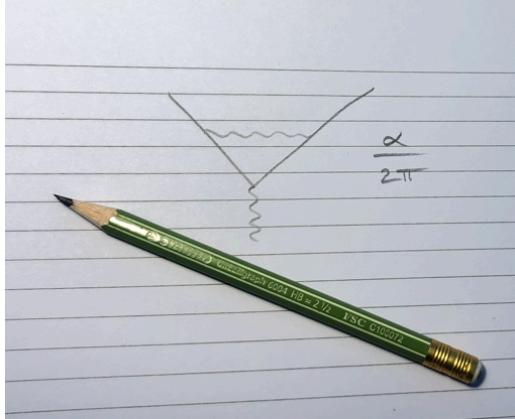


Muon g-2 \Leftrightarrow $\Delta\alpha$ connection

Massimo Passera
INFN Padova

Université de Genève
September 22 2021

Theory



?

≠

Experiment



- Incredibly high precision: like measuring the length of a soccer field with an uncertainty smaller than the width of a human hair!
- If SM ≠ EXP, then there must be new undiscovered physics!

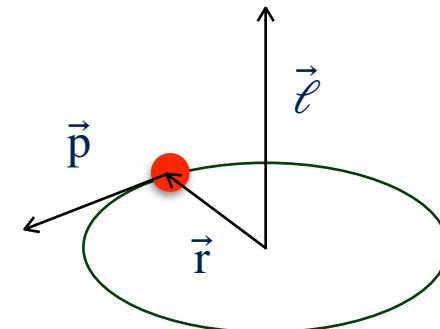
The magnetic moment of the muon

The motion of a classical particle of mass **m** and charge **e** with angular momentum

$$\vec{\ell} = \vec{r} \times \vec{p}$$

generates the (orbital) magnetic moment :

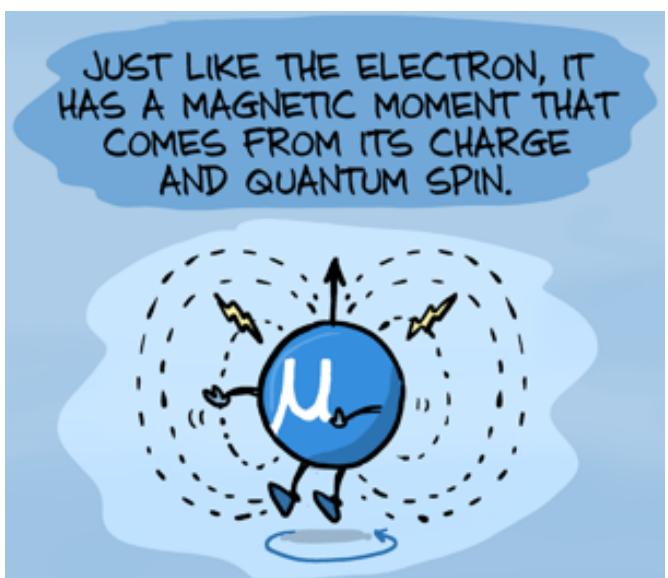
$$\vec{\mu}_\ell = \frac{e}{2m} \vec{\ell}$$



In 1925 Goudsmit & Uhlenbeck propose that the electron has an “internal rotation” characterised by a “spin” \vec{s} and an associated magnetic moment, like a tiny bar magnet:

$$\vec{\mu}_s = g \frac{e}{2m} \vec{s}$$

with **g = 2**, not 1! Very strange, but worked.



- 1928: Dirac's equation unifies the two fields that revolutionized XXth century physics: special relativity and quantum mechanics.

The Dirac equation predicts that a unit of spin interacts with a magnetic field twice as much as a unit of orbital angular momentum: $g=2$!

Great triumph for the Dirac equation, but not the end of the story...

- 1948: With improvements in experimental techniques, Kusch & Foley measure $g \neq 2$! The electron “magnetic moment anomaly” is:

$$a = (g-2)/2 = 0.00119(5)$$



What happened?? A relativistic quantum field theory of electromagnetism, ie Quantum ElectroDynamics (QED), is needed!

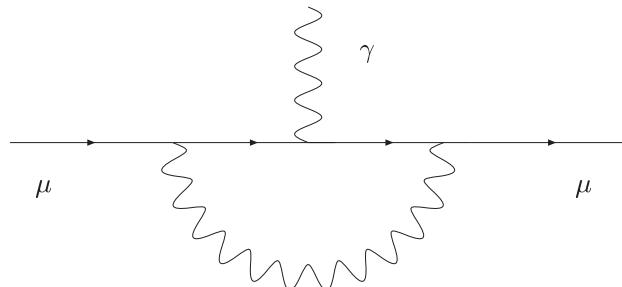
The QED prediction

- 1948: Schwinger, using Quantum ElectroDynamics (QED), predicts

$$a = (g-2)/2 = \alpha/(2\pi) = 0.00116$$

in perfect agreement with Kusch & Foley's measurement

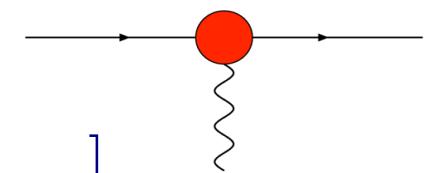
$$a = (g-2)/2 = 0.00119(5)$$



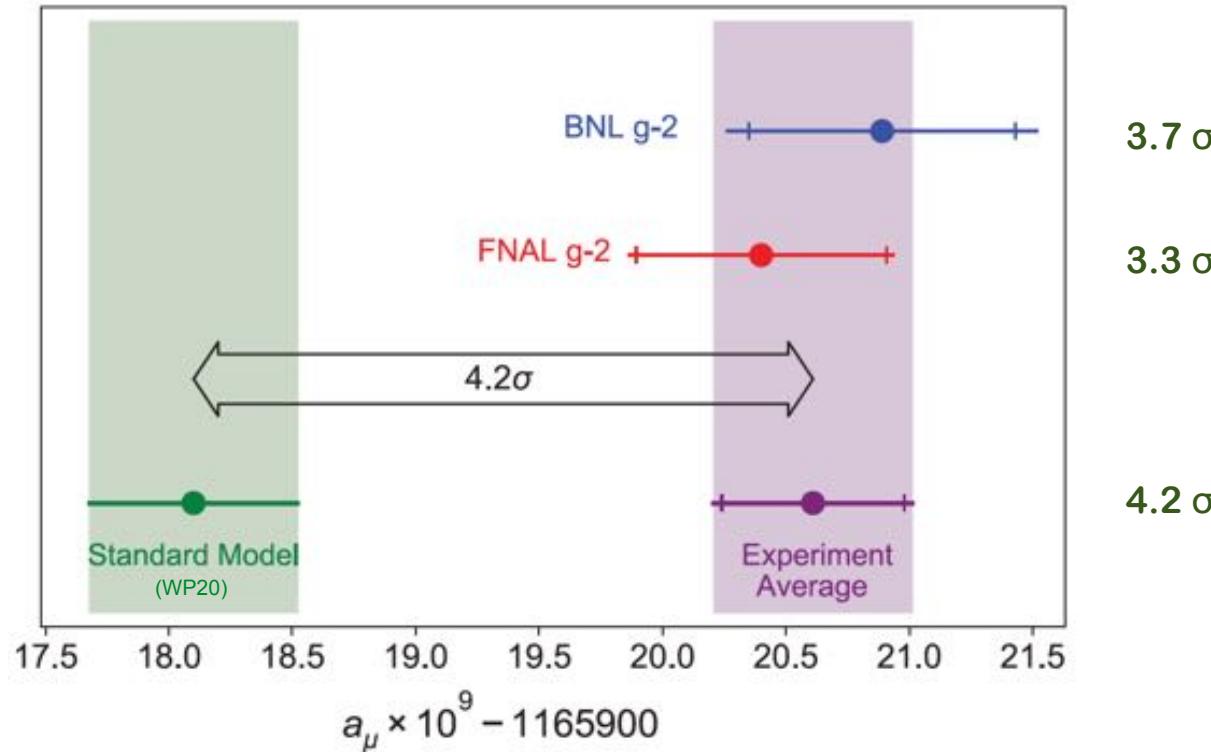
- Tremendous quantitative triumph for relativistic QFT (QED).
- Today we keep studying the lepton-photon vertex:

$$\Gamma^\mu = ie[\gamma^\mu F_1(q^2) + \frac{i\sigma^{\mu\nu}q_\nu}{2m}F_2(q^2) + \dots]$$

$$F_1(0) = 1 \quad F_2(0) = a$$



Muon g-2: FNAL confirms BNL



$$a_\mu^{\text{EXP}} = (116592089 \pm 63) \times 10^{-11} [0.54\text{ppm}] \quad \text{BNL E821}$$

$$a_\mu^{\text{EXP}} = (116592040 \pm 54) \times 10^{-11} [0.46\text{ppm}] \quad \text{FNAL E989 Run 1}$$

$$a_\mu^{\text{EXP}} = (116592061 \pm 41) \times 10^{-11} [0.35\text{ppm}] \quad \text{WA}$$

- FNAL aims at 16×10^{-11} . First 4 runs completed, 5th soon.
- Muon g-2 proposal at J-PARC: Phase-1 with \sim BNL precision.

- ➊ Muon g-2: the Standard Model prediction
- ➋ Muon g-2 \Leftrightarrow $\Delta\alpha$ connection
- ➌ The MUonE project

Muon g-2: the Standard Model prediction

WP20 = White Paper of the Muon g-2 Theory Initiative: arXiv:2006.04822

Muon g-2: the QED contribution

$$a_\mu^{\text{QED}} = (1/2)(\alpha/\pi) \quad \text{Schwinger 1948}$$

$$+ 0.765857426 (16) (\alpha/\pi)^2$$

Sommerfield; Petermann; Suura&Wichmann '57; Elend '66; MP '04

$$+ 24.05050988 (28) (\alpha/\pi)^3$$

Remiddi, Laporta, Barbieri ... ; Czarnecki, Skrzypek '99; MP '04;
Friot, Greynat & de Rafael '05, Ananthanarayan, Friot, Ghosh 2020

$$+ 130.8780 (60) (\alpha/\pi)^4$$

Kinoshita & Lindquist '81, ... , Kinoshita & Nio '04, '05;
Aoyama, Hayakawa, Kinoshita & Nio, 2007, Kinoshita et al. 2012 & 2015;
Steinhauser et al. 2013, 2015 & 2016 (all electron & τ loops, analytic);
Laporta, PLB 2017 (mass independent term) **COMPLETED²!**

$$+ 750.86 (88) (\alpha/\pi)^5 \text{ COMPLETED!}$$

Kinoshita et al. '90, Yelkhovsky, Milstein, Starshenko, Laporta,...

Aoyama, Hayakawa, Kinoshita, Nio 2012, 2015, 2017 & 2019.

Volkov 1909.08015: A₁⁽¹⁰⁾[no lept loops] at variance, but negligible $\delta a_\mu \sim 6 \times 10^{-14}$

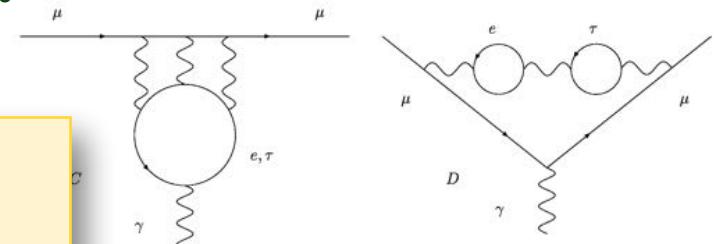
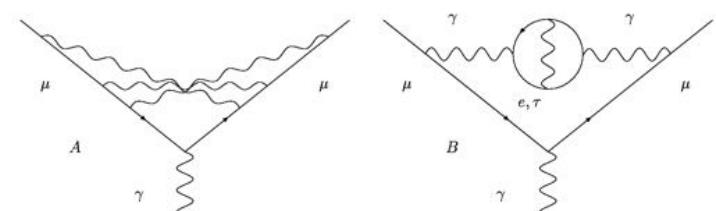
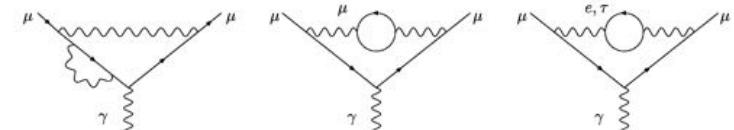
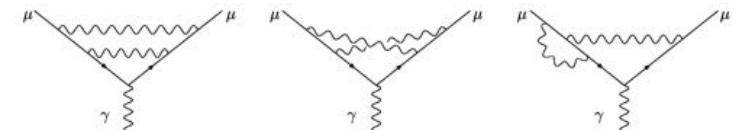
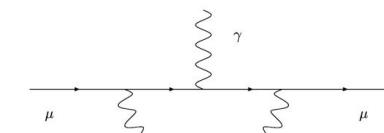
Adding up, we get:

$$a_\mu^{\text{QED}} = 116584718.931 (19)(100)(23) \times 10^{-11}$$

mainly from 4-loop coeff. unc. ↗ 6-loop ↘ from $a(\text{Cs})$

$a = 1/137.035999046(27)$ [0.2ppb] Parker et al 2018

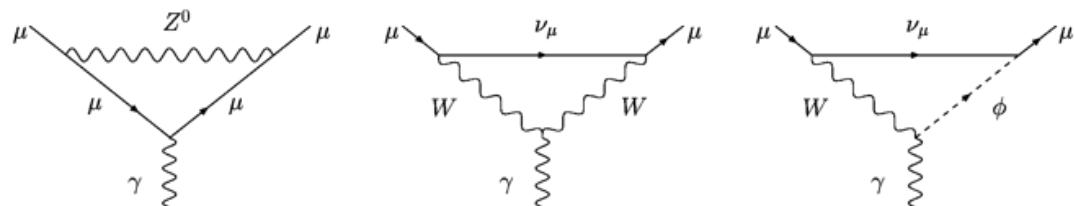
WP20 value



The electroweak contribution

μ

- One-loop term:



$$a_\mu^{\text{EW}}(\text{1-loop}) = \frac{5G_\mu m_\mu^2}{24\sqrt{2}\pi^2} \left[1 + \frac{1}{5} (1 - 4 \sin^2 \theta_W)^2 + O\left(\frac{m_\mu^2}{M_{Z,W,H}^2}\right) \right] \approx 195 \times 10^{-11}$$

1972: Jackiw, Weinberg; Bars, Yoshimura; Altarelli, Cabibbo, Maiani; Bardeen, Gastmans, Lautrup; Fujikawa, Lee, Sanda;
Studenikin et al. '80s

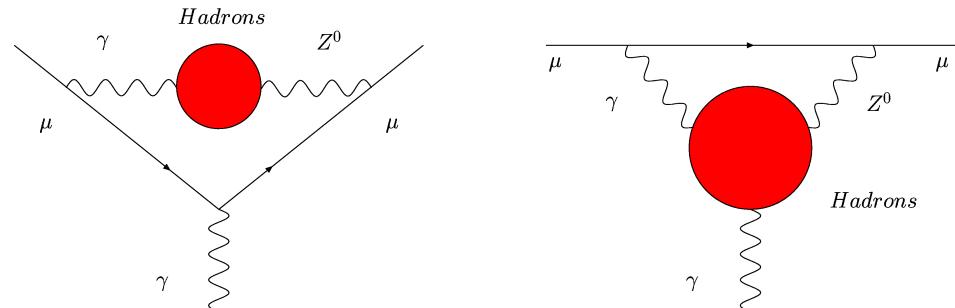
- One-loop plus higher-order terms:

$a_\mu^{\text{EW}} = 153.6 (1.0) \times 10^{-11}$

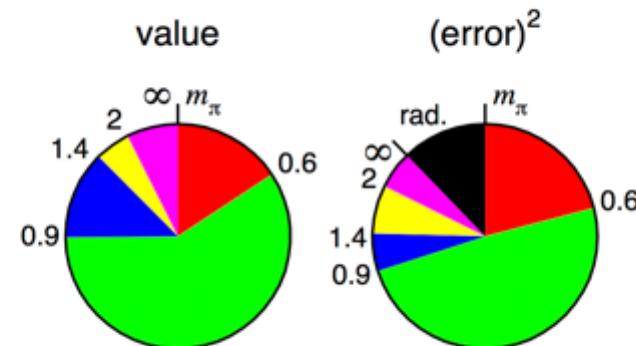
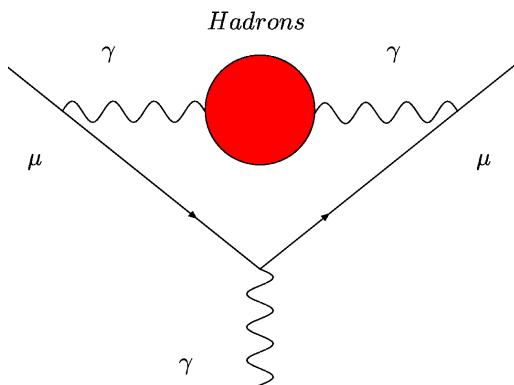
Kukhto et al. '92; Czarnecki, Krause, Marciano '95; Knecht, Peris, Perrottet, de Rafael '02; Czarnecki, Marciano and Vainshtein '02; Degrassi and Giudice '98; Heinemeyer, Stockinger, Weiglein '04; Gribouk and Czarnecki '05; Vainshtein '03; Gnendiger, Stockinger, Stockinger-Kim 2013, Ishikawa, Nakazawa, Yasui, 2019.

Hadronic loop uncertainties (and 3-loop nonleading logs).

WP20 value



The hadronic LO contribution



Keshavarzi, Nomura, Teubner 2018

$$a_\mu^{\text{HLO}} = \frac{1}{4\pi^3} \int_{m_\pi^2}^\infty ds K(s) \sigma_{\text{had}}^{(0)}(s)$$

$$K(s) = \int_0^1 dx \frac{x^2 (1-x)}{x^2 + (1-x) (s/m_\mu^2)}$$

$a_\mu^{\text{HLO}} = 6895 (33) \times 10^{-11}$

F. Jegerlehner, arXiv:1711.06089

$= 6939 (40) \times 10^{-11}$

Davier, Hoecker, Malaescu, Zhang, arXiv:1908.00921

$= 6928 (24) \times 10^{-11}$

Keshavarzi, Nomura, Teubner, arXiv:1911.00367

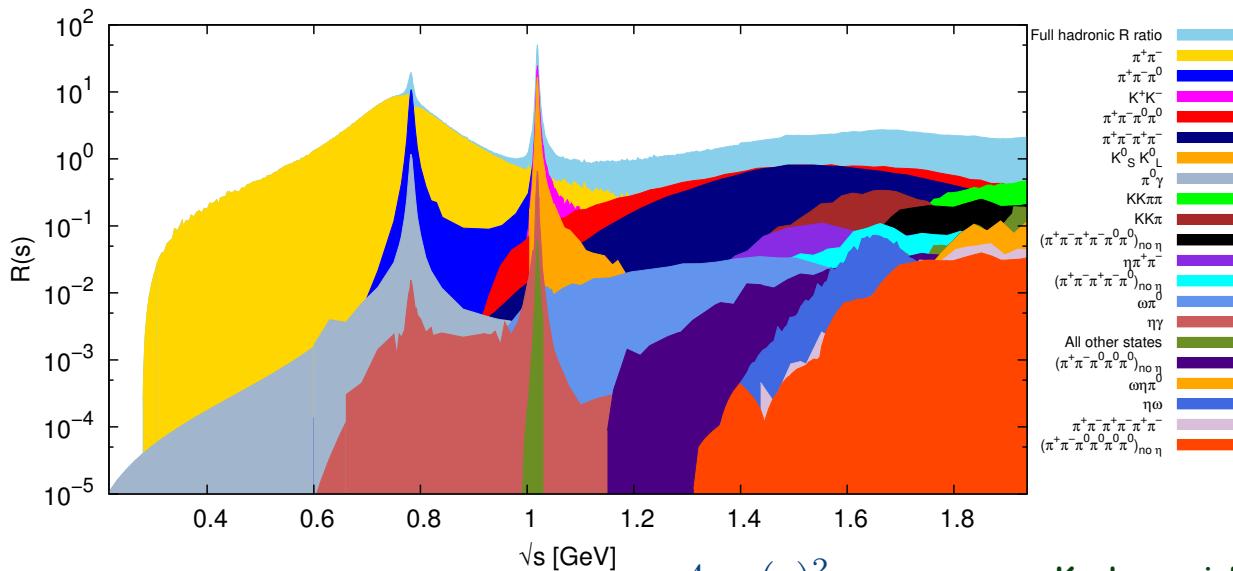
$= 6931 (40) \times 10^{-11} (0.6\%)$

WP20 value

- 🎙 **WP20 value obtained merging conservatively DHMZ + KNT + constraints from CHHKS**
Colangelo, Hoferichter, Hoid, Kubis, Stoffer 2018-19
- 🎙 **Radiative Corrections to $\sigma(s)$ are crucial.**
S. Actis et al, Eur. Phys. J. C66 (2010) 585

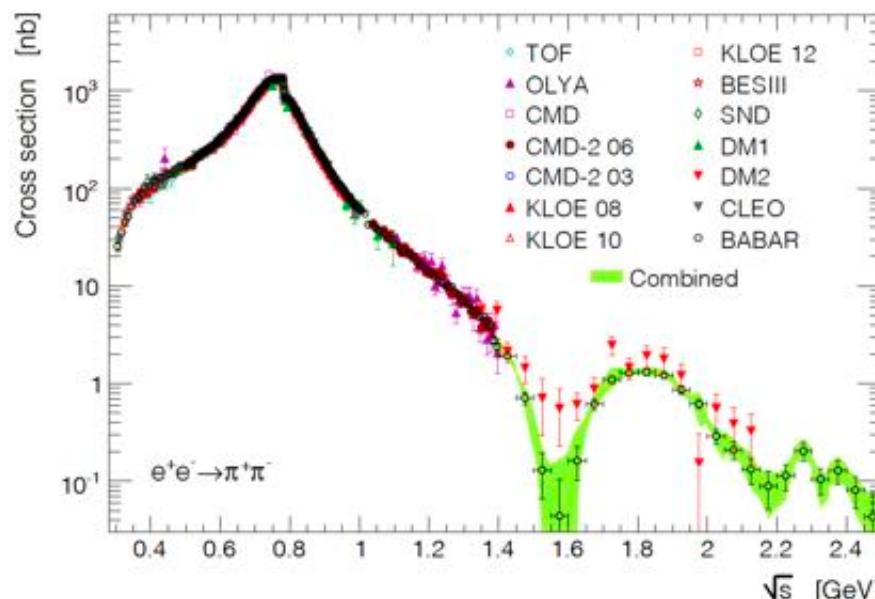
The low-energy hadronic cross section

μ



$$R(s) = \sigma(e^+e^- \rightarrow \text{hadrons}) / \frac{4\pi\alpha(s)^2}{3s}$$

Keshavarzi, Nomura Teubner
PRD 2018



Davier, Hoecker, Malaescu, Zhang
EPJC 2020

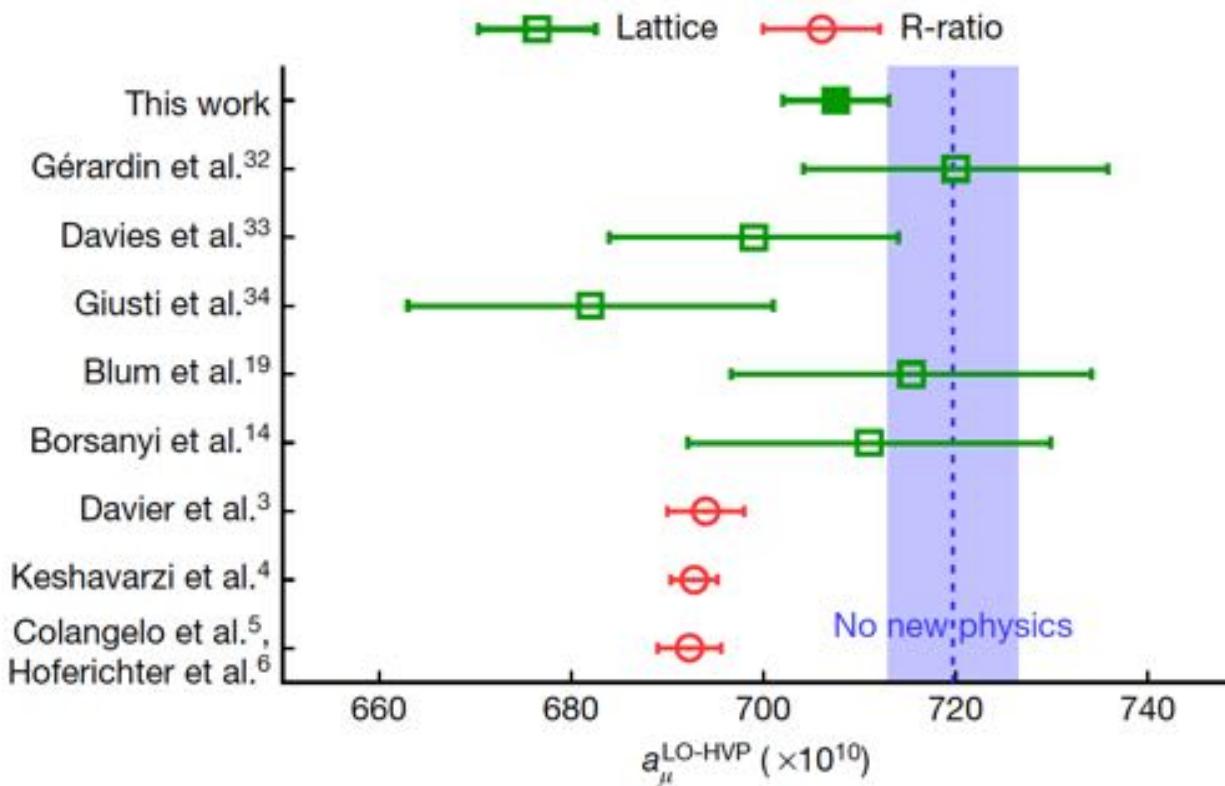
The hadronic LO contribution from lattice QCD

μ

- Great progress in lattice QCD results. The BMW collaboration reached 0.8% precision:

$$a_\mu^{\text{HLO}} = 7075(23)_{\text{stat}}(50)_{\text{syst}} [55]_{\text{tot}} \times 10^{-11}$$

- 2–2.5 σ tension with the dispersive evaluations. BMW collaboration 2021

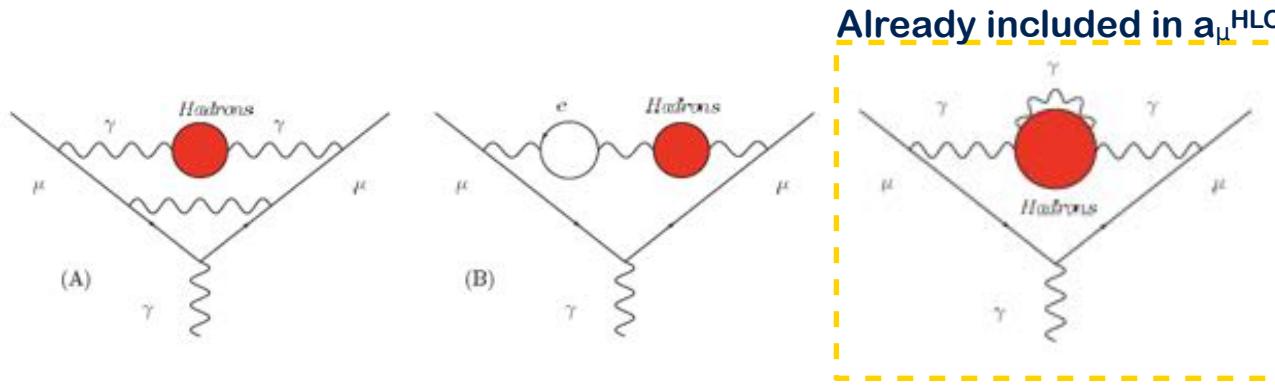


Borsanyi et al (BMWc), Nature 2021

The hadronic HO VP contribution

μ

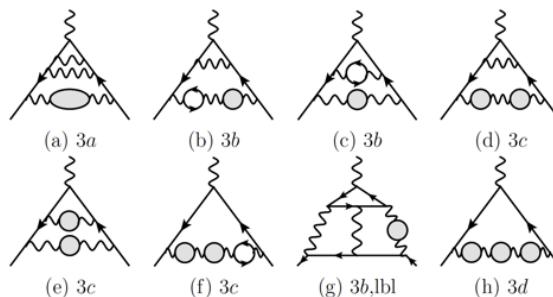
- $O(\alpha^3)$ contributions of diagrams containing HVP insertions:



$$a_\mu^{\text{HNLO(vp)}} = -98.3(7) \times 10^{-11}$$

Krause '96; Keshavarzi, Nomura, Teubner 2019; WP20.

- $O(\alpha^4)$ contributions of diagrams containing HVP insertions:



$$a_\mu^{\text{HNNLO(vp)}} = 12.4(1) \times 10^{-11}$$

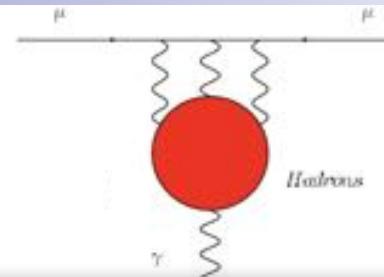
Kurz, Liu, Marquard, Steinhauser 2014

The hadronic LbL contribution

μ

- Hadronic light-by-light at $O(\alpha^3)$

- ⌚ This term had a troubled life! But nowadays:



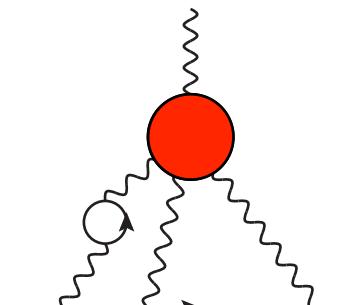
$$\begin{aligned} a_\mu^{\text{HNLO}}(|b|) &= 80 \text{ (40)} \times 10^{-11} && \text{Knecht \& Nyffeler '02} \\ &= 136 \text{ (25)} \times 10^{-11} && \text{Melnikov \& Vainshtein '03} \\ &= 105 \text{ (26)} \times 10^{-11} && \text{Prades, de Rafael, Vainshtein '09} \\ &= 100 \text{ (29)} \times 10^{-11} && \text{Jegerlehner, arXiv:1705.00263} \\ &= 92 \text{ (19)} \times 10^{-11} && \text{WP20 (phenomenology)} \end{aligned}$$

- ⌚ Significant improvements due to data-driven dispersive approach.
Colangelo, Hoferichter, Procura, Stoffer, 2014–17; Pauk, Vanderhaeghen 2014.
- ⌚ Lattice: RBC: $82(35)\times 10^{-11}$ 1911.08123 Mainz: $110(15)\times 10^{-11}$ 2104.02632

- Hadronic light-by-light at $O(\alpha^4)$

$$a_\mu^{\text{HNNLO}}(|b|) = 2 \text{ (1)} \times 10^{-11}$$

Colangelo, Hoferichter, Nyffeler, MP, Stoffer 2014; WP20



- Comparing the SM prediction with the measured muon g-2 value:

$$a_\mu^{\text{EXP}} = 116592061 (41) \times 10^{-11}$$

BNL+FNAL

$$a_\mu^{\text{SM}} = 116591810 (43) \times 10^{-11}$$

WP20

$$\Delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = 251 (59) \times 10^{-11}$$

4.2 σ

If BMW 2021 HLO instead of WP20, EXP & SM differ only by 1.6σ

- Is Δa_μ due to new physics beyond the SM? Could be due to:
 - NP at the weak scale and weakly coupled to SM particles
 - NP very heavy and strongly coupled to SM particles
 - NP very light ($\Lambda \lesssim 1$ GeV) and feebly coupled to SM particles

Muon g-2 \iff $\Delta\alpha$ connection

Marciano, MP, Sirlin 2008 & 2010

Keshavarzi, Marciano, MP, Sirlin 2020

- Can Δa_μ be due to missing contributions in the hadronic $\sigma(s)$?
- An upward shift of $\sigma(s)$ also induces an increase of $\Delta a_{\text{had}}^{(5)}(M_Z)$.
- Consider:

$$\begin{aligned} a_{\mu^{\text{HLO}}} &\rightarrow a = \int_{4m_\pi^2}^{s_u} ds f(s) \sigma(s), \quad f(s) = \frac{K(s)}{4\pi^3}, \quad s_u < M_Z^2, \\ \Delta a_{\text{had}}^{(5)} &\rightarrow b = \int_{4m_\pi^2}^{s_u} ds g(s) \sigma(s), \quad g(s) = \frac{M_Z^2}{(M_Z^2 - s)(4\alpha\pi^2)}, \end{aligned}$$

and the increase

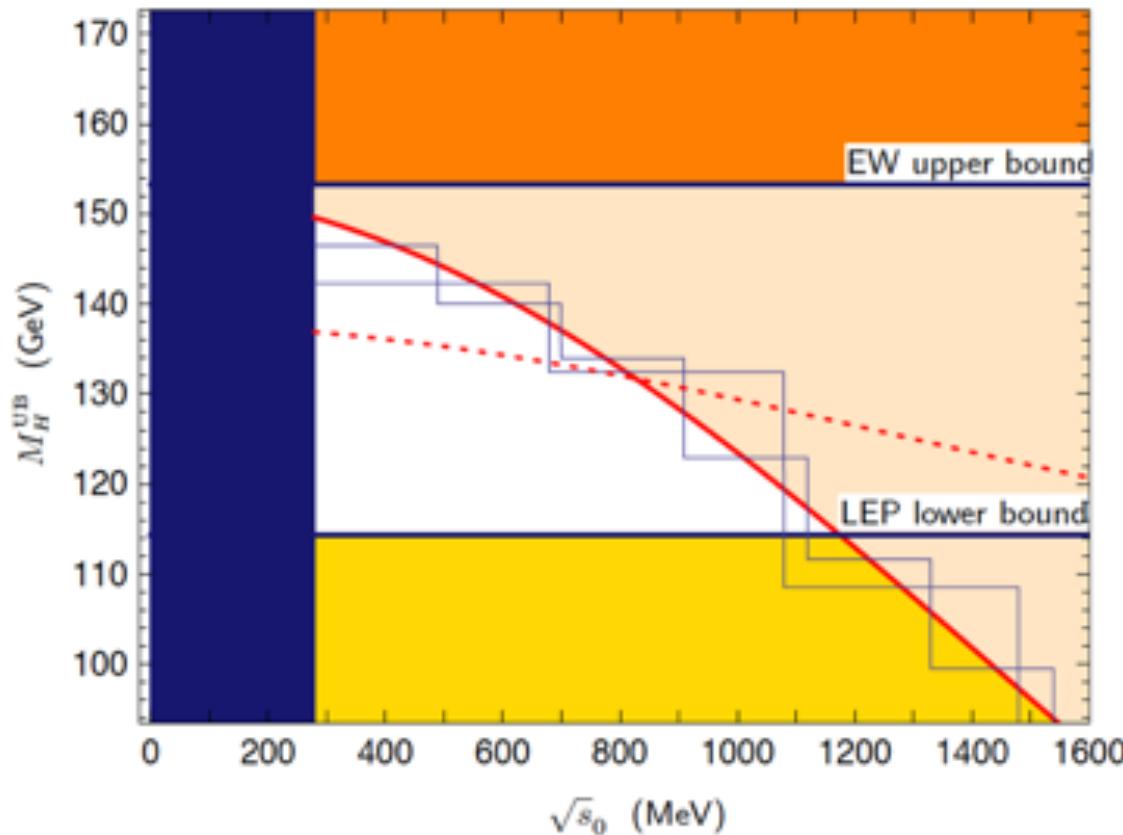
$$\Delta\sigma(s) = \epsilon\sigma(s)$$

$\epsilon > 0$, in the range:

$$\sqrt{s} \in [\sqrt{s_0} - \delta/2, \sqrt{s_0} + \delta/2]$$



How much does the M_H upper bound from the EW fit change when we shift up $\sigma(s)$ by $\Delta\sigma(s)$ [and thus $\Delta\alpha_{\text{had}}^{(5)}(M_Z)$] to fix $\Delta\alpha_\mu$?

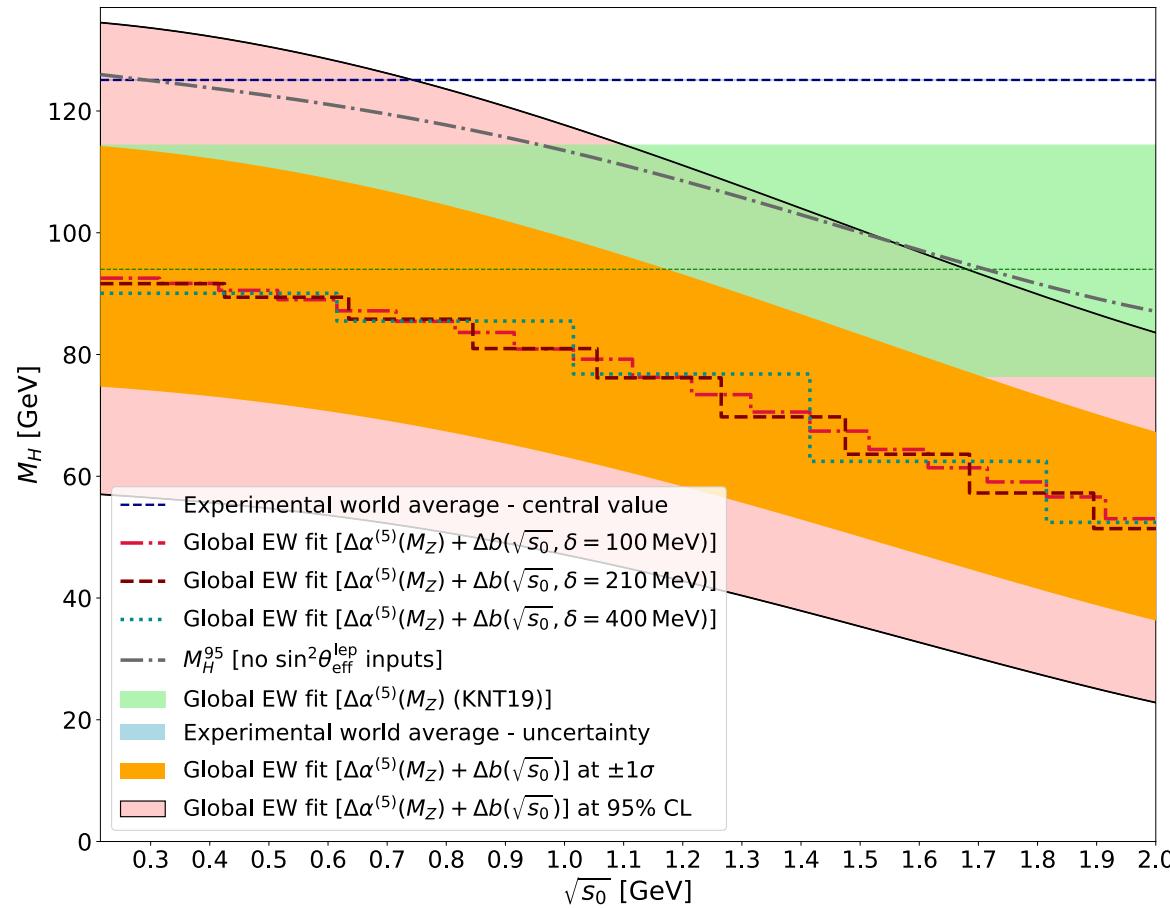


Marciano, MP, Sirlin, PRD 2008

Major update: Higgs discovered, improved EW observables (M_W , $\sin^2\theta$, M_{top} , ...), updates to $\sigma(s)$, theory improvements, global fit, ...

Parameter	Input value	Reference	Fit result	Result w/o input value
M_W (GeV)	80.379(12)	[5]	80.359(3)	80.357(4)(5)
M_H (GeV)	125.10(14)	[5]	125.10(14)	94^{+20+6}_{-18-6}
$\Delta\alpha_{had}^{(3)}(M_Z^2) \times 10^4$	276.1(1.1)	[23]	275.8(1.1)	272.2(3.9)(1.2)
m_t (GeV)	172.9(4)	[5]	173.0(4)	...
$\alpha_s(M_Z^2)$	0.1179(10)	[5]	0.1180(7)	...
M_Z (GeV)	91.1876(21)	[5]	91.1883(20)	...
Γ_Z (GeV)	2.4952(23)	[5]	2.4940(4)	...
Γ_W (GeV)	2.085(42)	[5]	2.0903(4)	...
ϕ_{had}^0 (nb)	41.541(37)	[108]	41.490(4)	...
R_t^0	20.767(25)	[108]	20.732(4)	...
R_c^0	0.1721(30)	[108]	0.17222(8)	...
R_b^0	0.21629(66)	[108]	0.21581(8)	...
\bar{m}_c (GeV)	1.27(2)	[5]	1.27(2)	...
\bar{m}_b (GeV)	$4.18^{+0.03}_{-0.02}$	[5]	$4.18^{+0.03}_{-0.02}$...
A_{FB}^{0J}	0.0171(10)	[108]	0.01622(7)	...
$A_{FB}^{0\pi}$	0.0707(35)	[108]	0.0737(2)	...
$A_{FB}^{0,b}$	0.0992(16)	[108]	0.1031(2)	...
A_f	0.1499(18)	[75,108]	0.1471(3)	...
A_c	0.670(27)	[108]	0.6679(2)	...
A_b	0.923(20)	[108]	0.93462(7)	...
$\sin^2\theta_{eff}^{loop}(Q_{FB})$	0.2324(12)	[108]	0.23152(4)	0.23152(4)(4)
$\sin^2\theta_{eff}^{loop}(\text{Had Coll})$	0.23140(23)	[100]	0.23152(4)	0.23152(4)(4)

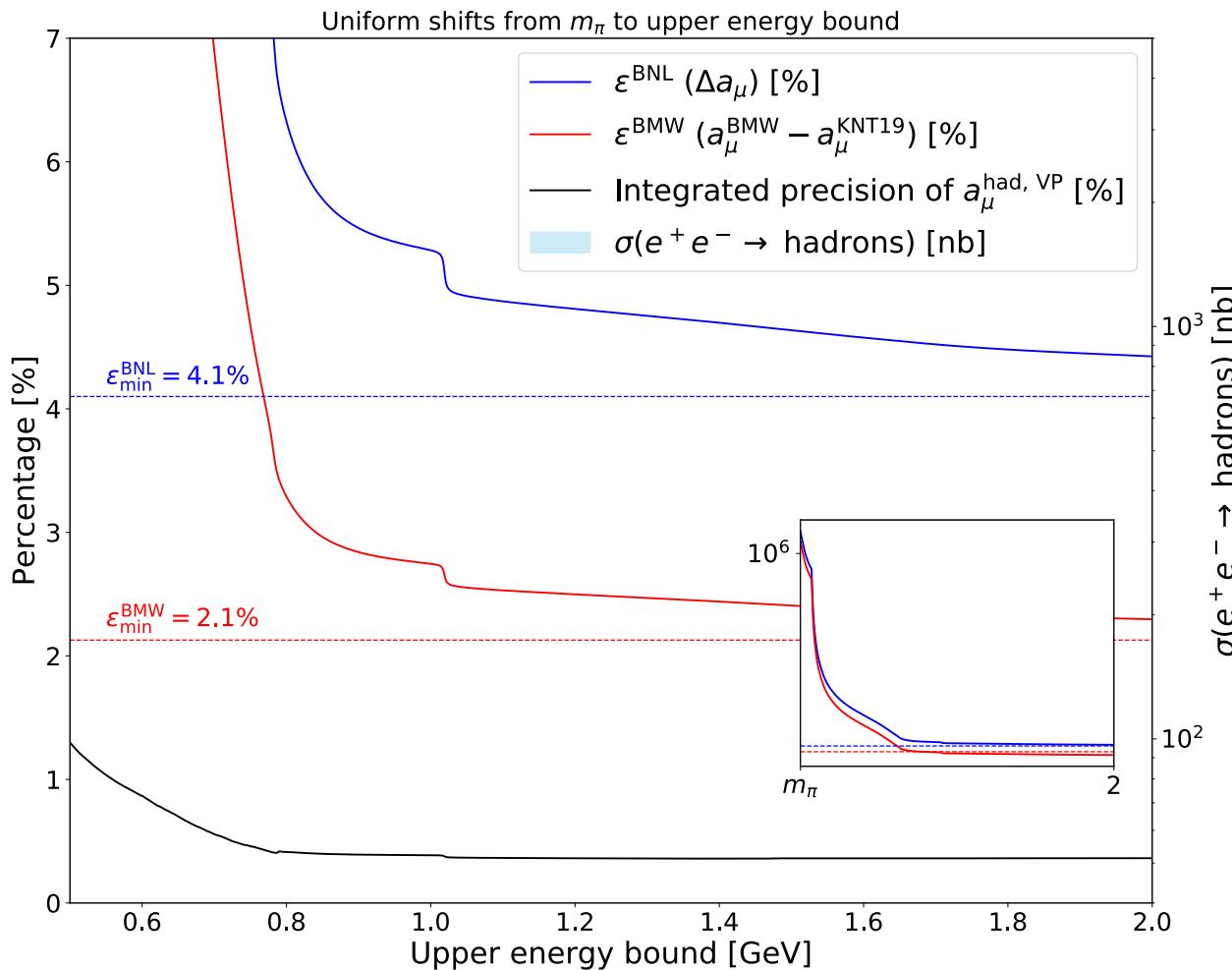
Keshavarzi, Marciano, MP, Sirlin, PRD 2020 (using Gfitter)



Shifts $\Delta\sigma(s)$ to fix Δa_μ are possible,
but conflict with the EW fit if they occur above ~ 1 GeV

How large are the required shifts $\Delta\sigma(s)$?

$\Delta\alpha$



Shifts below ~ 1 GeV conflict with the quoted exp. precision of $\sigma(s)$

Keshavarzi, Marciano, MP, Sirlin, PRD 2020 (updated 2021)

What happens to the electron g-2?

- The 2008 measurement of the electron g-2 is:

$$a_e^{\text{EXP}} = 11596521807.3 (2.8) \times 10^{-13} \quad \text{Hanneke et al, PRL100 (2008) 120801}$$

vs. old (factor of 15 improvement, 1.8σ difference):

$$a_e^{\text{EXP}} = 11596521883 (42) \times 10^{-13} \quad \text{Van Dyck et al, PRL59 (1987) 26}$$

- Equate $a_e^{\text{SM}}(\alpha) = a_e^{\text{EXP}}$ → “ $g_e\text{-}2$ ” determination of alpha:

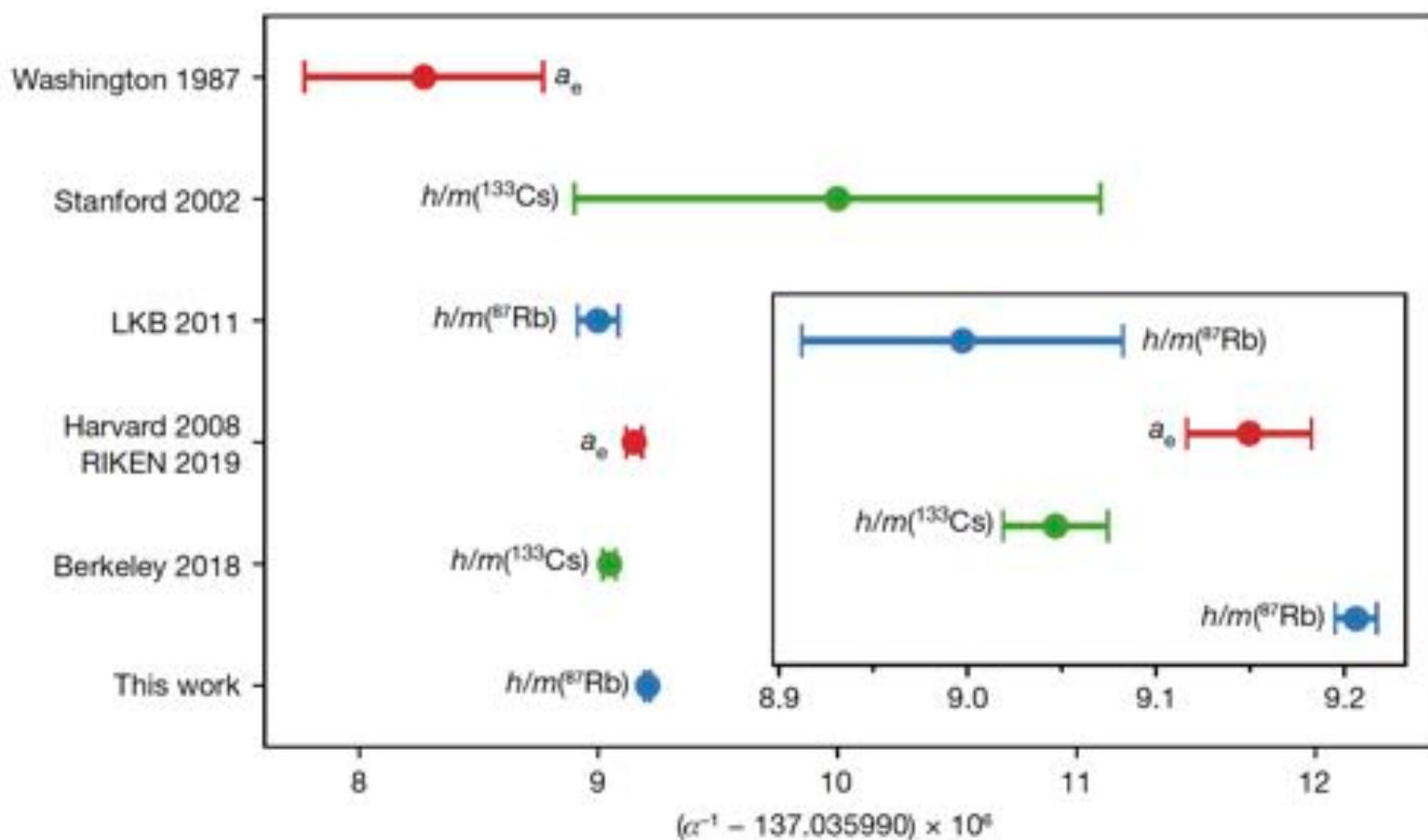
$$\alpha^{-1} = 137.035\ 999\ 151 (33) \quad [0.24 \text{ ppb}]$$

- The best determination of α is obtained via atomic interferometry:

$$\alpha^{-1} = 137.035\ 999\ 046 (27) [0.20 \text{ ppb}] \quad \text{Parker et al, Science 360 (2018) 192 (Cs)}$$

$$\alpha^{-1} = 137.035\ 999\ 206 (11) [0.08 \text{ ppb}] \quad \text{Morel et al, Nature 588 (2020) 61 (Rb)}$$

2018→2020: improvement in precision, but 5.4σ difference!



Morel et al, Nature 588 (2020) 61

- Using the best determinations of α (which differ by $5.4\sigma!$):

$$\alpha = 1/137.035\,999\,046 (27) \text{ [Cs 2018]}$$

$$\alpha = 1/137.035\,999\,206 (11) \text{ [Rb 2020]}$$

$$\begin{aligned} a_e^{\text{SM}} &= 115\,965\,218\,16.16 (0.11) (0.08) (2.28) \times 10^{-13} \text{ [Cs18]} \\ &= 115\,965\,218\,02.64 (0.11) (0.08) (0.93) \times 10^{-13} \text{ [Rb20]} \end{aligned}$$

δC_5^{qed} δa_e^{had} from $\delta \alpha$

$$a_e^{\text{EXP}} = 115\,965\,218\,07.3 (2.8) \times 10^{-13} \quad \text{Hanneke et al, PRL 2008}$$

- The (EXP – SM) difference is:

$$\begin{aligned} \Delta a_e &= a_e^{\text{EXP}} - a_e^{\text{SM}} = -8.9 (3.6) \times 10^{-13} \text{ [2.5}\sigma\text{] [Cs18]} \\ &= +4.7 (3.0) \times 10^{-13} \text{ [1.6}\sigma\text{] [Rb20]} \end{aligned}$$

QED 5-loop: $a_e^{\text{QED5}} = 4.6 \times 10^{-13}$

- NP sensitivity limited only by the experimental errors in α and a_e . May soon play a pivotal role in probing NP in the leptonic sector.

- Using $\alpha(\text{Rb2020})$, the sensitivity is $\delta\Delta a_e = 3.0 \times 10^{-13}$, ie ($\times 10^{-13}$):

$$(0.1)_{\text{QED5}}, \quad (0.1)_{\text{HAD}}, \quad (0.9)_{\delta\alpha}, \quad (2.8)_{\delta a_e^{\text{EXP}}}$$

$\underbrace{\qquad\qquad\qquad}_{(0.2)_{\text{TH}}}$

- The $(g-2)_e$ experimental error may soon drop below $10^{-13} \rightarrow$
a_e sensitivity below 10^{-13} may soon be reached!
- In a broad class of BSM theories, contributions to a_l scale as

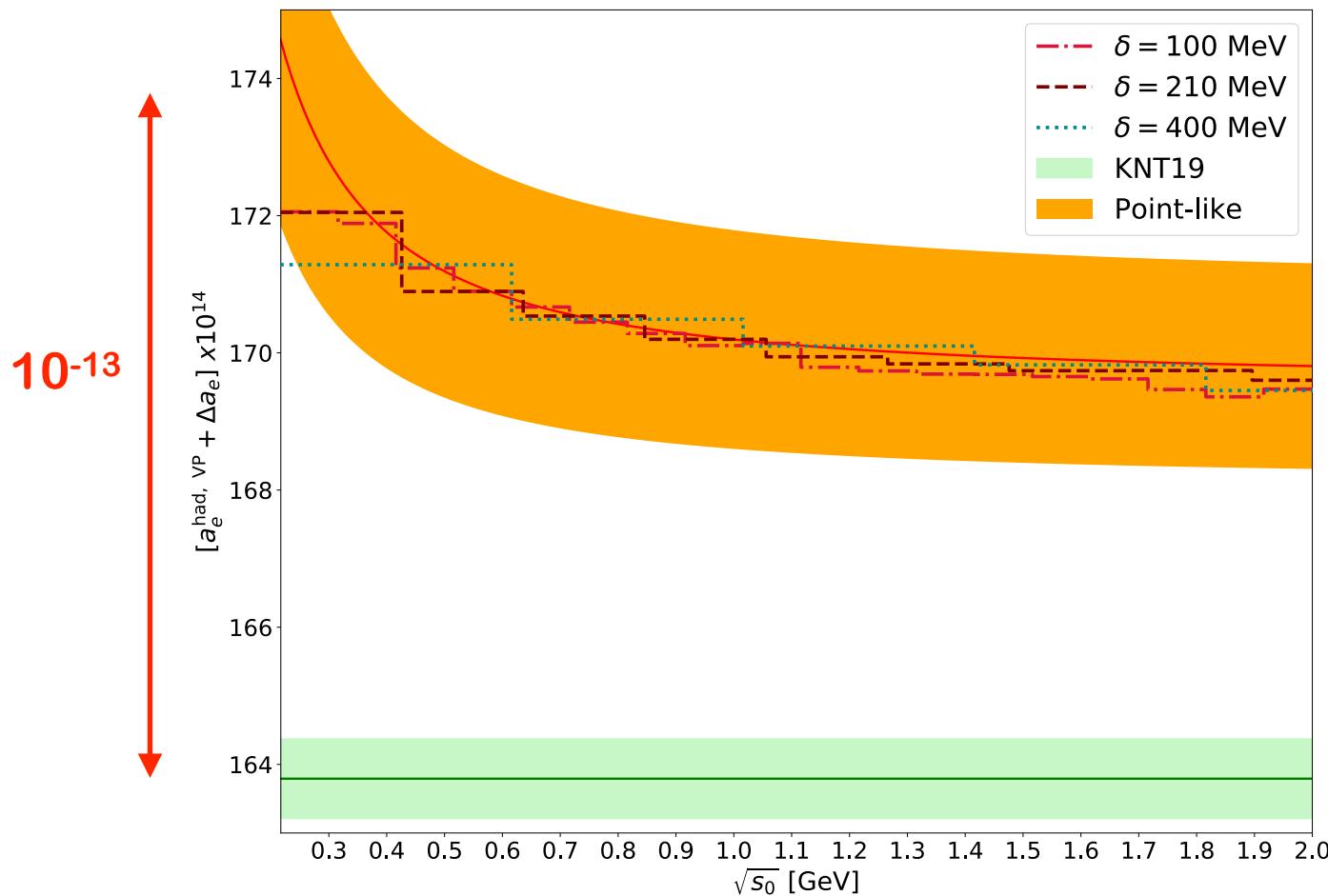
$$\frac{\Delta a_{\ell_i}}{\Delta a_{\ell_j}} = \left(\frac{m_{\ell_i}}{m_{\ell_j}} \right)^2 \quad \text{This Naive Scaling leads to:}$$

$$\Delta a_e = \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.7 \times 10^{-13}; \quad \Delta a_\tau = \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.8 \times 10^{-6}$$

Giudice, Paradisi & MP, JHEP 2012

Shift of the electron g-2

e

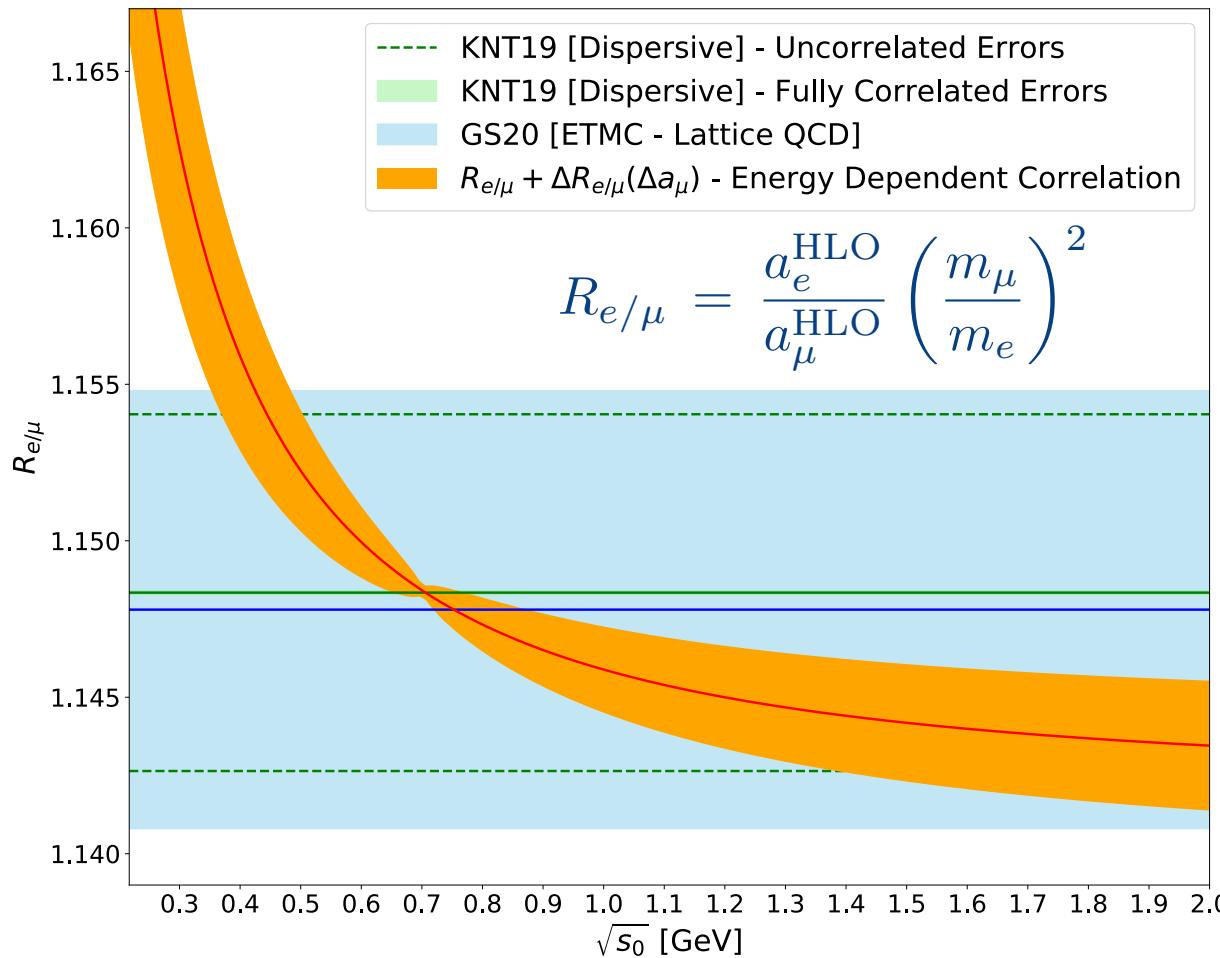


Shifts $\Delta\sigma(s)$ to fix Δa_μ only slightly change Δa_e

Keshavarzi, Marciano, MP, Sirlin, PRD 2020

Shift of the e/μ g-2 scaled HLO ratio

e/μ



**Good agreement between lattice [Giusti & Simula 2020] and KNT19.
Possible future bounds on very low energy shifts $\Delta\sigma(s)$?**

Keshavarzi, Marciano, MP, Sirlin, PRD 2020

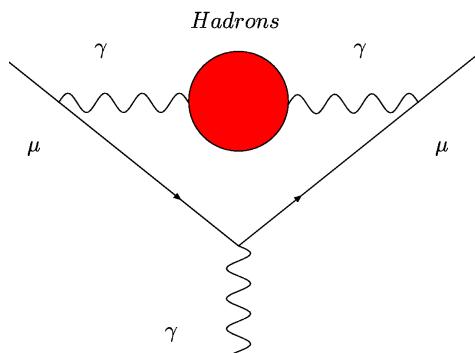
- Crivellin, Hoferichter, Manzari and Montull, “Hadronic vacuum polarization: $(g-2)_\mu$ versus global electroweak fits,” arXiv:2003.04886.
- Eduardo de Rafael, “On Constraints Between $\Delta\alpha_{\text{had}}(M^2)$ and $(g_\mu-2)_{\text{HVP}}$,” arXiv:2006.13880.
- Malaescu and Schott, “Impact of correlations between a_μ and a_{QED} on the EW fit,” arXiv:2008.08107.
- Colangelo, Hoferichter and Stoffer, “Constraints on the two-pion contribution to hadronic vacuum polarization,” arXiv:2010.07943.

The MUonE project



The spacelike method for a_μ^{HLO}

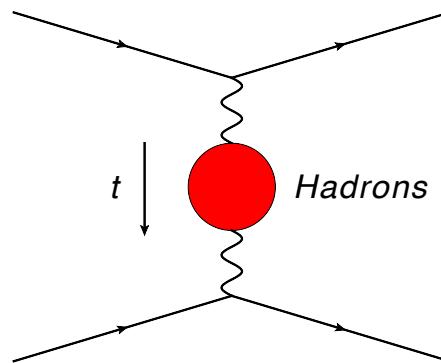
- Leading hadronic contribution computed via the usual dispersive (timelike) formula:



$$a_\mu^{\text{HLO}} = \frac{1}{4\pi^3} \int_{m_\pi^2}^\infty ds K(s) \sigma_{\text{had}}^{(0)}(s)$$

$$K(s) = \int_0^1 dx \frac{x^2 (1-x)}{x^2 + (1-x) (s/m_\mu^2)}$$

- Alternatively, simply exchanging the x and s integrations:



$$a_\mu^{\text{HLO}} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{\text{had}}[t(x)]$$

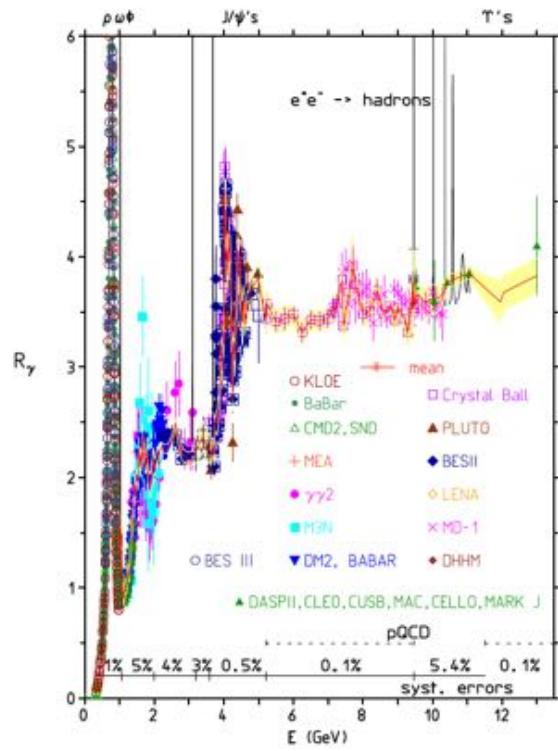
$$t(x) = \frac{x^2 m_\mu^2}{x-1} < 0$$

Lautrup, Peterman, de Rafael, 1972

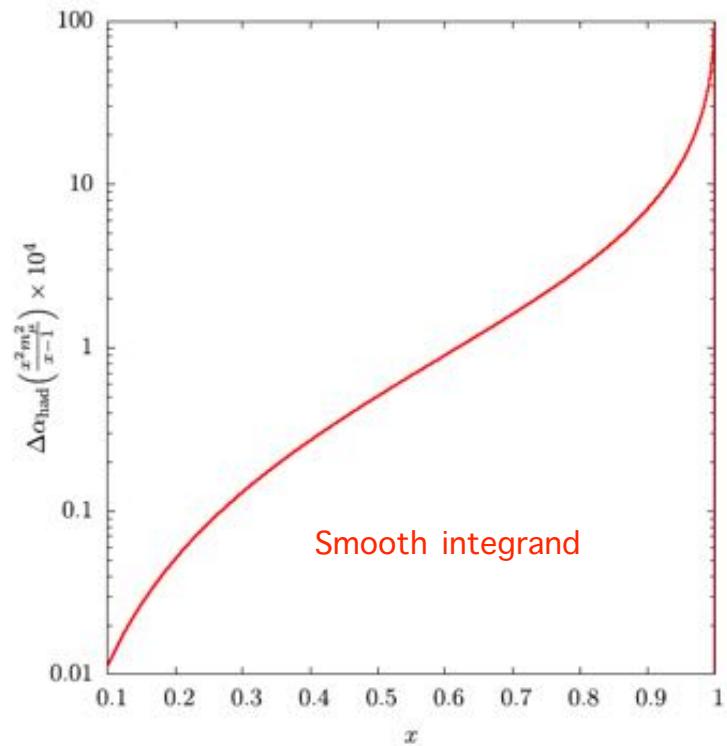
$\Delta\alpha_{\text{had}}(t)$ is the hadronic contribution to the space-like running of α : proposal to measure a_μ^{HLO} via scattering data!

a_μ^{HLO} : timelike vs spacelike method

Timelike



Spacelike

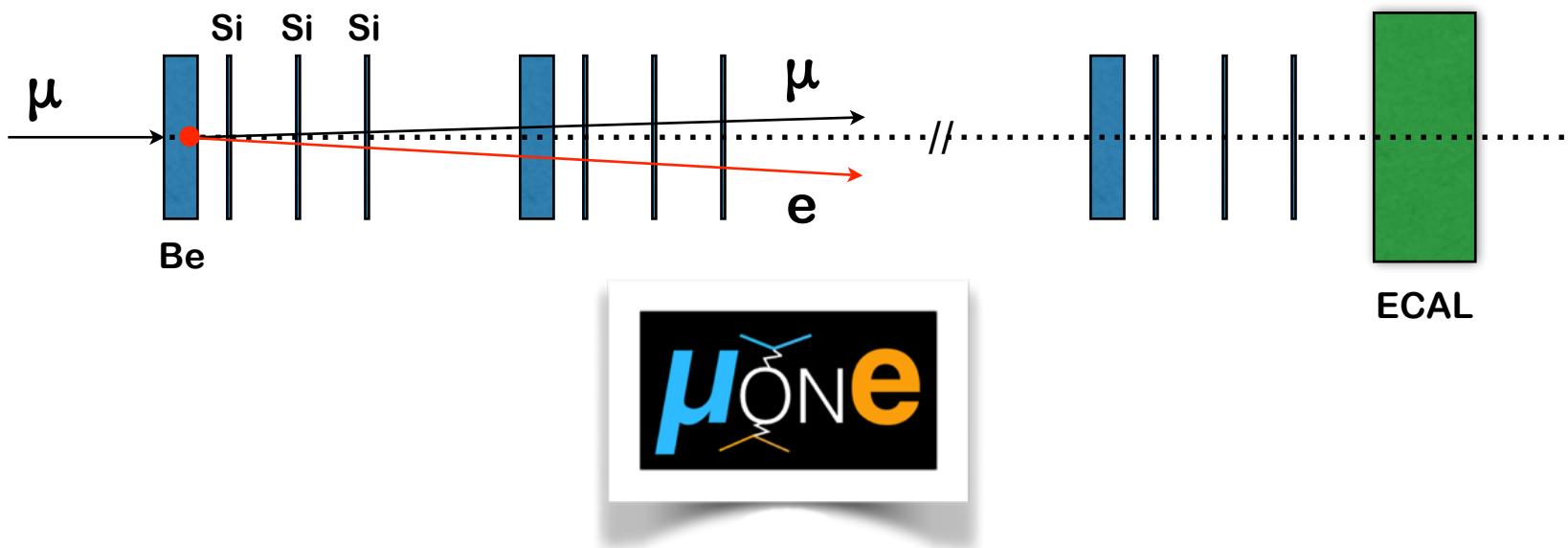


F. Jegerlehner, arXiv:1511.04473

Carloni Calame, MP, Trentadue, Venanzoni, PLB 2015

- Inclusive measurement
- Smooth integrand
- Direct interplay with lattice QCD

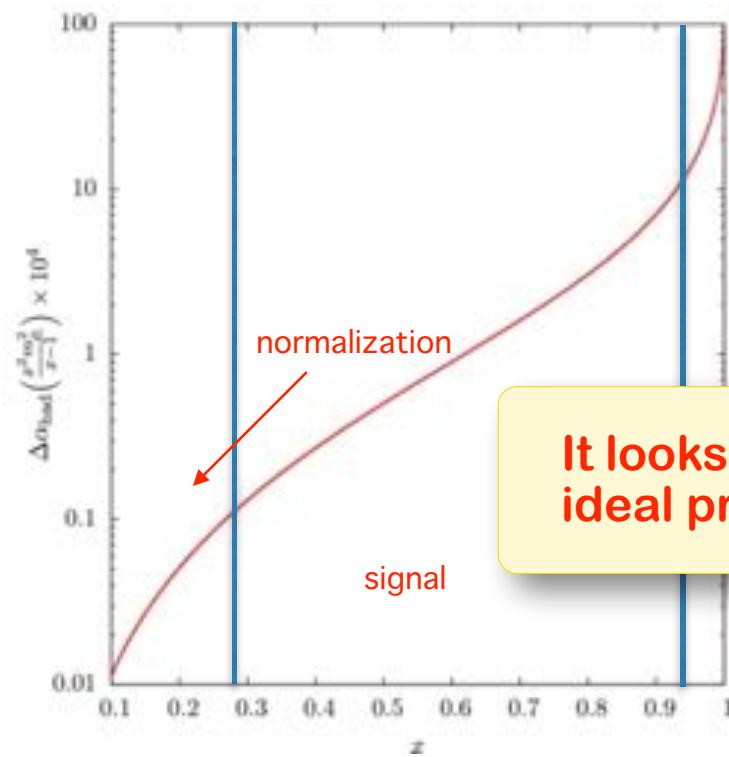
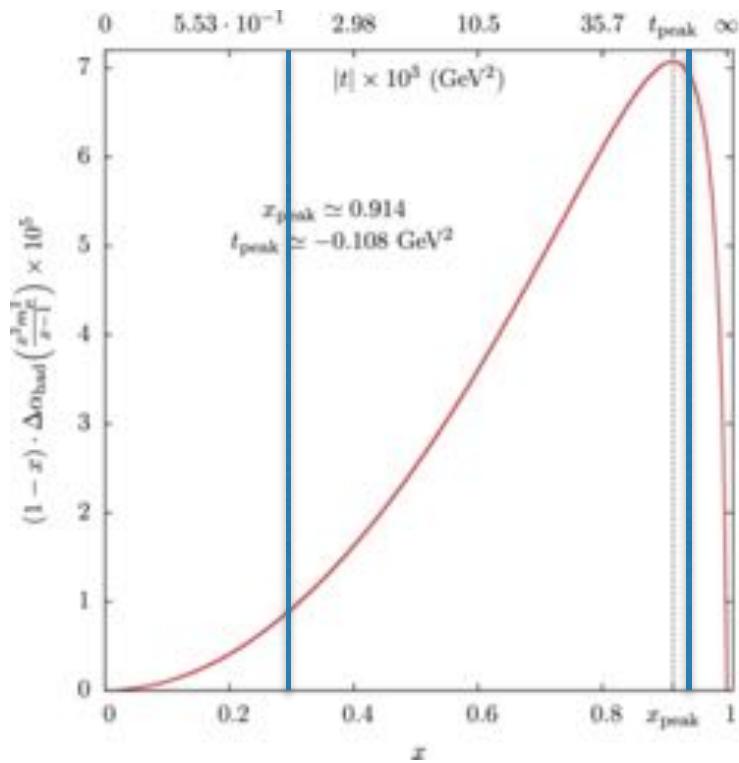
- $\Delta\alpha_{had}(t)$ can be measured via the elastic scattering $\mu e \rightarrow \mu e$.
- We propose to scatter a 150 GeV muon beam, available at CERN's North Area, on a fixed electron target (Beryllium). Modular apparatus: each station has one layer of Beryllium (target) followed by several thin Silicon strip detectors.



Abbiendi, Carloni Calame, Marconi, Matteuzzi, Montagna,
Nicrosini, MP, Piccinini, Tenchini, Trentadue, Venanzoni

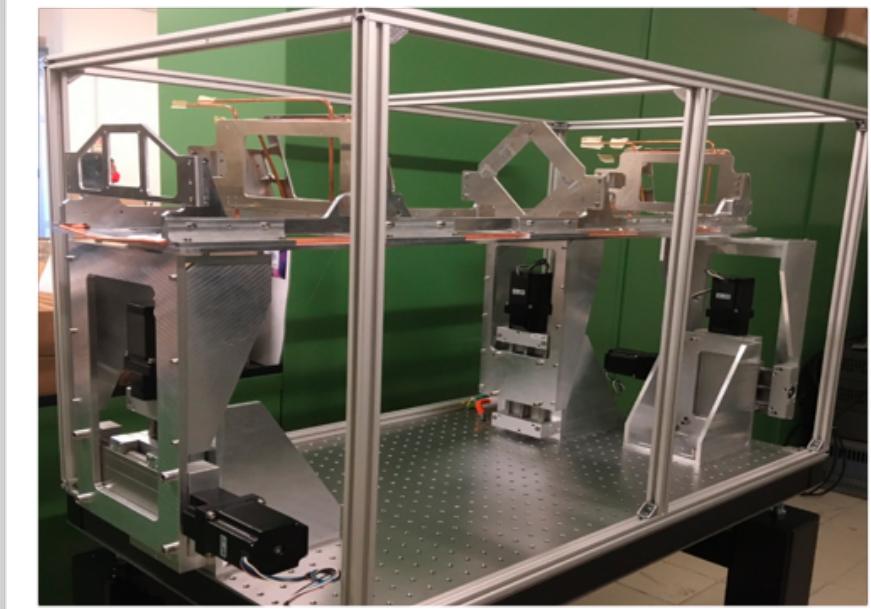
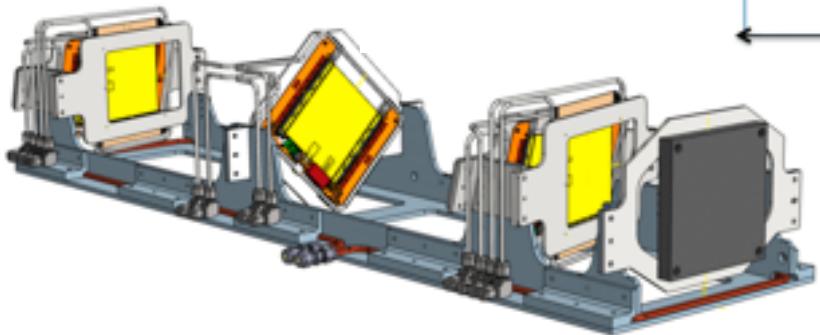
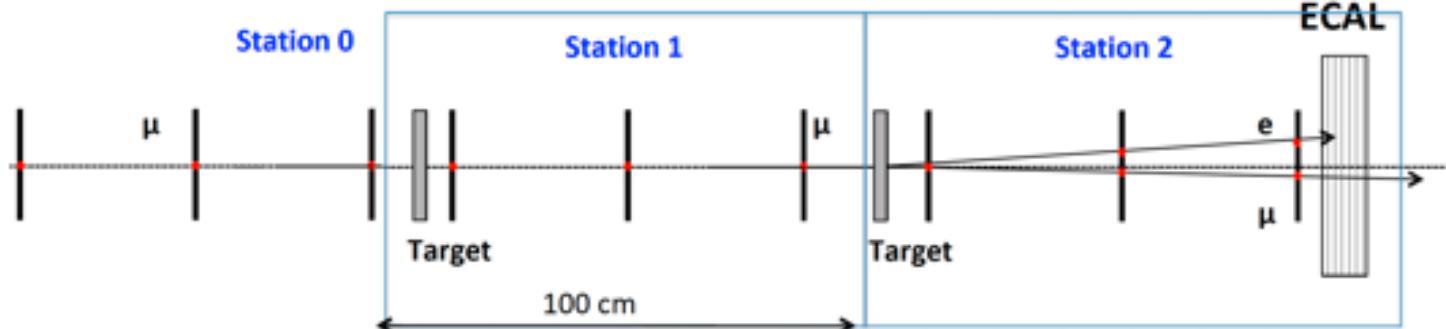
EPJC 2017 - arXiv:1609.08987

- For a 150 GeV muon beam ($\sqrt{s} \sim 400$ MeV), MUonE's scan region extends up to $x=0.932$, ie beyond the $x=0.914$ peak!



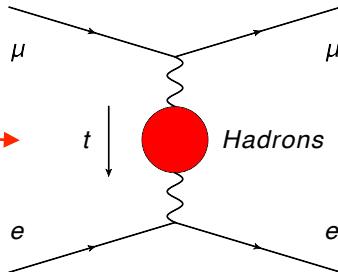
- **Statistics:** With CERN's 150 GeV muon beam M2 ($1.3 \times 10^7 \mu/\text{s}$), incident on 40 15mm Be targets (total Be thickness: 60cm), 2-3 years of data taking ($2 \times 10^7 \text{ s/yr}$) $\rightarrow \mathcal{L}_{\text{int}} \sim 1.5 \times 10^7 \text{ nb}^{-1}$.
- With this \mathcal{L}_{int} we estimate that measuring the shape of $d\sigma/dt$ we can reach a statistical sensitivity of $\sim 0.3\%$ on a_{μ}^{HLO} , ie $\sim 20 \times 10^{-11}$.
- **Systematic** effects must be known at $\lesssim 10\text{ppm}$!
- Test beams performed at CERN in 2017 & 2018 arXiv:1905.11677, 2102.11111
- Lol submitted to CERN SPSC in 2019: **Test run approved for 2021, delayed to 2022.**
- Full-statistics run hopefully in 2023–24.

MUonE — Getting ready for the Test Run



From R.N. Pilato's talk, FNAL, May 27th 2021

- To extract $\Delta\alpha_{\text{had}}(t)$ from MUonE's measurement, the ratio of the SM cross sections in the signal and normalisation regions must be known at $\lesssim 10\text{ppm}$!



- Fully differential fixed-order MC @ NLO ready Pavia and PSI 2018-19
- NNLO QED: Master Integrals for 2-loop box diagrams computed.
Full 2-loop amplitude completed! ($m_e=0$) Padova 2017 - present
- Two MC built including partial subsets of the NNLO QED corrections due to electron and muon radiation Pavia and PSI 2020
- NNLO hadronic effects computed Padova and KIT 2019
- Extraction of the leading electron mass effects from the massless muon-electron scattering amplitudes PSI 2019-present
- New Physics extracting $\Delta\alpha_{\text{had}}(t)$ at MUonE? Padova and Heidelberg 2020
- ...

Theory for muon-electron scattering @ 10 ppm:
A report of the MUonE theory initiative. arXiv:2004.13663

MUonE — Theory workshops



Padova
Europe/Rome timezone



Muon-electron scattering: Theory kickoff workshop

4-5 September 2017

- [Overview](#)
- [Venue](#)
- [Timetable](#)
- [Logistic](#)
- [Map](#)

[Support](#)



**MUonE theory workshops: Padova 2017, Mainz 2018, Zurich 2019
Next MUonE theory workshop: MITP Mainz 2020-21 postponed to 2022**

Conclusions

- Fermilab's Muon g-2 experiment confirms BNL's result: the discrepancy between experiment and SM increases to 4.2σ .
- The BMWc lattice QCD result weakens the exp-SM discrepancy. It must be confirmed or refuted by other lattice calculations.
- Is Δa_μ due to missed contributions in the hadronic cross section? Shifts above 1 GeV to fix Δa_μ conflict with the electroweak fit.
- Leading hadronic contribution to a_μ : dispersive vs lattice. MUonE will provide a new independent & alternative determination.