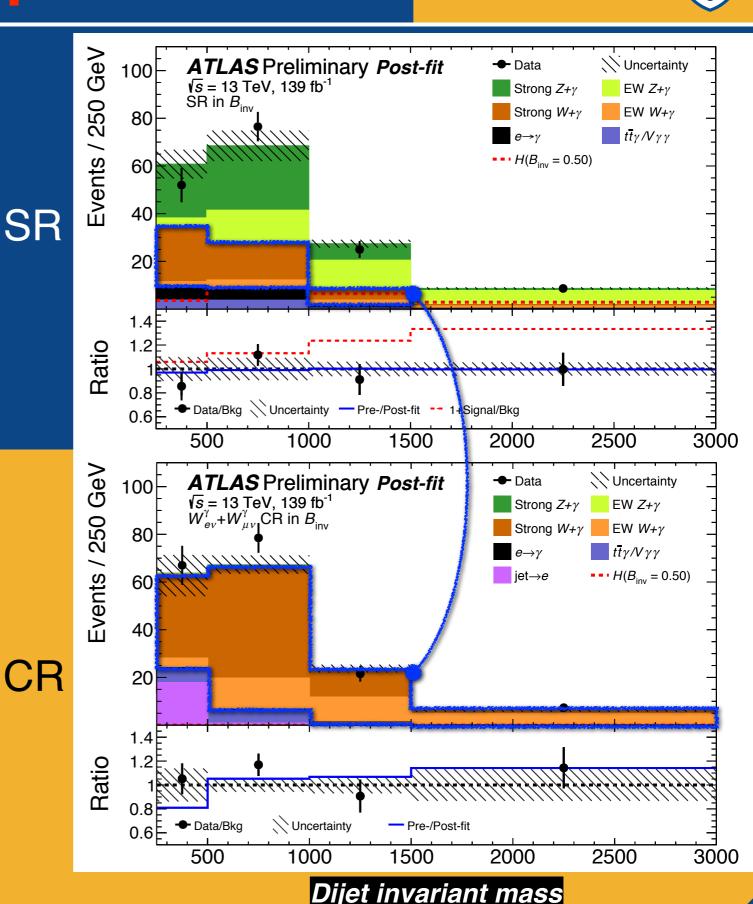
- Z → vv No leptons
- W → ℓv Loses a lepton

Signal Region

- E_Tmiss trigger, > 150 GeV
- "Centrality" of γ, 3rd jet
- For +γ_{ISR}, 15 < p_T^γ < 110 GeV
- For $+\gamma_{dark}$, $max(110,0.7 m_T)$

Control Region

- For W → ℓv, Require a lepton
- Lepton trigger, > 30 GeV
- Reverse γ centrality cut



Uncertainties, for +v



Statistical

- √N —
- MC

- Theoretical
 - Wγ, Zγ theory

- Experimental
 - JES, JER

1σ	Uncertainty on $\mathcal{B}_{ ext{inv}}$
-----------	--

	on $\mathcal{B}(H \to \gamma \gamma_{\rm d})$
--	---

Data stats.	0.106	0.0051
$V\gamma$ + jets theory	0.056	0.0028
MC stats.	0.045	0.0026
Jet Scale and Resolution	0.045	0.0011
Photon	0.032	0.0011
$e \rightarrow \gamma$, jet $\rightarrow e, \gamma$ Bkg.	0.026	0.0024
Pileup	0.025	0.0004
$W\gamma$ + jets/ $Z\gamma$ + jets Norm.	0.021	0.0005
$E_{ m T}^{ m miss}$	0.012	0.0003
Signal theory	0.004	0.0010
Lepton	0.002	0.0008
Total	0.148	0.0071

http://cern.ch/Atlas/GROUPS/PHYSICS/CONFNOTES/ATLAS-CONF-2021-004/tab_05.pdf

Evaluated by fixing parameters to their bestfit values and quadratically subtracting from the total nominal systematic uncertainty

MC samples for +y



Table 1: Summary of generators used for simulation. The details and the corresponding references are provided in the body of the text. The V in V+jets represents either a W or a Z boson.

Process	Generator	ME Order	PDF	Parton Shower	Tune
		Signal Samples			
ggF Higgs	Powheg v2 NNLOPS	NNLO	PDF4LHC15	Рутніа8.230	AZNLO
VBF Higgs+γ	MadGraph5_aMC@NLO 2.6.2	NLO	PDF4LHC15	Herwig 7.1.3p1	A14
ggF Higgs $\rightarrow \gamma \gamma_{\rm d}$	Powheg v2 NNLOPS	NNLO	PDF4LHC15	Рутніа8.244р3	AZNLO
VBF Higgs $\rightarrow \gamma \gamma_{\rm d}$	Powheg v2	NLO	CTEQ6L1	Рутніа8.244р3	AZNLO
	1	Background Samples			
Strong $V\gamma$ + jets	Sherpa v2.2.8	NLO (up to 1-jets), LO (up to 3-jets)	NNPDF3.0nnlo	SHERPA MEPS@NLO	Sherpa
EW $V\gamma$ + jets	MadGraph5_aMC@NLO 2.6.5	LO	NNPDF3.11o	Рутніа8.240	A14
EW VV+jets	Sherpa v2.2.1 or Sherpa v2.2.2	LO	NNPDF3.0nnlo	SHERPA MEPS@LO	SHERPA
VV+jets	Sherpa v2.2.1 or Sherpa v2.2.2	NLO (up to 1-jet), LO (up to 3-jets)	NNPDF3.0nnlo	SHERPA MEPS@NLO	SHERPA
EW V+ jets	Herwig 7.1.3 or Herwig 7.2.0	NLO	MMHT2014nlo68cl	Herwig 7.1.3	Herwig 7
Strong $W(\rightarrow \mu \nu) + \text{jets}/$ $W(\rightarrow \tau \nu) + \text{jets}$	Sherpa v2.2.8	NLO (up to 2-jets), LO (up to 4-jets)	NNPDF3.0nnlo	SHERPA MEPS@NLO	SHERPA
$tar{t}\gamma$	MadGraph5_aMC@NLO 2.2.3	NLO	NNPDF2.31o	Рутніа8.186	A14
$t\bar{t}$	PowhegBox v2	NLO	NNPDF3.0nlo	Рутніа8.230	A14
γ + jet	Sherpa v2.2.2	NLO (up to 2-jets), LO (up to 4-jets)	NNPDF3.0nnlo	SHERPA MEPS@NLO	SHERPA
		Systematic Samples			
$V\gamma$ + jets α^4 interference	MadGraph5_aMC@NLO 2.6.2	LO	NNPDF3.11o	Рутніа8.240	AZNLO

CR Fake_a CR

Signal region for +y



Table 3: Summary of the requirements defining the different regions considered in this analysis. Where present, the values in squared brackets are referring to the regions defined in the search for $H \to \gamma \gamma_d$ signal. The leading and subleading jets must satisfying the fJVT requirements mentioned in Sec. 5. In the SR and $Z_{\text{Rev.Cen.}}^{\gamma}$ CR definitions $E_{\text{T}}^{\text{miss,lep-rm}} \equiv E_{\text{T}}^{\text{miss}}$ since no lepton is present.

 W^{γ} CD W^{γ} CD Z^{γ}

	Variable	SK	$W'_{\mu\nu}$ CR	W'_{ev} CR	Z' _{Rev.Cen.} CR	Fake-e CR
→	$p_{\mathrm{T}}(j_1)$ [GeV]	> 60				
→	$p_{\mathrm{T}}(j_2)$ [GeV]	> 50				
	$N_{\rm jet}$	2,3				
	$N_{ ext{b-jet}}$	< 2				
→	$\Delta\phi_{ m ij}$	< 2.5 [2.0]				
→	$ \Delta \hat{\eta}_{ m jj} $	> 3.0				
	$\eta(j_1) \times \eta(j_2)$	< 0				
	C_3	< 0.7				
→	$m_{\rm jj}$ [TeV]	> 0.25				
ŕ	$E_{\rm T}^{\rm miss}$ [GeV]	> 150	_	> 80	> 150	< 80
→	$E_{\rm T}^{\rm miss,lep-rm}$ [GeV]	_	> 150	> 150	_	> 150
	$E_{\mathrm{T}}^{\mathrm{miss,lep-rm}}$ [GeV] $E_{\mathrm{T}}^{\mathrm{jets,no-jvt}}$ [GeV]	> 130				
	$\Delta \phi(j_i, E_{\mathrm{T}}^{\mathrm{miss,lep-rm}})$	> 1.0				
	N_{γ}	1				
	$p_{\mathrm{T}}^{\prime}(\gamma)$ [GeV]	$> 15, < 110 [> 15, < max(110,0.733 \times m_T)]$				
	C_{γ}	> 0.4	> 0.4	> 0.4	< 0.4	> 0.4
	$\Delta\phi(\gamma, E_{ m T}^{ m miss,lep-rm})$	> 1.8 [-]				
	N_ℓ	0	1μ	1 <i>e</i>	0	1 <i>e</i>
	$p_{\rm T}$ (ℓ) [GeV]	> 30				

8 variables fed to DNN

$$\Rightarrow \eta_{\gamma}, \eta_{j2}$$

http://cern.ch/Atlas/GROUPS/PHYSICS/CONFNOTES/ATLAS-CONF-2021-004/tab_03.pdf

centrality C_{γ} [102] is defined as

Variable

$$C_{\gamma} = \exp\left(-\frac{4}{(\eta_1 - \eta_2)^2}(\eta_{\gamma} - \frac{\eta_1 + \eta_2}{2})^2\right),\tag{1}$$