

# A Novel $\mu \rightarrow eee$ Experiment



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**Université de Genève  
June 8th, 2011**

# History

G.Feinberg, P.Kabir, S.Weinberg, PRL 3 527 (1959)

„Absence of:

- **Br** ( $\mu \rightarrow e \gamma$ )
- **Br** ( $\mu \rightarrow eee$ )
- **Br** ( $\mu N \rightarrow eN$ )

does not constitute a paradox there being no compelling reason why muons should transform into electrons, but it seems a **mystery** that processes which are allowed energetically and in every other known respect do not occur...”

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→ **Introduction of lepton flavor quantum number**

Standard Model:  $\mu \rightarrow e \bar{\nu}_e \nu_\mu$

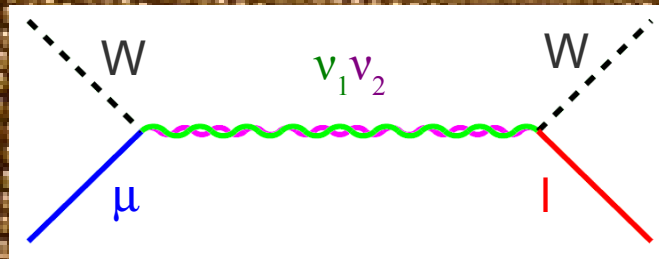
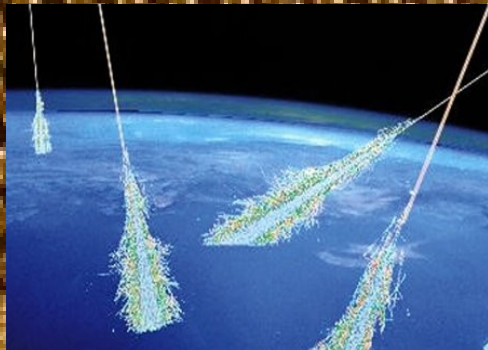


# Discovery of Neutrino Oscillations



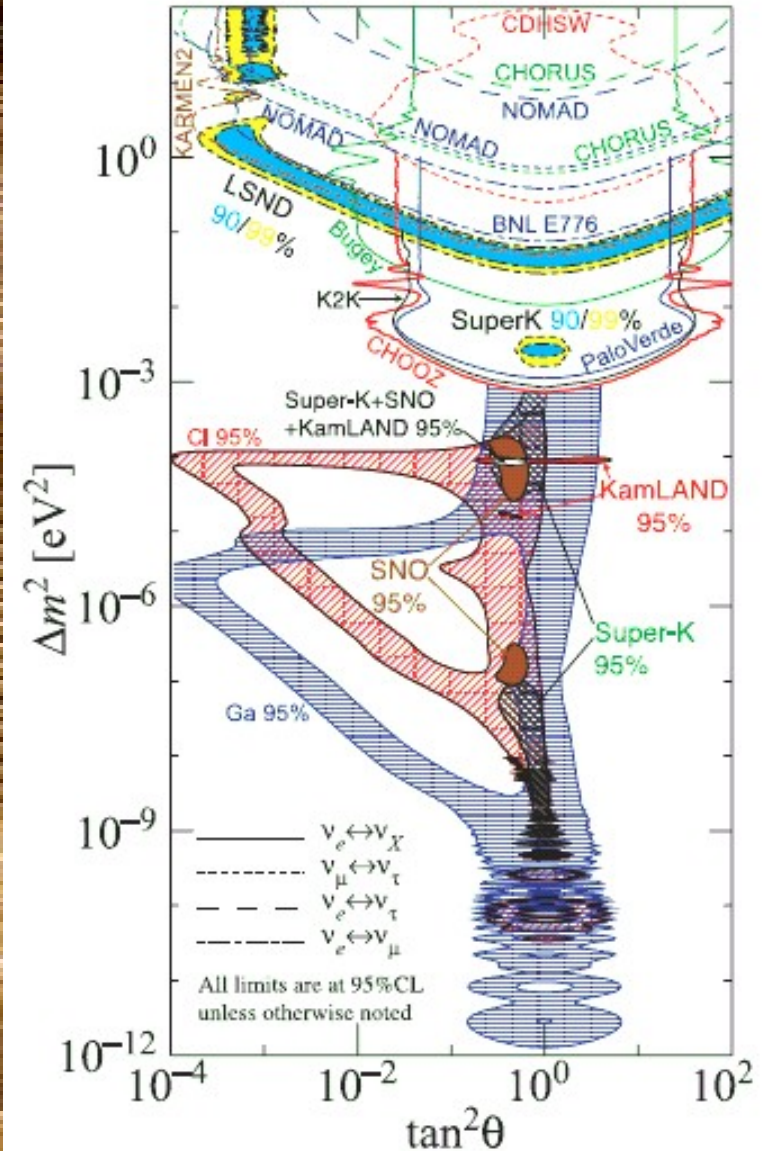
## • Neutrino Oscillations:

- solar neutrinos
- reactor neutrinos
- atmospheric neutrinos
- neutrino beams



$$P(\nu_{\alpha} \rightarrow \nu_{\beta}) = \sin^2(2\theta) \sin^2(1.27 \Delta m_{\alpha\beta}^2 \frac{L}{E})$$

“Feinberg Kabir and Weinberg were wrong!”



# Overview

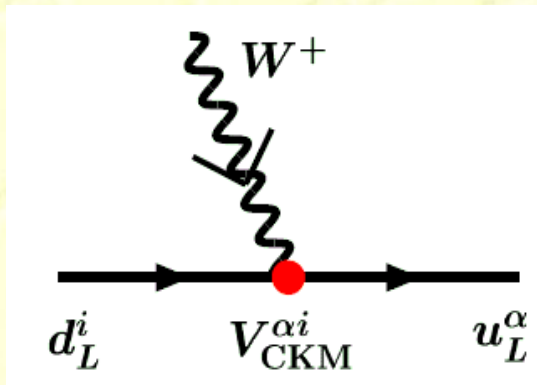
- **Introduction to Lepton Flavor Violation**
- **Motivation to Search for  $\mu \rightarrow eee$**
- **Backgrounds and Past Experiments**
- **(Novel) Detector Concept and Design**
- **Simulation Studies**
- **Summary**

# Fermion Mixing

## Quarks

### Cabibbo Kobayashi Maskawa (CKM)

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$





# Fermion Mixing

Quarks

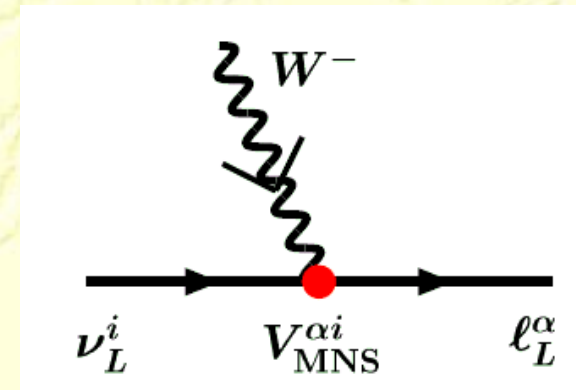
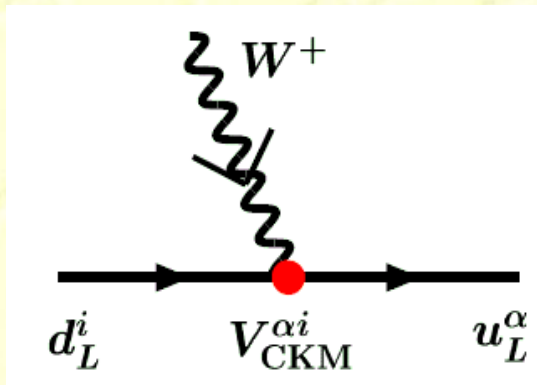
Leptons

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$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} V_{e1} & V_{e2} & V_{e3} \\ V_{\mu 1} & V_{\mu 2} & V_{\mu 3} \\ V_{\tau 1} & V_{\tau 2} & V_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



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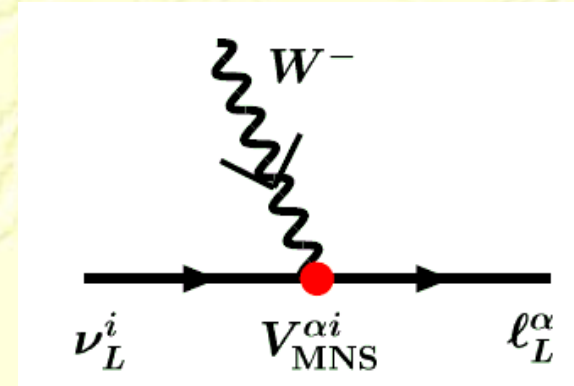
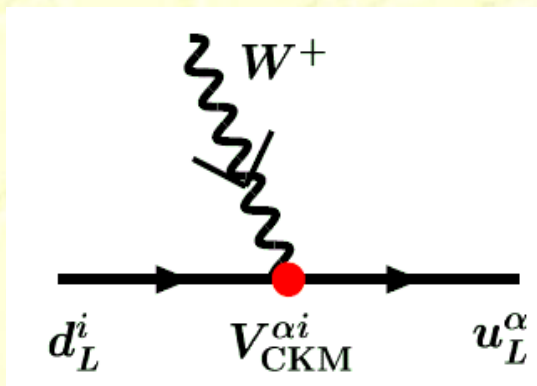
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- **W bosons** smell different flavors!
- **other gauge bosons ( $\gamma, Z, g$ ) do not** ( $\rightarrow$  no FCNC)



# Fermion Mixing

Quarks

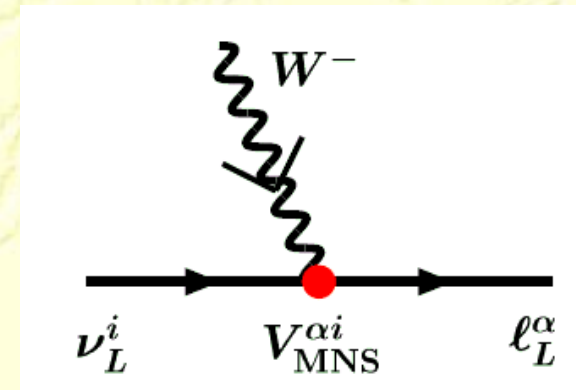
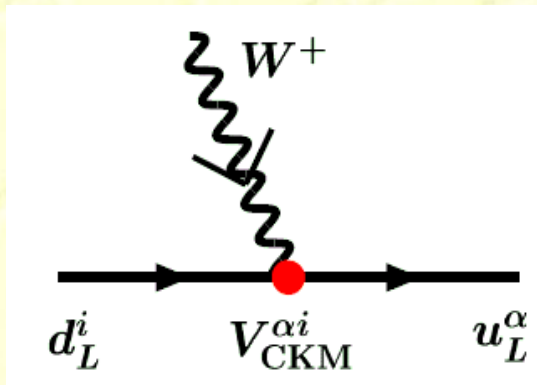
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$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} 0.974 & 0.225 & 0.003 \\ 0.225 & 0.973 & 0.041 \\ 0.009 & 0.040 & 0.999 \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} \approx \begin{pmatrix} 0.816 & 0.577 & < 0.2 \\ 0.408 & 0.577 & 0.707 \\ 0.408 & 0.577 & 0.707 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



- Large mixing effects in lepton sector!

# Lepton Mixing, LFV and FCNC

## $U =$ Neutrino Mixing Matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} u_{e1} & u_{e2} & u_{e3} \\ u_{\mu 1} & u_{\mu 2} & u_{\mu 3} \\ u_{\tau 1} & u_{\tau 2} & u_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

weak

eigenstates

mass

## $W =$ Ch. Lepton Mixing Matrix

$$\begin{pmatrix} e \\ \mu \\ \tau \end{pmatrix} = \begin{pmatrix} w_{e1} & w_{e2} & w_{e3} \\ w_{\mu 1} & w_{\mu 2} & w_{\mu 3} \\ w_{\tau 1} & w_{\tau 2} & w_{\tau 3} \end{pmatrix} \begin{pmatrix} l_1 \\ l_2 \\ l_3 \end{pmatrix}$$

weak

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mass

- Charged Current:

PMNS matrix:  $V_{ki} = \sum_{\alpha=1}^3 W_{\alpha k}^{l*} U_{\alpha i}^{\nu}$  only product measurable

→ product of lepton and neutrino mixing matrices (→ **flavor changing**)

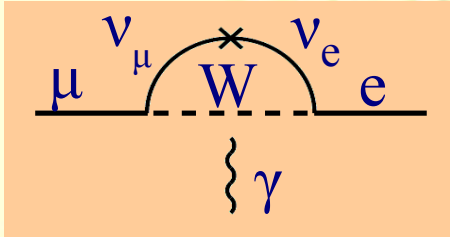
- Neutral Current:

unit matrix:  $\underline{1} = \sum_{\alpha=1}^3 U_{\alpha k}^{\nu*} U_{\alpha i}^{\nu} = \sum_{\alpha=1}^3 W_{\alpha k}^{l*} W_{\alpha i}^l$

→ unitary lepton and neutrino mixing matrices (→ **flavor conserving**)

# Lepton Flavor Violation in the SM

Higher Order!

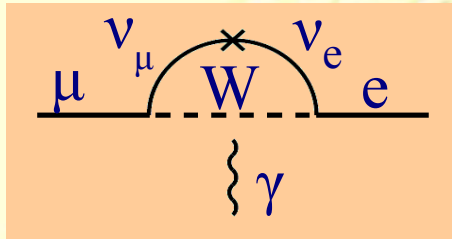


$$\mu \rightarrow e \gamma$$

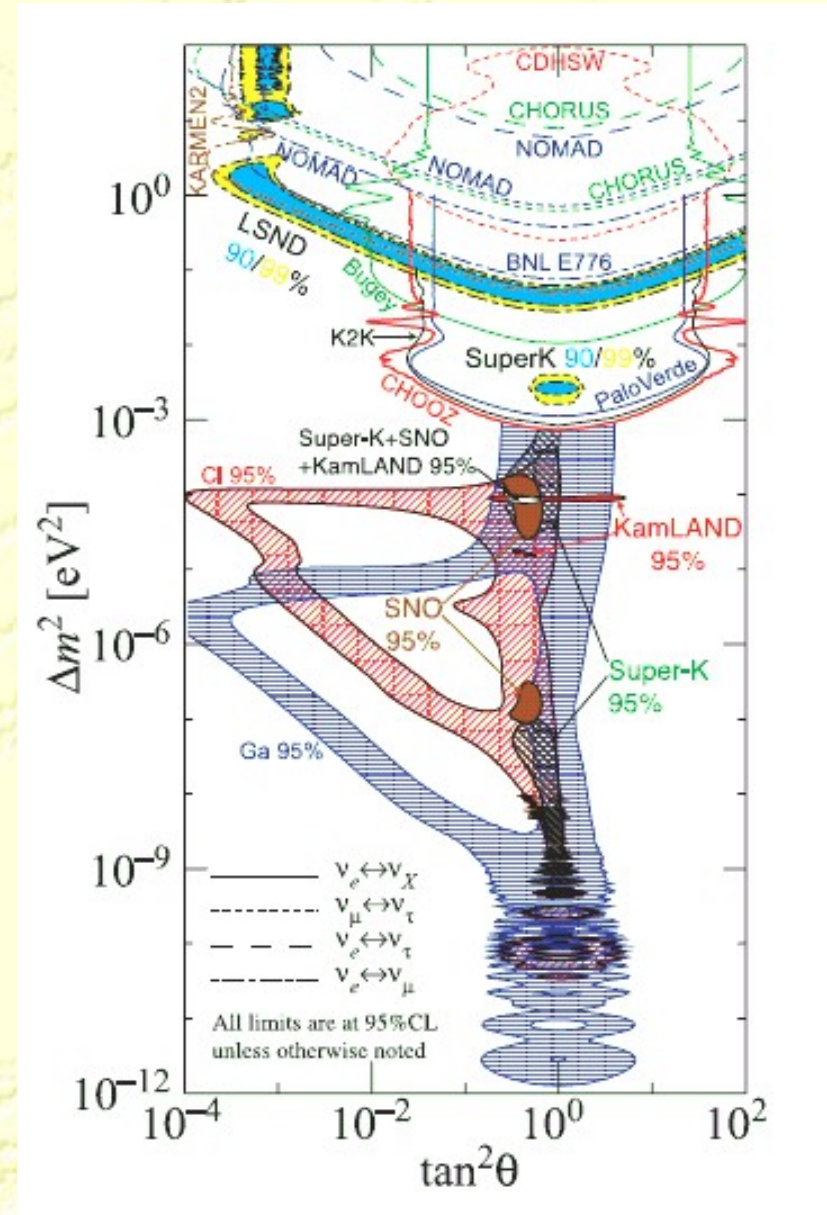
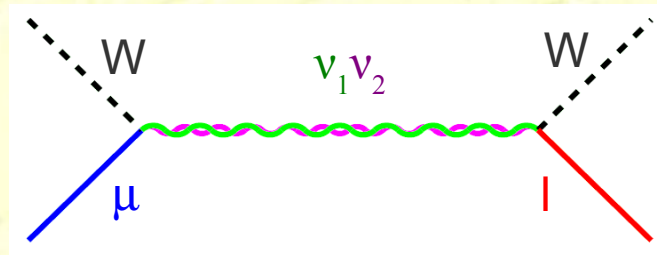


# Lepton Flavor Violation in the SM

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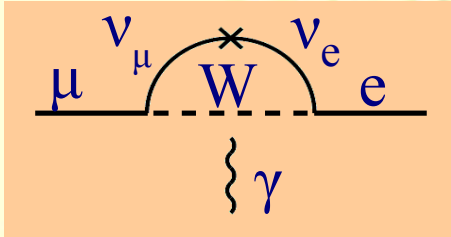


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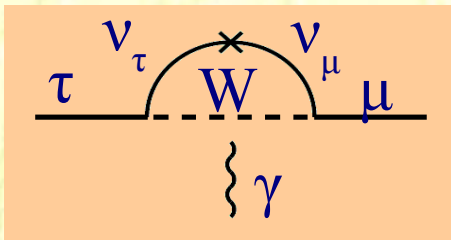


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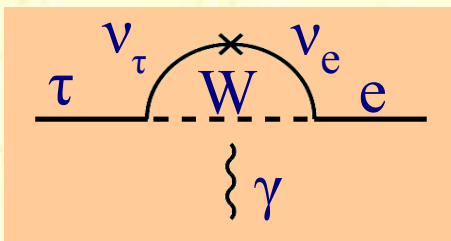
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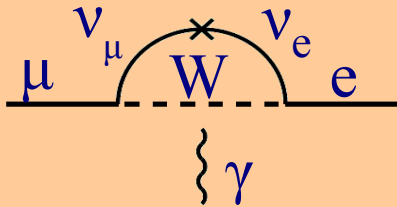
$$\tau \rightarrow \mu \gamma$$



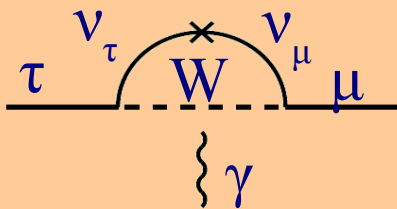
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# Lepton Flavor Violation in the SM

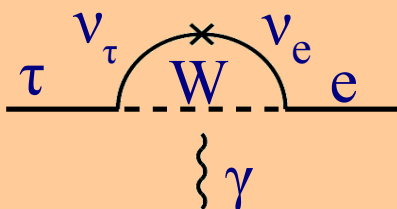
## Higher Order!



$$\mu \rightarrow e \gamma$$



$$\tau \rightarrow \mu \gamma$$



$$\tau \rightarrow e \gamma$$

## LFV is generated from lepton mixing:

$$BR(l_j \rightarrow l_k \gamma) \propto \left( \sum_i V_{ij} V_{jk}^* \frac{m_{\nu_i}^2}{M_W^2} \right)^2 \sim \left( \frac{\Delta m_{\nu_{jk}}^2}{M_W^2} \right)^2$$

GIM – like suppression:

$$\sim 10^{-50}$$

→ unobservable

→ high sensitivity to new physics!!!

c.t. quark mixing:

→ FCNC in SM  $\sim 10^{-10}$

$$\left( \frac{\Delta m_{c-u}^2}{M_W^2} \right)^2 \sim 10^{-7}$$



# Searches of Lepton<sup>±</sup> Flavor Violation

## Lepton Decays:

- $\mu \rightarrow e \gamma$
- $\mu \rightarrow eee$
- $\tau \rightarrow e(\mu) \gamma$
- $\tau \rightarrow lll$  ( $l=e,\mu$ )
- $\tau \rightarrow lh$

## Meson Decays:

- $\Phi, K \rightarrow ll'$
- $D, J/\psi \rightarrow ll'$
- $B, Y \rightarrow ll'$

## Conversion ( $\mu$ -Capture):

- $\mu N \rightarrow e N$

**LFV**

## Collider Experiments:

- $e p \rightarrow \mu(\tau) X$  HERA
- $Z' \rightarrow ll'$  LHC
- $\chi^{0\pm} \rightarrow ll' X$

## Fixed Target Experiments:

- $\mu N \rightarrow \tau N$  proposed
- $e N \rightarrow \mu(\tau) N$  proposed

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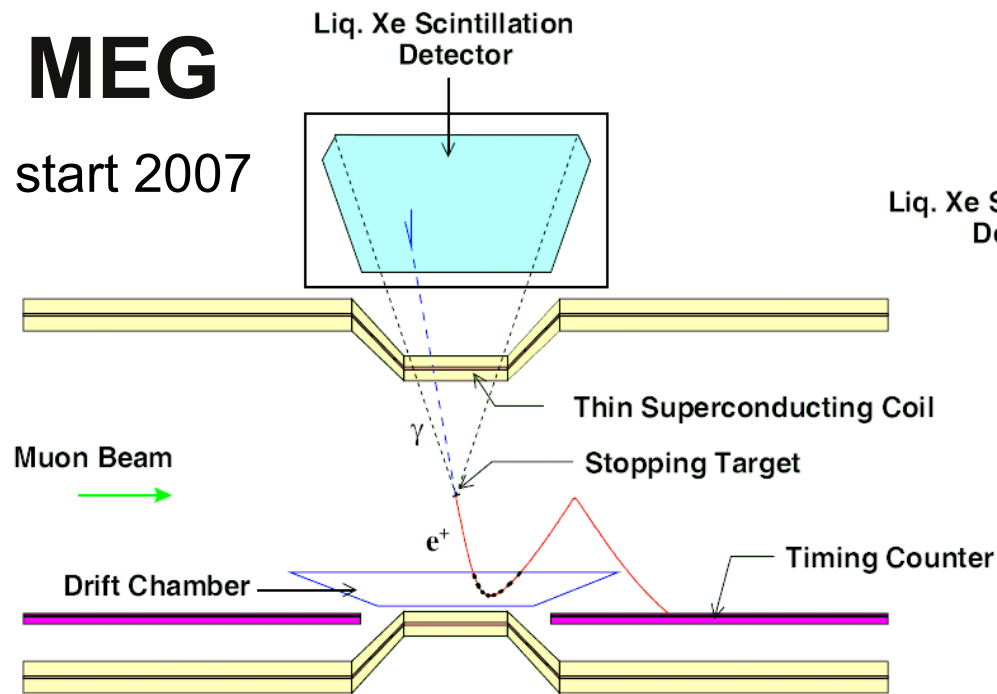
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# The MEG Experiment

**MEG**

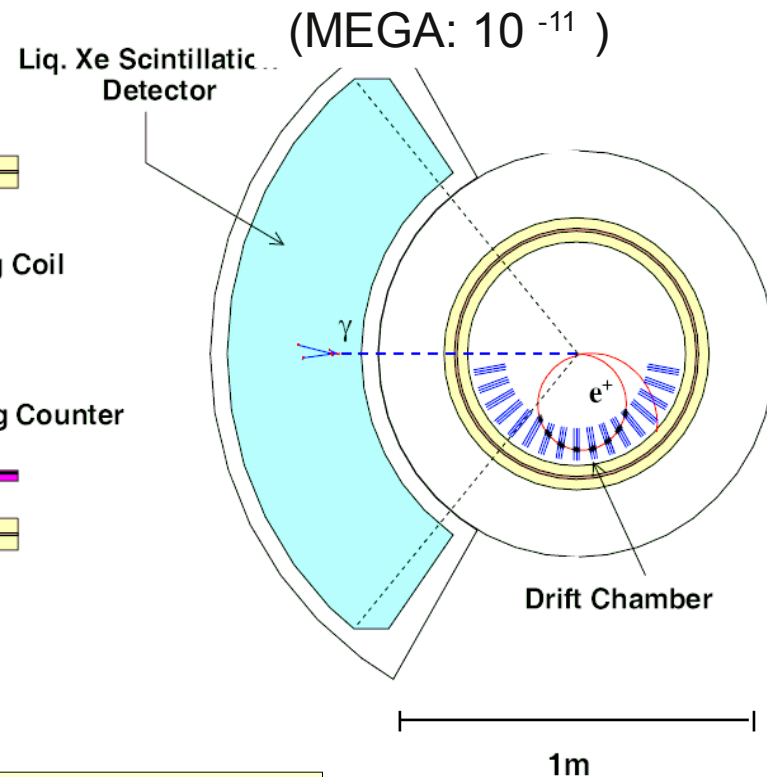
start 2007



LFV decay:  $\mu^+ \rightarrow e^+ \gamma$

sensitivity reach:

$$BR(\mu^+ \rightarrow e^+ \gamma) < 10^{-13}$$

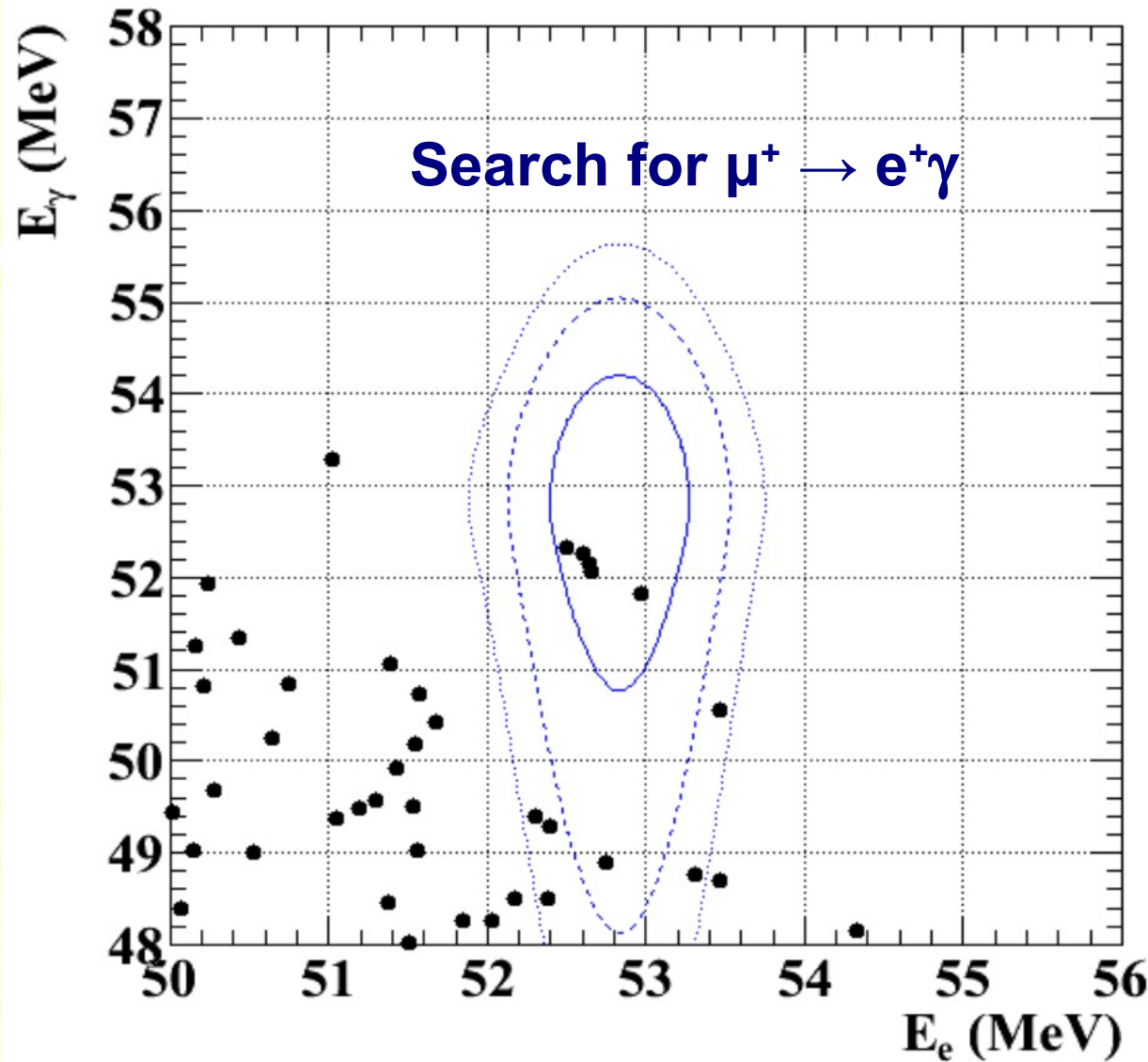


## Limitation:

- accidental background
- ➔ better space resolution
- ➔ improve tracking



# MEG Preliminary



MEG, ICHEP 2010

first indication of  
lepton flavor violation  
in muon decays?

# Experimental LFV Results

## Purely Leptonic LFV:

- $\text{Br}(\mu \rightarrow e \gamma) < 10^{-11}$  [MEGA]  
→  $10^{-13}$  MEG
- $\text{Br}(\tau \rightarrow \mu(e) \gamma) < \sim 4 \cdot 10^{-8}$  (B-factories)
- $\text{Br}(\mu \rightarrow eee) < 10^{-12}$  [SINDRUM]  
→  $10^{-16}$  this talk
- $\text{Br}(Z \rightarrow e\mu) < 10^{-6}$  [LEP]

## Semihadronic LFV:

- $\text{Br}(K \rightarrow \pi\mu e) < \approx 10^{-11}$
- $\text{Br}(\mu_{\text{capt}} N \rightarrow eN) < \sim 10^{-12}$  [SINDRUM2]  
→  $10^{-17}$  Mu2e, Prism
- $\mu N \rightarrow eN'$  or  $eN \rightarrow \mu(\tau)N'$  (DIS HERA):

# Experimental LFV Results

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- $\text{Br}(\mu \rightarrow e \gamma) < 10^{-11}$  [MEGA]  
→  $10^{-13}$  MEG
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## Semihadronic LFV:

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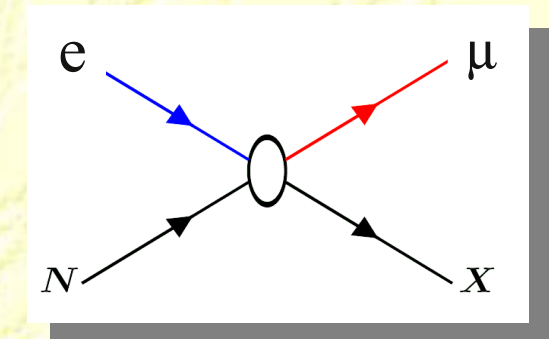
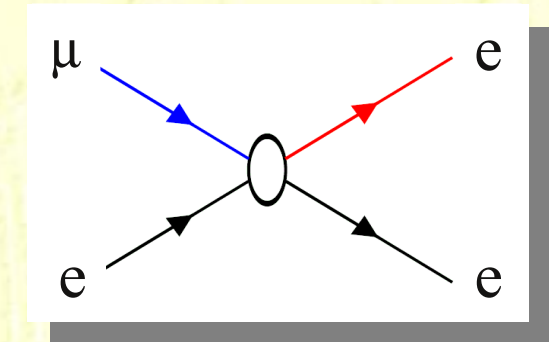
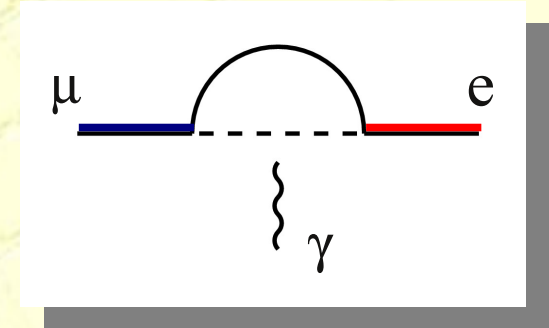
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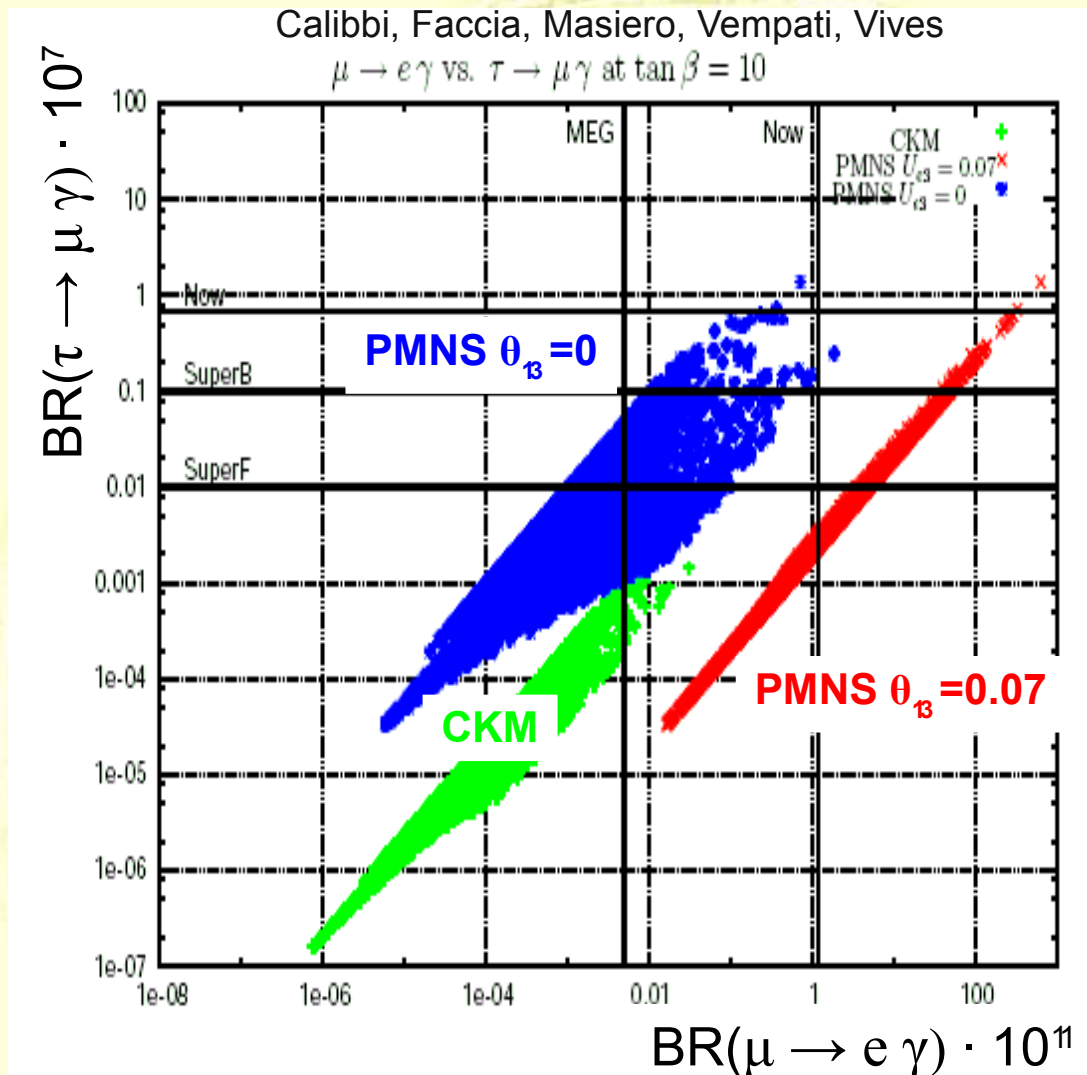
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# LFV in SUSY SO(10) GUT



points = SUSY LHC parameters

Yukawa couplings to neutrinos

$$h_\nu = h_u \quad (\text{CKM-case})$$

$$h_\nu = U_{PMNS} h_u^{diag} \quad (\text{PMNS-case})$$

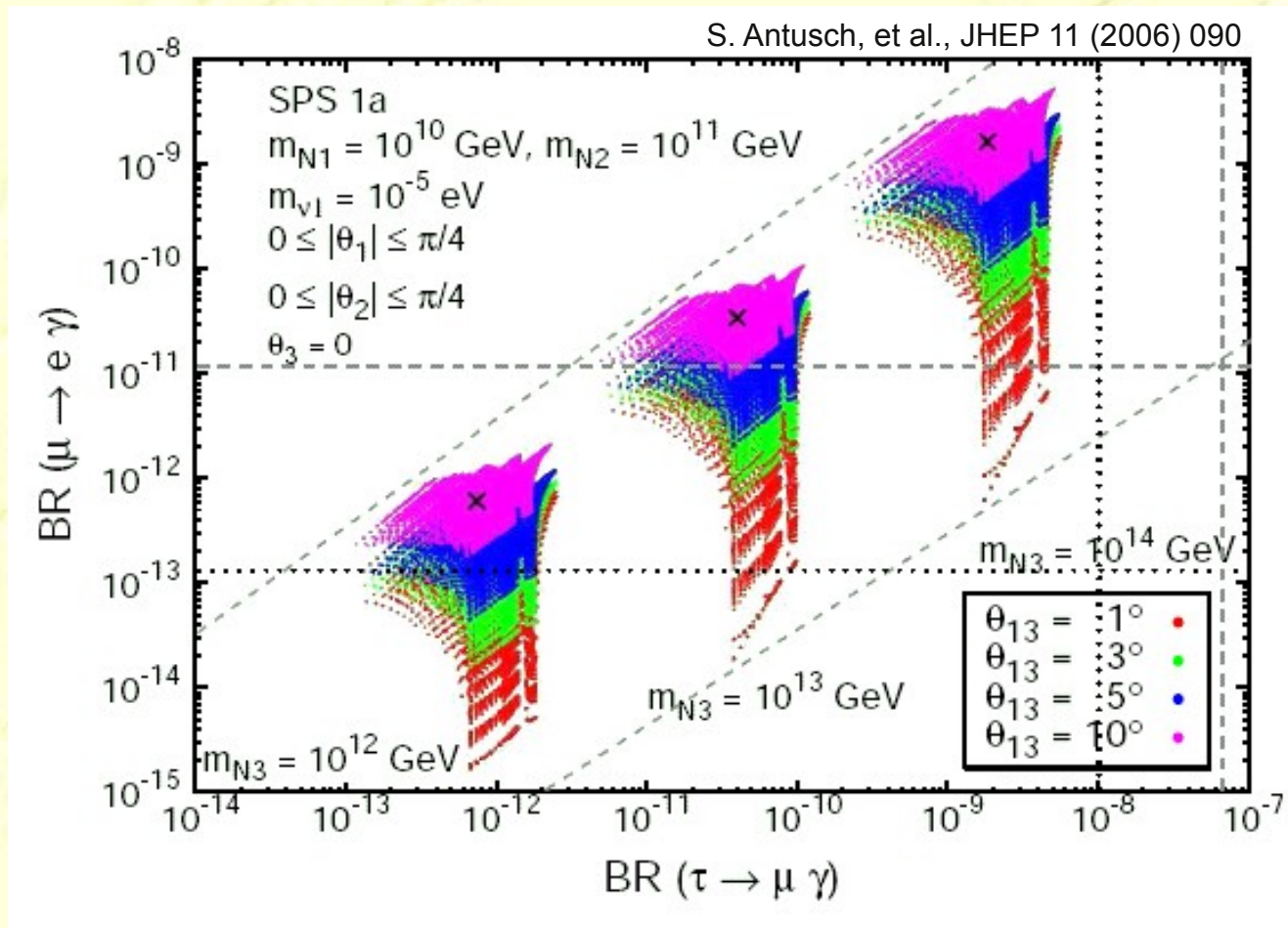
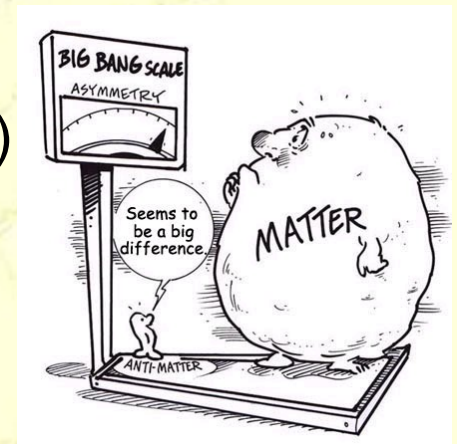
→ quasi model-dependent predictions: (G. Isidori et al.)

$$\text{CKM: } BR(\tau \rightarrow \mu \gamma) : BR(\tau \rightarrow e \gamma) : BR(\mu \rightarrow e \gamma) : \sim 10^4 : 500 : 1$$

$$\text{PMNS: } BR(\tau \rightarrow \mu \gamma) : BR(\tau \rightarrow e \gamma) : BR(\mu \rightarrow e \gamma) : \sim 500-10 : 1 : 1$$

# cMSSM Seesaw with Leptogenesis

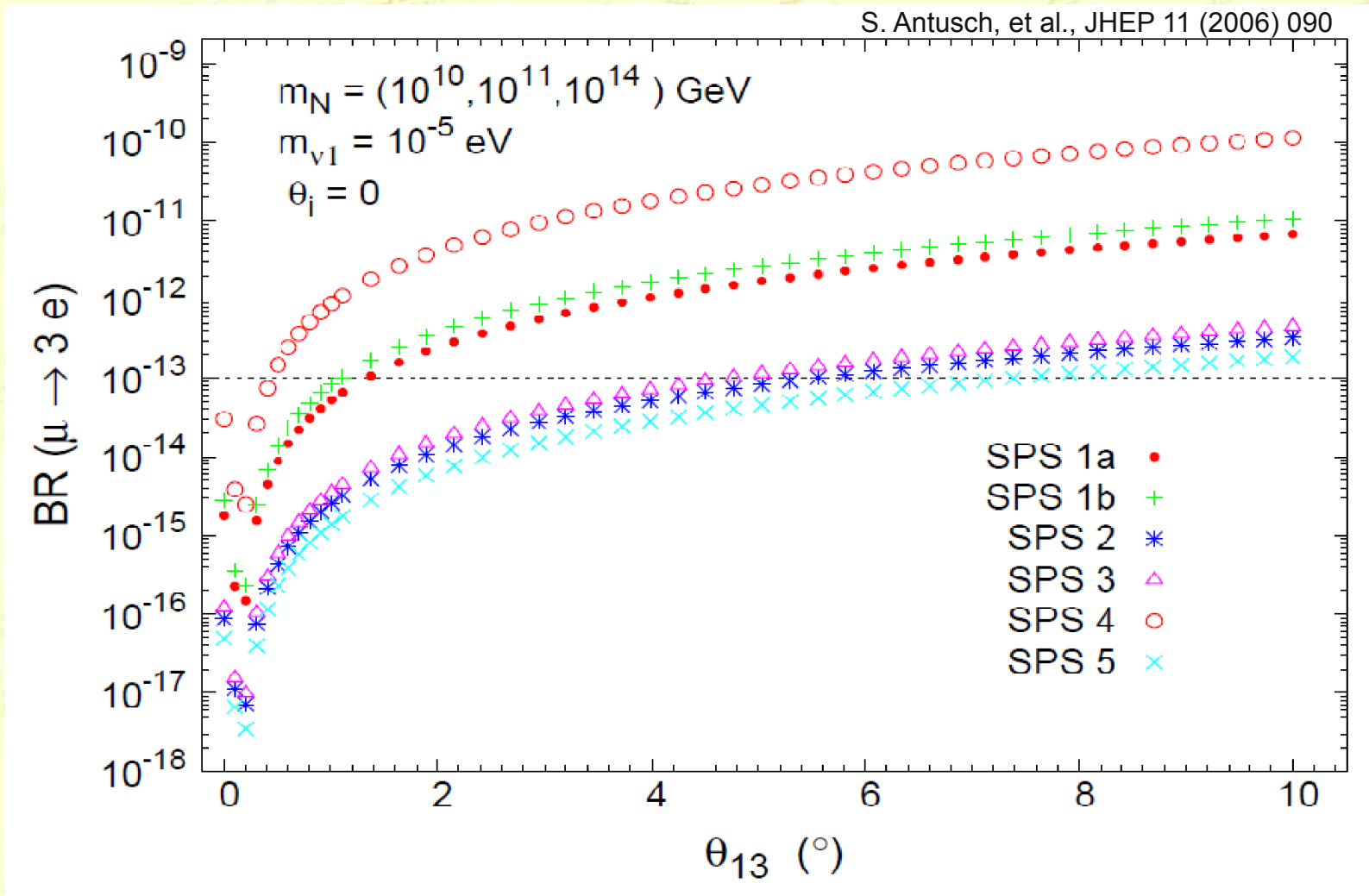
- SUSY SPS 1a
- require successful BAU (baryon asymmetry in universe)



→ sensitivity to heavy Majorana Neutrino Masses



# cMSSM Seesaw with Leptogenesis



$$\sin^2 \Theta_{13} < 0.057 \text{ (PDG)}$$

# Motivation to Search for $\mu^+ \rightarrow e^+e^+e^-$

# Effective Model for $\mu^+ \rightarrow e^+e^+e^-$

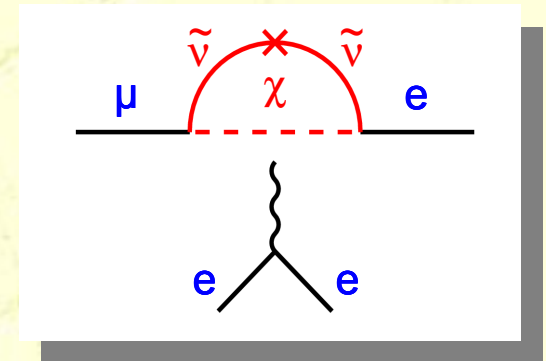
Effective charged LFV Lagrangian (Y. Kuno and Y Okada):

Tensor terms (dipole)

$$L_{\mu \rightarrow eee} = \frac{4G_F}{2} [m_\mu A_R \bar{\mu}_R \sigma^{\mu\nu} e_L F_{\mu\nu} + m_\mu A_L \bar{\mu}_L \sigma^{\mu\nu} e_R F_{\mu\nu}]$$

e.g. Supersymmetry

dipole coupling





# Effective Model for $\mu^+ \rightarrow e^+e^+e^-$

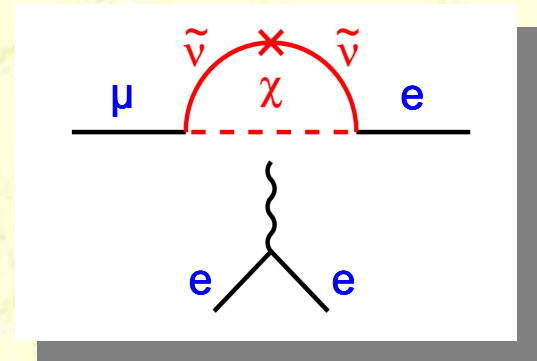
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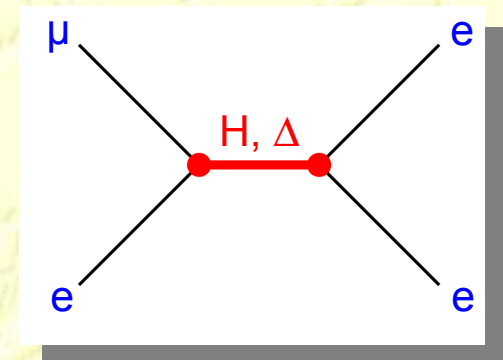


Four-fermion terms

$$\begin{aligned} &+ g_1 (\bar{\mu}_R e_L) (\bar{e}_R e_L) + g_2 (\bar{\mu}_L e_R) (\bar{e}_L e_R) && \text{(scalar)} \\ &+ g_3 (\bar{\mu}_R \gamma e_R) (\bar{e}_R \gamma e_R) + g_4 (\bar{\mu}_L \gamma e_L) (\bar{e}_L \gamma e_L) && \text{(vector)} \\ &+ g_5 (\bar{\mu}_R \gamma e_R) (\bar{e}_L \gamma e_L) + g_6 (\bar{\mu}_L \gamma e_L) (\bar{e}_R \gamma e_R) + H.c. \end{aligned}$$

e.g. Higgs, Z', Doubly Charged Higgs

tree diagram

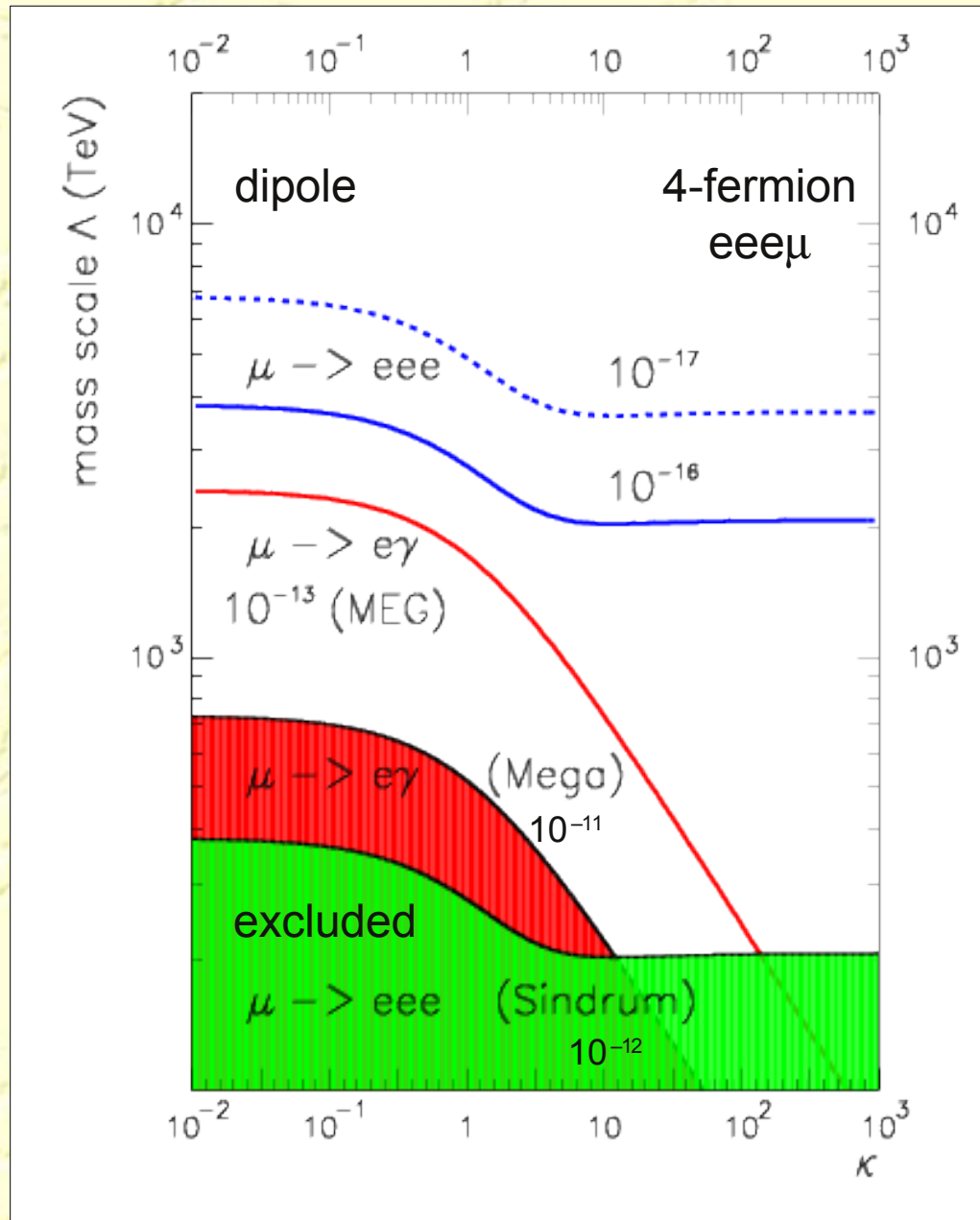


# Testing new Mass Scales

Effective cLFV Lagrangian:

$$L = \frac{m_\mu}{\Lambda^2 (1+\kappa)} H^{dipole} + \frac{\kappa}{\Lambda^2 (1+\kappa)} J_\nu^{e\mu} J^{\nu,ee}$$

“André de Gouvêa”  
plot for  $\mu eee$



# Testing new Mass Scales

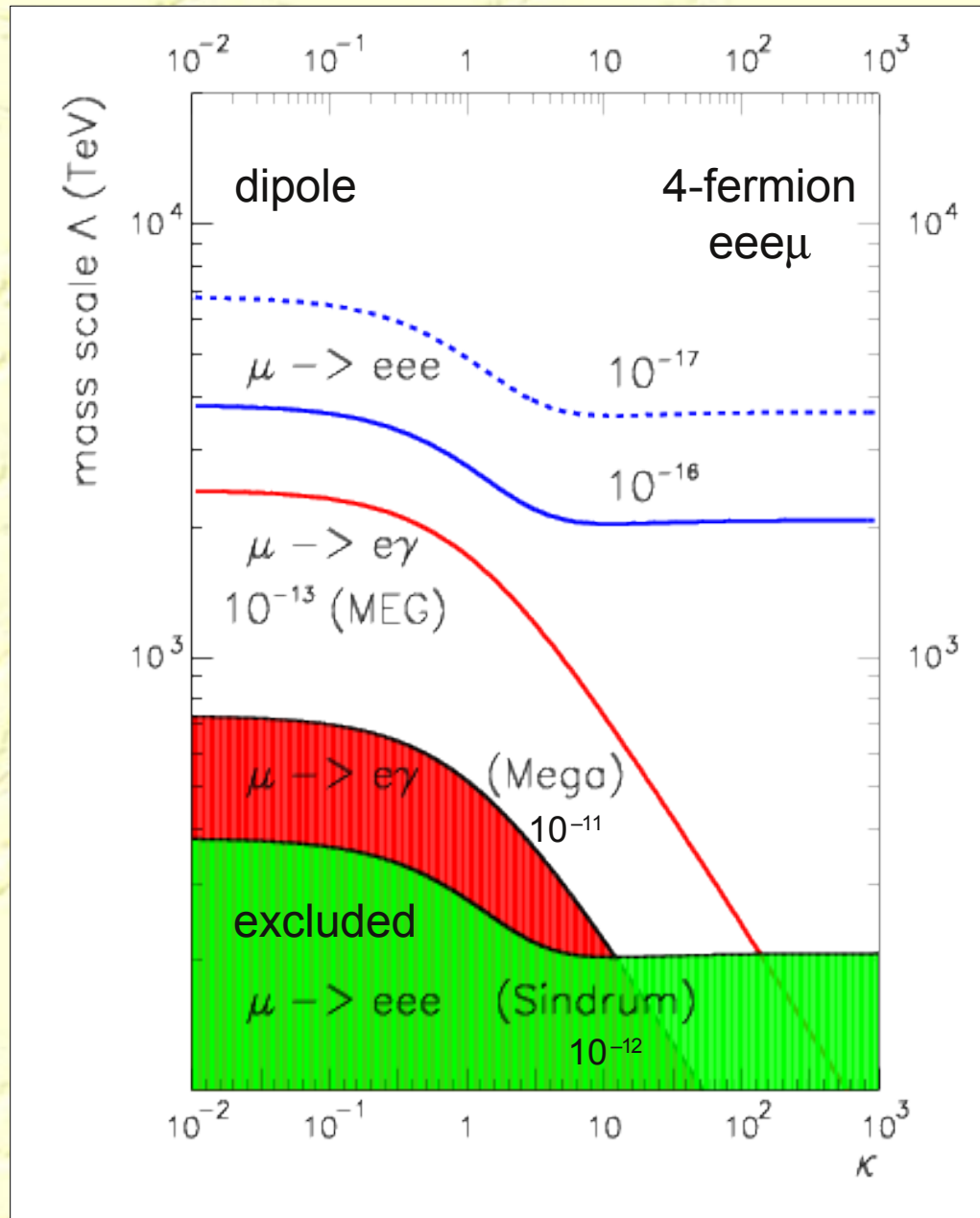
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- Almost factor 2 higher mass reach beyond future MEG

$\Lambda > 4 \cdot 10^3 \text{ TeV}$  (LFV dipole couplings)

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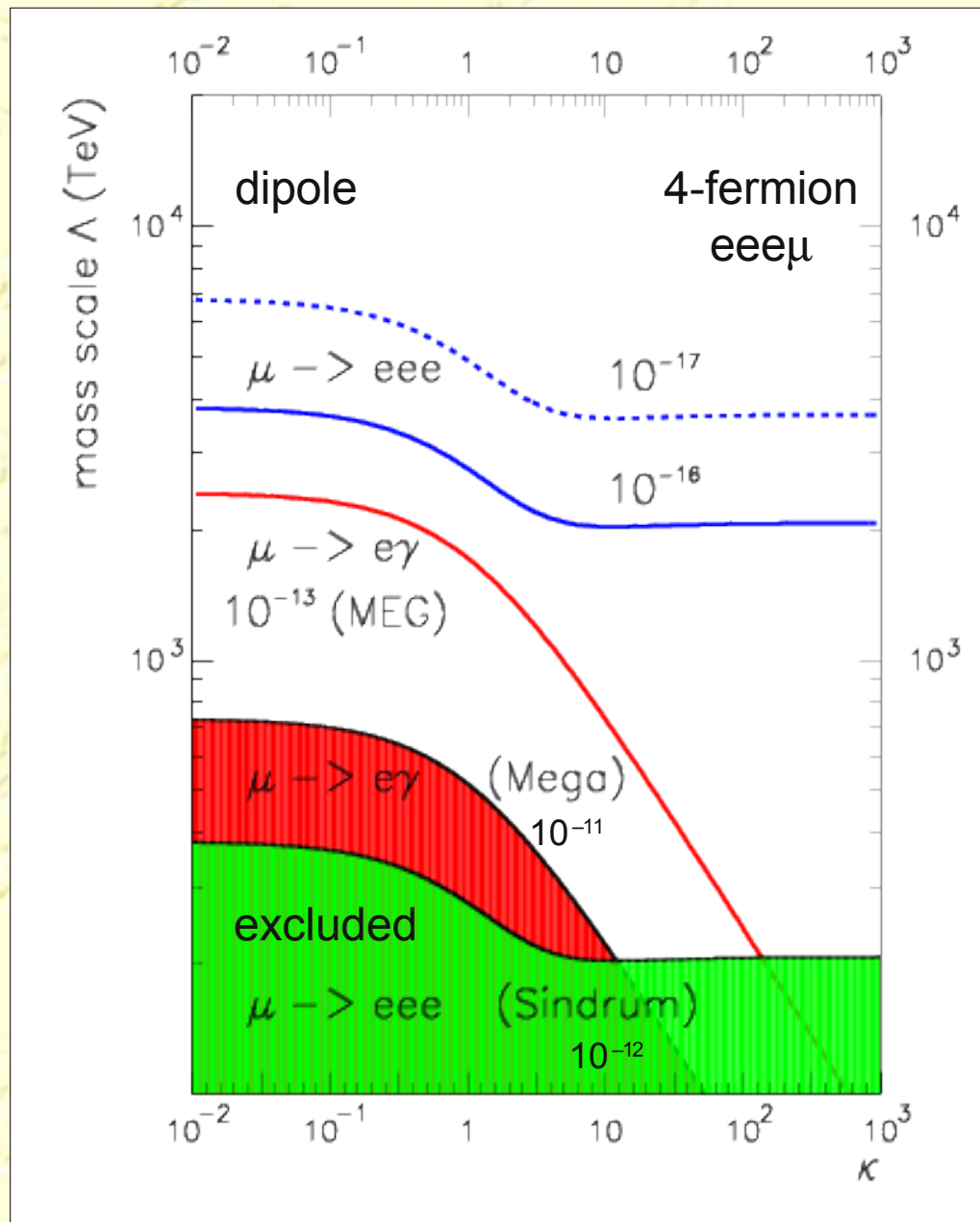
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$\Lambda > 4 \cdot 10^3 \text{ TeV}$  (LFV dipole couplings)

- x 10 mass reach beyond SINDRUM

$\Lambda > 2 \cdot 10^3 \text{ TeV}$  (LFV four-fermion couplings)

“André de Gouvêa”  
plot for  $\mu e e e$



# Predictions: $\mu \rightarrow eee$ versus $\mu \rightarrow e\gamma$

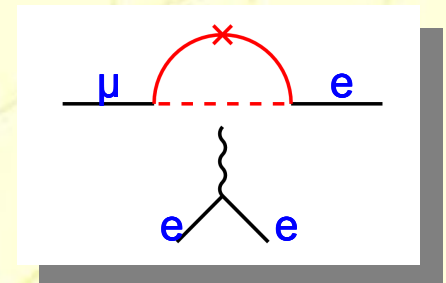
- In case of dominating LFV dipole couplings  $\kappa = 0$  ( $A_{L,R} \gg g_i$ )

$$\frac{B(\mu \rightarrow eee)}{B(\mu \rightarrow e\gamma)} \approx 0.006$$

$B(\mu \rightarrow eee) = 10^{-15}$  corresponds to  $B(\mu \rightarrow e\gamma) \sim 10^{-13}$

$B(\mu \rightarrow eee) = 10^{-16}$  corresponds to  $B(\mu \rightarrow e\gamma) \sim 10^{-14}$

dipole coupling



# Predictions: $\mu \rightarrow eee$ versus $\mu \rightarrow e\gamma$

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$$\frac{B(\mu \rightarrow eee)}{B(\mu \rightarrow e\gamma)} \approx 0.006$$

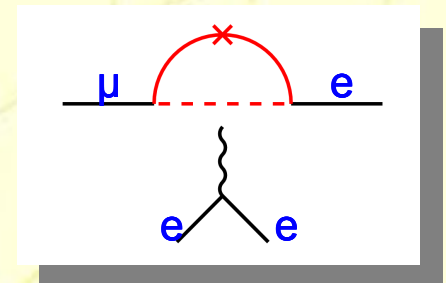
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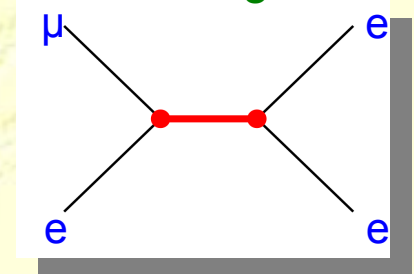
- Specific Models

Predictions	$B(\mu \rightarrow eee) / B(\mu \rightarrow e\gamma)$	$B(\mu \rightarrow eee)$
mSUGRA + seesaw	$\sim 10^{-2}$	$< 10^{-13}$
SUSY + SO(10)	$\sim 10^{-2}$	$< 10^{-13}$
SUSY + Higgs	$\sim 10^{-2}$	$< 10^{-13}$
Z', Kaluzza Klein	$> 1$	
Little Higgs	0.1 - 1	$< 10^{-13}$
Higgs Triplet	$10^{-3} - 10^{+3}$	$< 10^{-12}$

dipole coupling



tree diagram

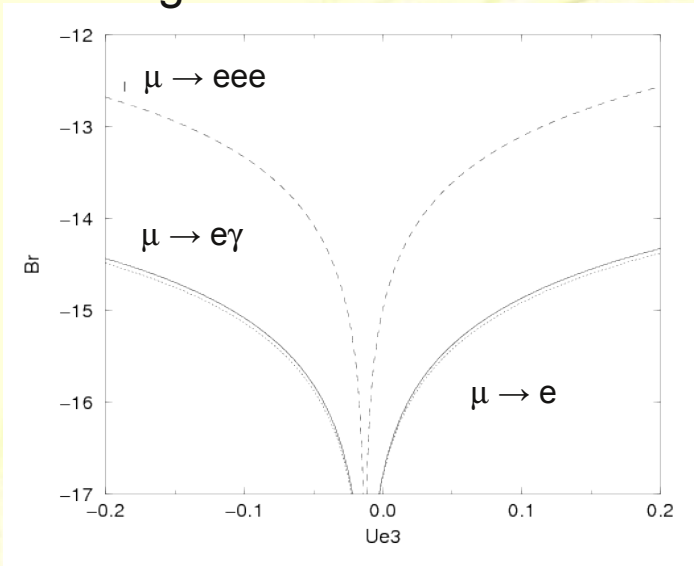




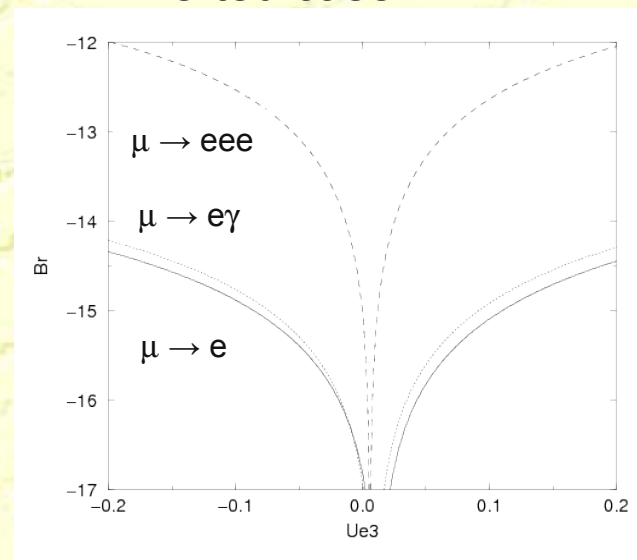
# Higgs Triplet Models

M. Kakizaki et al., Phys. Lett. B 566 (2003) 210

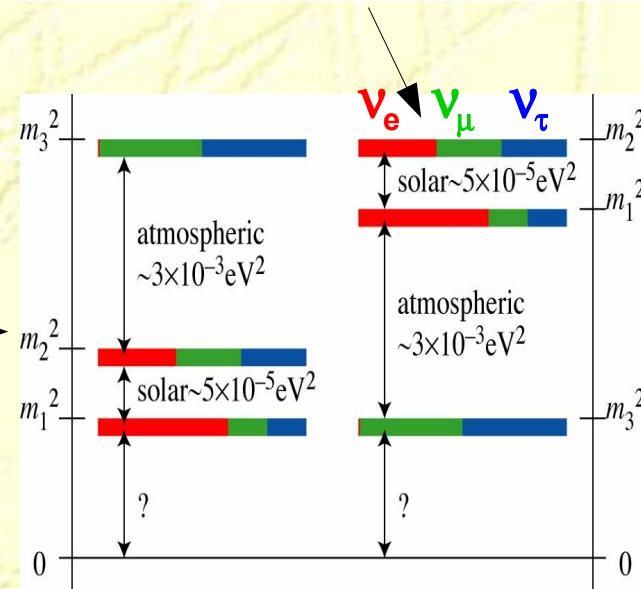
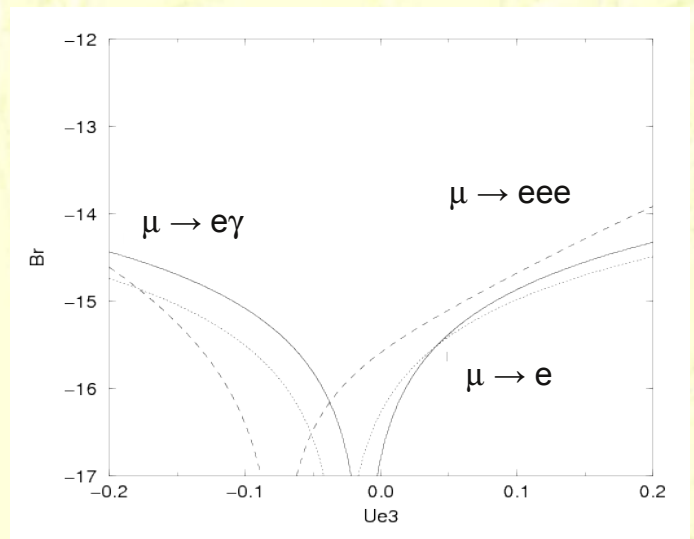
degenerate case



inverted case



hierarchical case



# CP Violation in $\mu \rightarrow eee$

- Measurement of CP violation requires interference of diagrams
- 3-body decay kinematics allows for study of discrete symmetries!

Okada et al. PRD 61, 094001 (2000)

$$\frac{dB}{dx_1 dx_2 d \cos \theta d \varphi} = \frac{3}{2\pi} [C_1 \alpha_1(x_1, x_2)(1 + P \cos \theta) + C_2 \alpha_1(x_1, x_2)(1 - P \cos \theta)$$

$$+ C_3 \{ \alpha_2(x_1, x_2) + P \beta_1(x_1, x_2) \cos \theta + P \gamma_1(x_1, x_2) \sin \theta \cos \varphi \}$$

$$+ C_4 \{ \alpha_2(x_1, x_2) - P \beta_1(x_1, x_2) \cos \theta - P \gamma_1(x_1, x_2) \sin \theta \cos \varphi \}$$

$$+ C_5 \{ \alpha_3(x_1, x_2) + P \beta_2(x_1, x_2) \cos \theta + P \gamma_2(x_1, x_2) \sin \theta \cos \varphi \}$$

$$+ C_6 \{ \alpha_3(x_1, x_2) - P \beta_2(x_1, x_2) \cos \theta - P \gamma_2(x_1, x_2) \sin \theta \cos \varphi \}$$

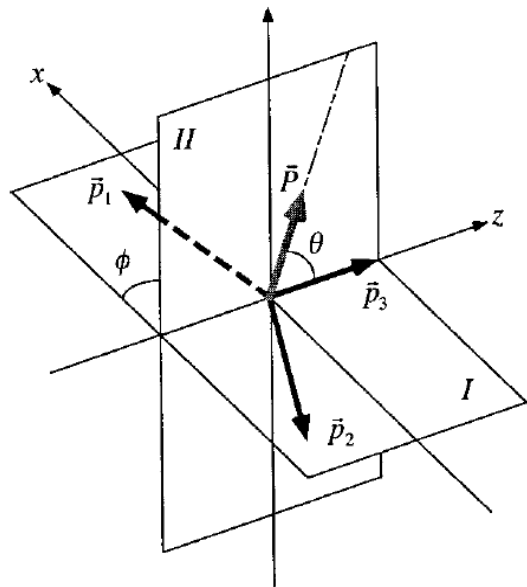
$$+ C_7 \{ \alpha_4(x_1, x_2)(1 - P \cos \theta) + P \gamma_3(x_1, x_2) \sin \theta \cos \varphi \}$$

$$+ C_8 \{ \alpha_4(x_1, x_2)(1 + P \cos \theta) - P \gamma_3(x_1, x_2) \sin \theta \cos \varphi \}$$

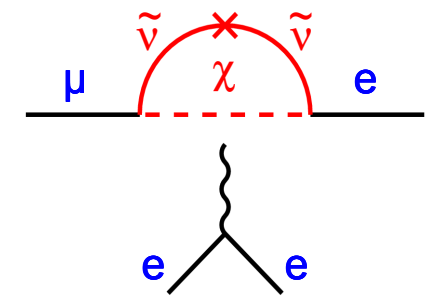
$$+ C_9 \{ \alpha_5(x_1, x_2)(1 + P \cos \theta) - P \gamma_4(x_1, x_2) \sin \theta \cos \varphi \}$$

$$+ C_{10} \{ \alpha_5(x_1, x_2)(1 - P \cos \theta) + P \gamma_4(x_1, x_2) \sin \theta \cos \varphi \}$$

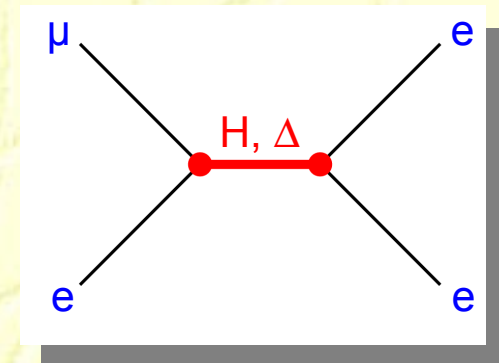
$$+ C_{11} P \gamma_3(x_1, x_2) \sin \theta \sin \varphi - C_{12} P \gamma_4(x_1, x_2) \sin \theta \sin \varphi],$$



dipole coupling



tree diagram



**T-odd**

(can also distinguish e.g. SU(5) from SO(10) models)

# Motivation for $\mu^+ \rightarrow e^+e^+e^-$ Search I

- New Particles at the “Terascale” naturally induce LFV

$$\left( \frac{\Delta_M^2}{M^2} \right)^2$$

- Search  $\mu^+ \rightarrow e^+e^+e^-$  is complementary to other LFV searches



# Motivation for $\mu^+ \rightarrow e^+e^+e^-$ Search II

- Advances in detector technologies allow for **high rate / high precision** experiments at low energies
- Plans to improve PSI beamlines and targets:  $> 10^9$  muon stops/s
  - would allow to test muon decay branching ratios at  $10^{-16}$
  - current exp. limit  $B(\mu^+ \rightarrow e^+e^+e^-) = 10^{-12}$  (Bellgard 1988)

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- A search for  $B(\mu^+ \rightarrow e^+e^+e^-) > 10^{-16}$  has a large potential to find **LFV signal** or to set very stringent bounds on **new physics**



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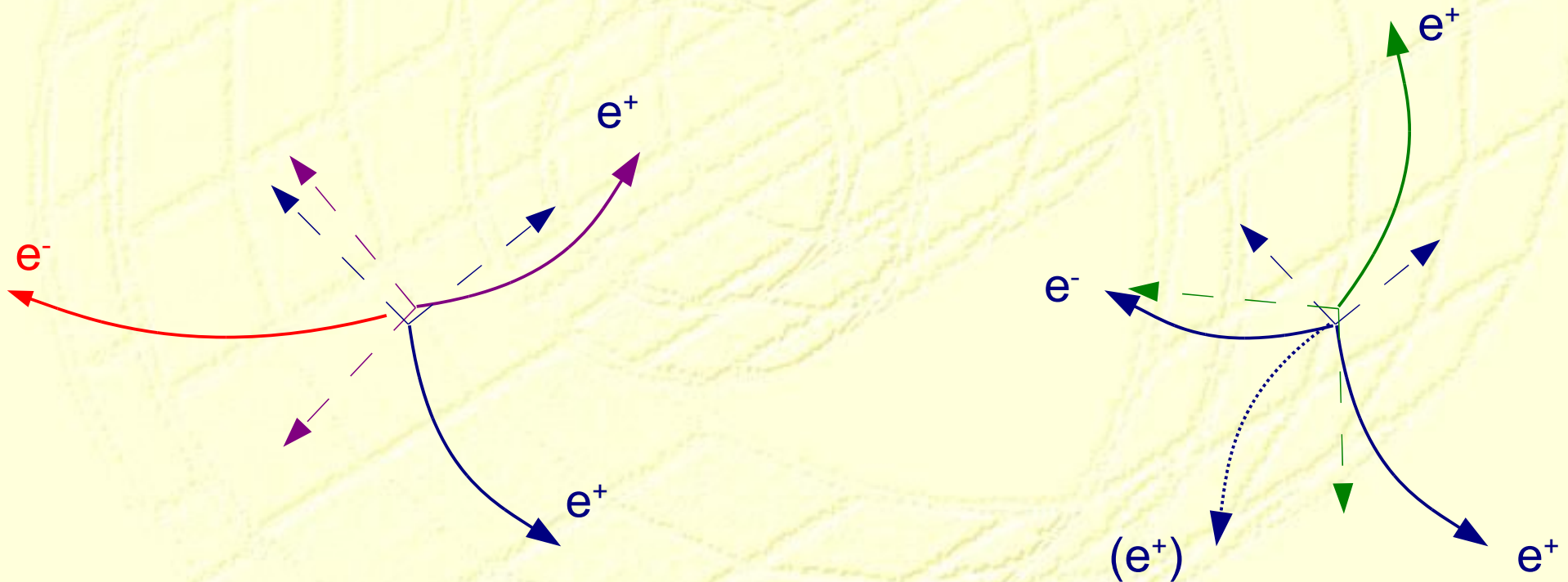
# **Backgrounds and Previous Experiments**



# Backgrounds for $\mu^+ \rightarrow e^+e^+e^-$

- **Combinatorial Background (Pile up):**

- Two muon decays  $2 \times (\mu^+ \rightarrow e^+ \nu \nu)$  and one fake  $e^-$  (wrong charge: reconstruction, Bhabha, back-curling  $e^+ \rightarrow e^-$ )
- Radiative decay with internal conversion  $\mu \rightarrow (e^+) e^+e^- \nu \nu$  and muon decay  $\mu^+ \rightarrow e^+ \nu \nu$



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- ◆ kinematic constraints
- ◆ vertex requirements

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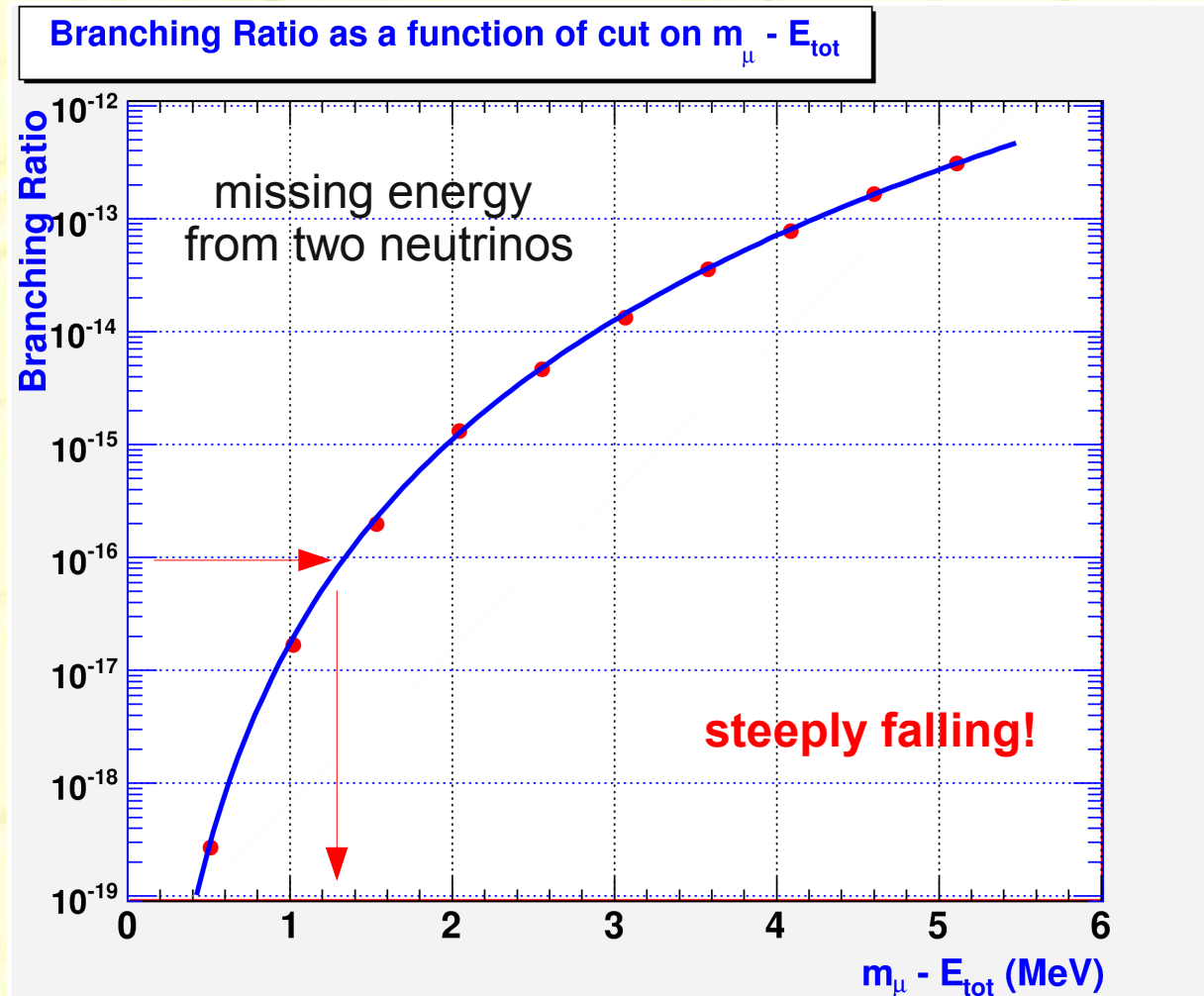
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- **Radiative decay with internal conversion  $\mu^+ \rightarrow e^+e^+e^- \nu \nu$**

**irreducible background**  $\text{BR}(\mu^+ \rightarrow e^+e^+e^- \nu \nu) = 3.4 \cdot 10^{-5}$



# Background from $\mu^+ \rightarrow e^+e^+e^- \nu \nu$



R.M.Djilkibaev and  
R.V.Konoplich  
PRD79 (2009)

Good energy (momentum) resolution  $E_{\text{tot}} = \sum |E_i| \sim \sum |p_i|$  essential !!!

# Comparison: $\mu$ -Decay Experiments

- **Sindrum 1988:**

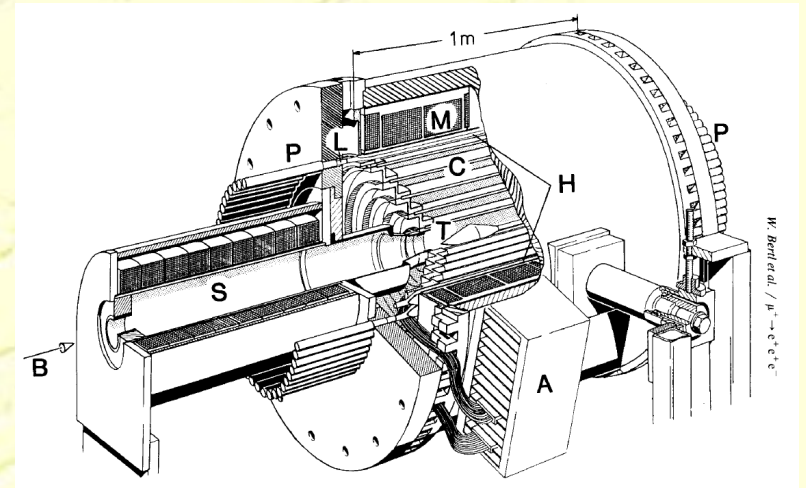
$$\sigma_p/p (50 \text{ MeV}/c) = 5.1\%$$

$$\sigma_p/p (20 \text{ MeV}/c) = 3.6\%$$

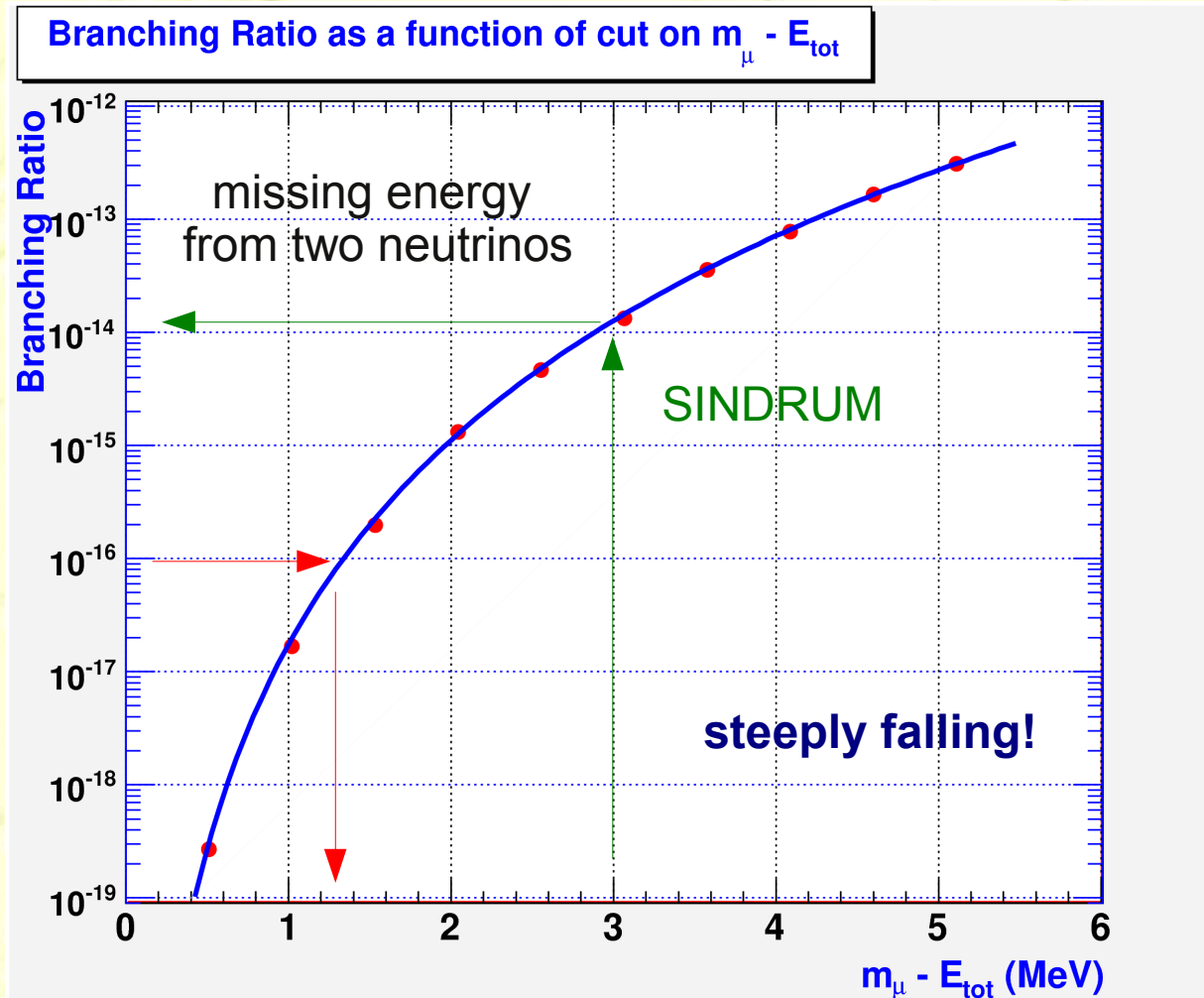
$$\sigma_\theta (20 \text{ MeV}/c) = 28 \text{ mrad}$$

$$\text{VTX: } \sigma_d = \sim 1 \text{ mm}$$

$$\text{X0(MWPC)} = 0.08\% - 0.17\% \text{ per layer}$$



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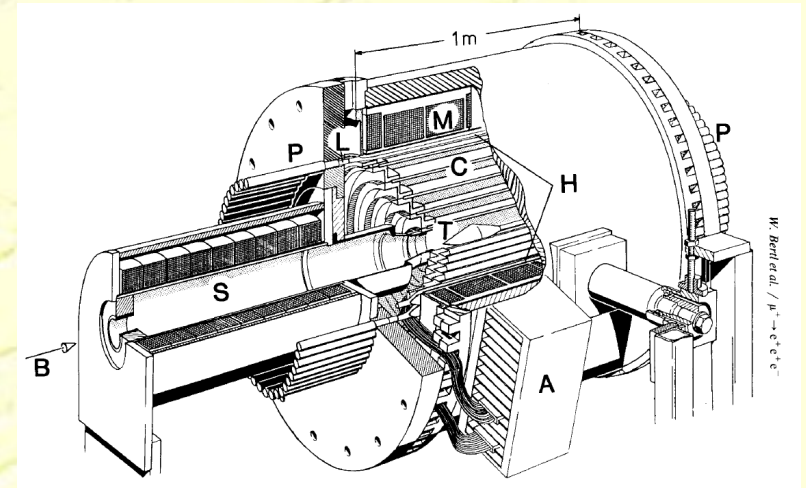
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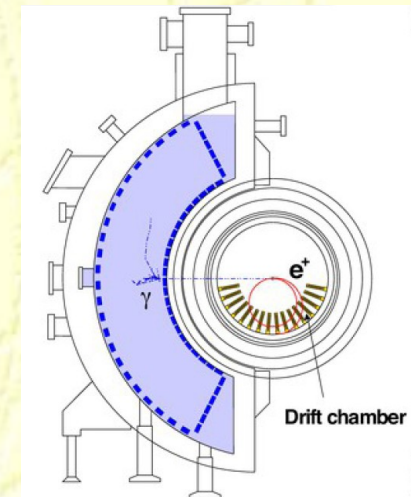
- **MEG 2010 (preliminary):**

$$\sigma_p/p (53 \text{ MeV}/c) = 0.7 \%$$

$$\sigma_\theta (53 \text{ MeV}/c) = 8 \text{ mrad}$$

$$\sigma_\phi (53 \text{ MeV}/c) = 8 \text{ mrad}$$

$$\text{VTX: } \sigma_R = 1.4 \text{ mm}, \sigma_Z = 2.5 \text{ mm}$$



# Comparison: $\mu$ -Decay Experiments

- **Sindrum 1988:**

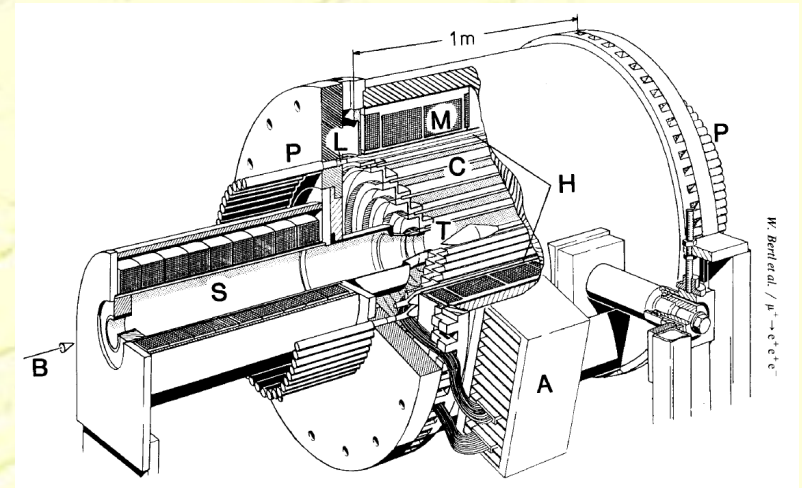
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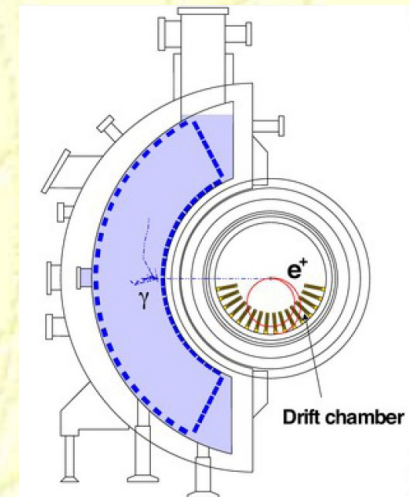
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→ **Aim for similar or better angular and momentum resolutions, high rates and better vertex resolution  $\sim 150 \mu\text{m}$  (combinatorial BG)**





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# Detector Concept and Design



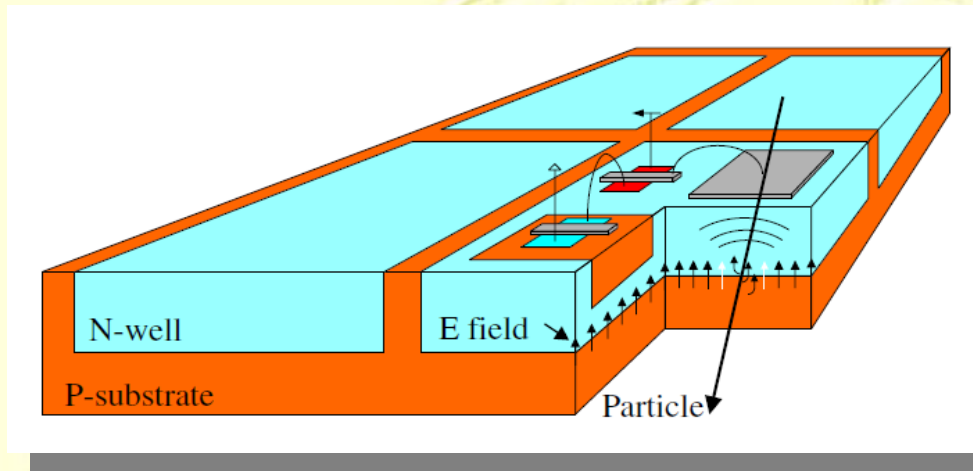
# Requirements for $\mu^+ \rightarrow e^+e^+e^-$

- **Aim for  $B(\mu^+ \rightarrow e^+e^+e^-) = 10^{-16}$** 
  - need  $10^9$  stopped muons per second
  - high rate of electrons in detector!
- **Tracking**
  - gas detector disfavored → **silicon detector**
  - fast readout
- **Momentum resolution**
  - high precision detector → **pixel sensor**
  - low multiple scattering → **thin sensors**

# Silicon Detectors Technologies

Technologies	Thickness	Speed	Readout
ATLAS pixel	260 $\mu\text{m}$	25 ns	extra RO chip
DEPFET	50 $\mu\text{m}$	slow (frames)	extra RO chip
MAPS	50 $\mu\text{m}$	slow (diffusion)	fully integrated
HV-MAPS	>30 $\mu\text{m}$	O(100ns)	fully integrated

# High Voltage Monolithic CMOS Pixel



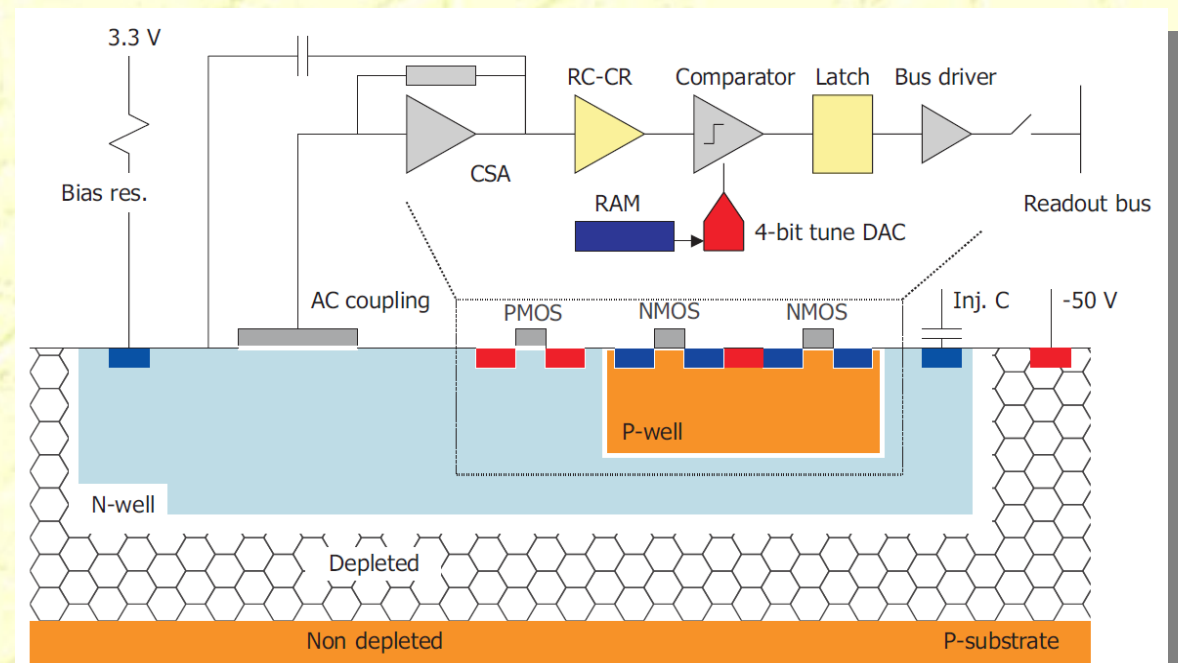
transistor logic embedded in N-well  
("smart diode array")

**New Technology!**

I. Peric, P. Fischer et al., NIM A 582 (2007) 876 (ZITI Mannheim, Uni Heidelberg)

Sensors tested successfully :

- radiation tolerant
- low noise:  $S/N > 40$
- tune DAC and zero suppression





# HV MAPS Sensor

- Preliminary Sensor Specifications

- Module Size **1 cm x 6 cm** inner and **2 cm x 6 cm** outer layer

- Pixel Size **80  $\mu\text{m}$  x 80  $\mu\text{m}$**

- **98k (196k) pixels 128 (256) x 768**

- resolution **1 bit per pixel**

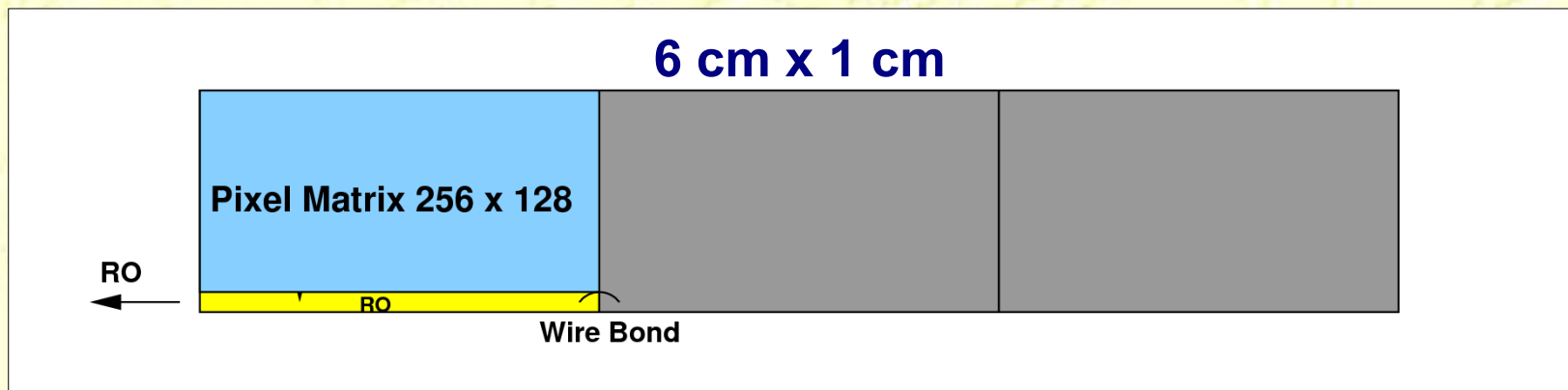
- power **150 mW/cm<sup>2</sup>**

- zero suppression

- data output **800 Mbit/s**

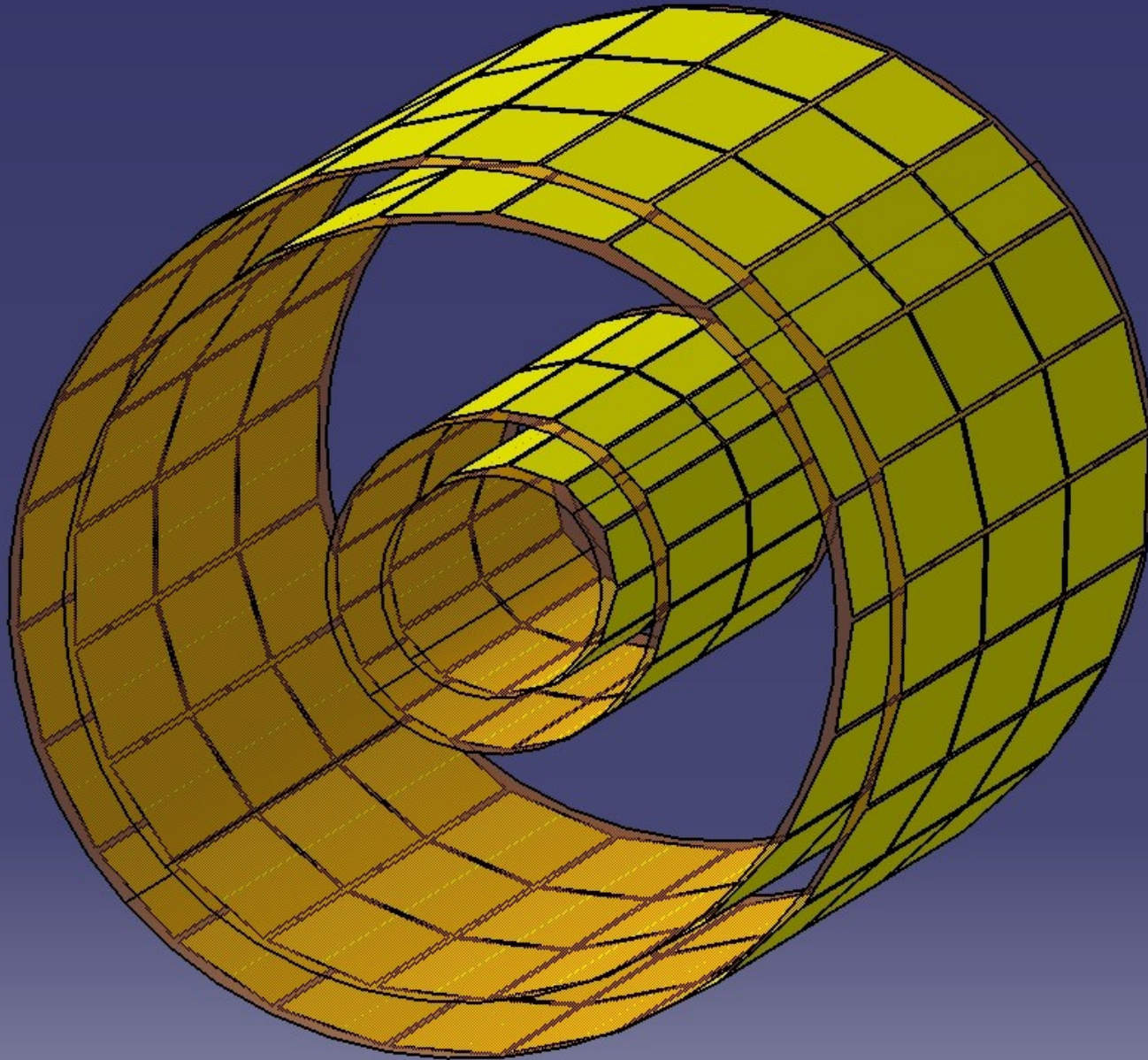
- time stamps every **100ns** (10 MHz clock → power)

first submission of test structures Feb. 2011  
(AMS HV 0.18 micron)



# Possible Tracker Layout

30-50  $\mu\text{m}$  Silicon  
on  
25  $\mu\text{m}$  Kapton





# Multiple Scattering in Silicon

Momentum range  $p = 15\text{-}53 \text{ MeV}$

→ **multiple scattering!**

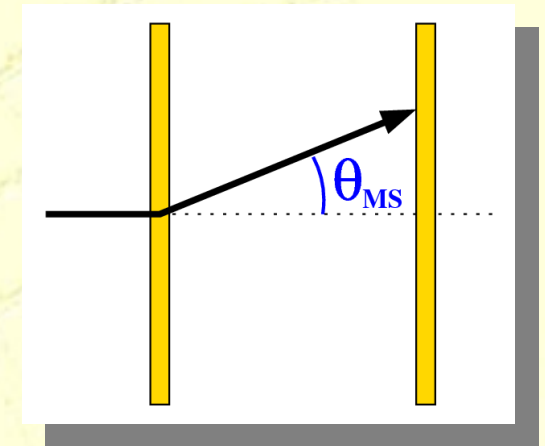
Example:  $p = 53 \text{ MeV}/c$

• MEG:  $\sigma_{\theta}^{\text{MS}} = 8 \text{ mrad}$

→ multiple scatt. per layer  $X/X_0 = 0.1\%$  → corresponds to **90  $\mu\text{m}$  Silicon**

•  $\mu \rightarrow \text{eee}$ :  $\sigma_{\theta}^{\text{MS}} = 5 \text{ mrad}$

→ multiple scatt. per layer  $X/X_0 = 0.044\%$  → corresponds to **40  $\mu\text{m}$  Silicon**

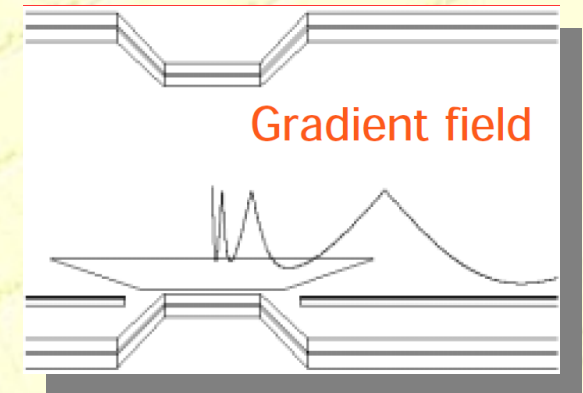
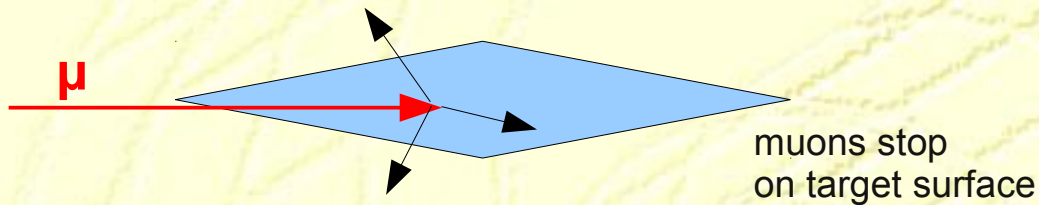


**Pixel sensors can be thinned down to 30-50  $\mu\text{m}$**   
(examples CMOS MAPS, DEPFET 50  $\mu\text{m}$ )



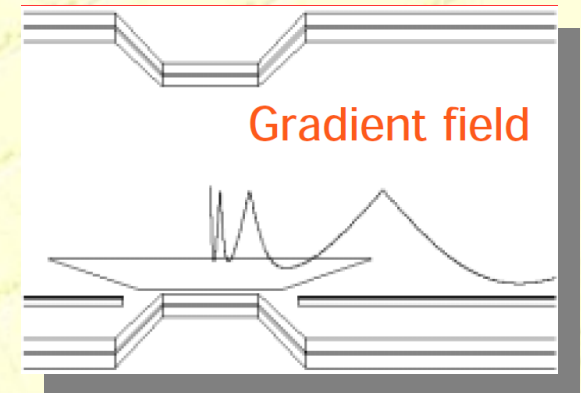
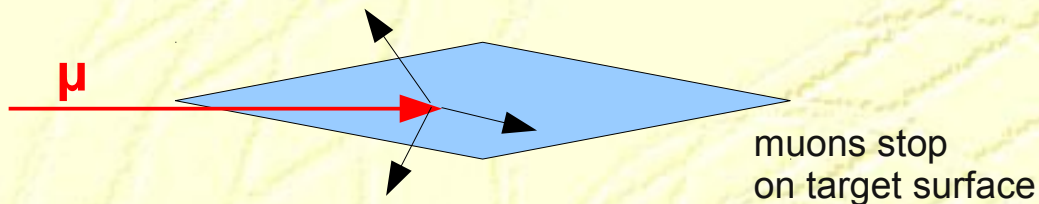
# “Novel” Experimental Concept

- Strong Magnet (e.g. Cobra from MEG)
- Hollow Double Cone Target (Sindrum)



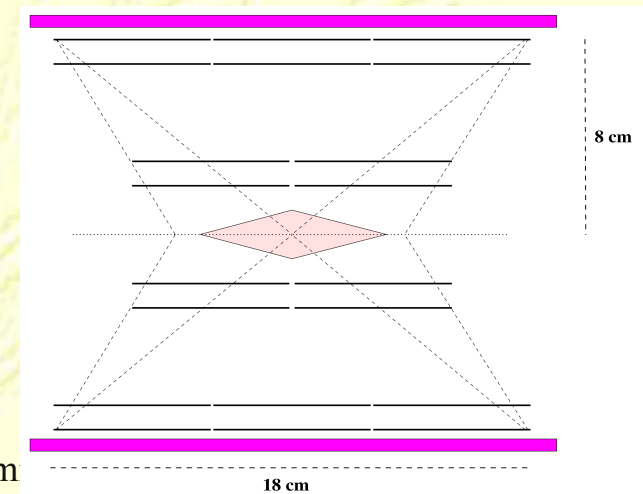
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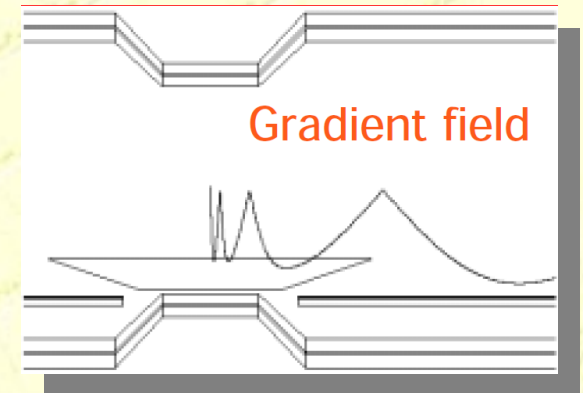
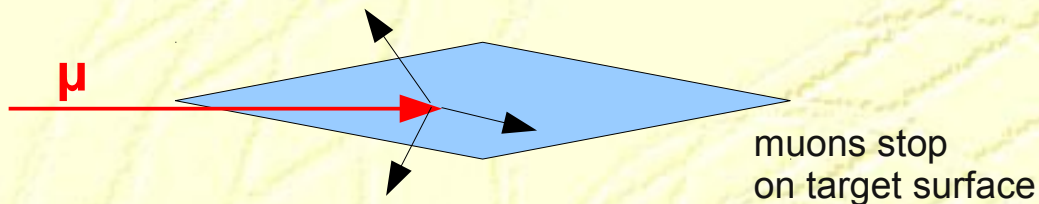
- Silicon pixel detector for tracking

- high resolution
- precise hit position  $80 \mu\text{m} \times 80 \mu\text{m}$  (c.t. multiple scattering  $\sigma_{\text{MS}} \sim 150 \mu\text{m}$ )



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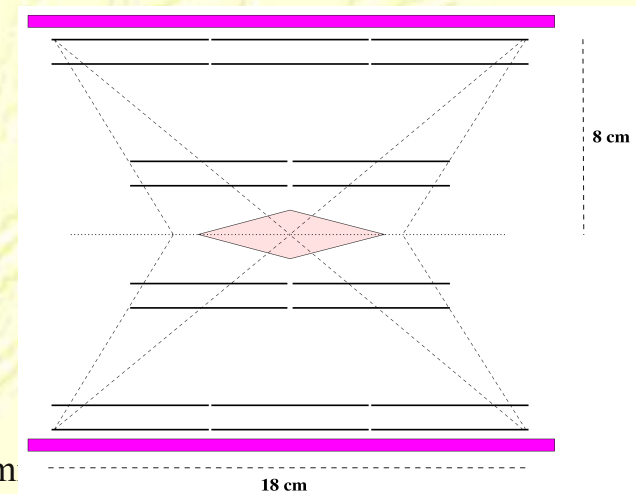


- Silicon pixel detector for tracking

- high resolution
- precise hit position **80 μm x 80 μm** (c.t. multiple scattering  $\sigma_{MS} \sim 150 \mu\text{m}$ )

- Scintillating fiber tracker for timing

- excellent timing  $\Delta T = 100 \text{ ps}$
- good spatial resolution
- vector tracking (particle direction)





# DC Muon Beams at PSI

- $\mu$ E1 beamline with rates up to  $\sim 5 \cdot 10^8$  muons/s
- $\pi$ E5 beamline (MEG experiment)  $\sim 10^8$  muons/s
- $\mu$ E4 beamline  $\sim 10^9$  muons/s
- SINQ target could even provide  $\sim 10^{10}$  muons/s
- New experiment (final stage) requires **muon rates  $\geq 1e9/s$**  focussed and collimated on a spot with about  $d=2$  cm diameter



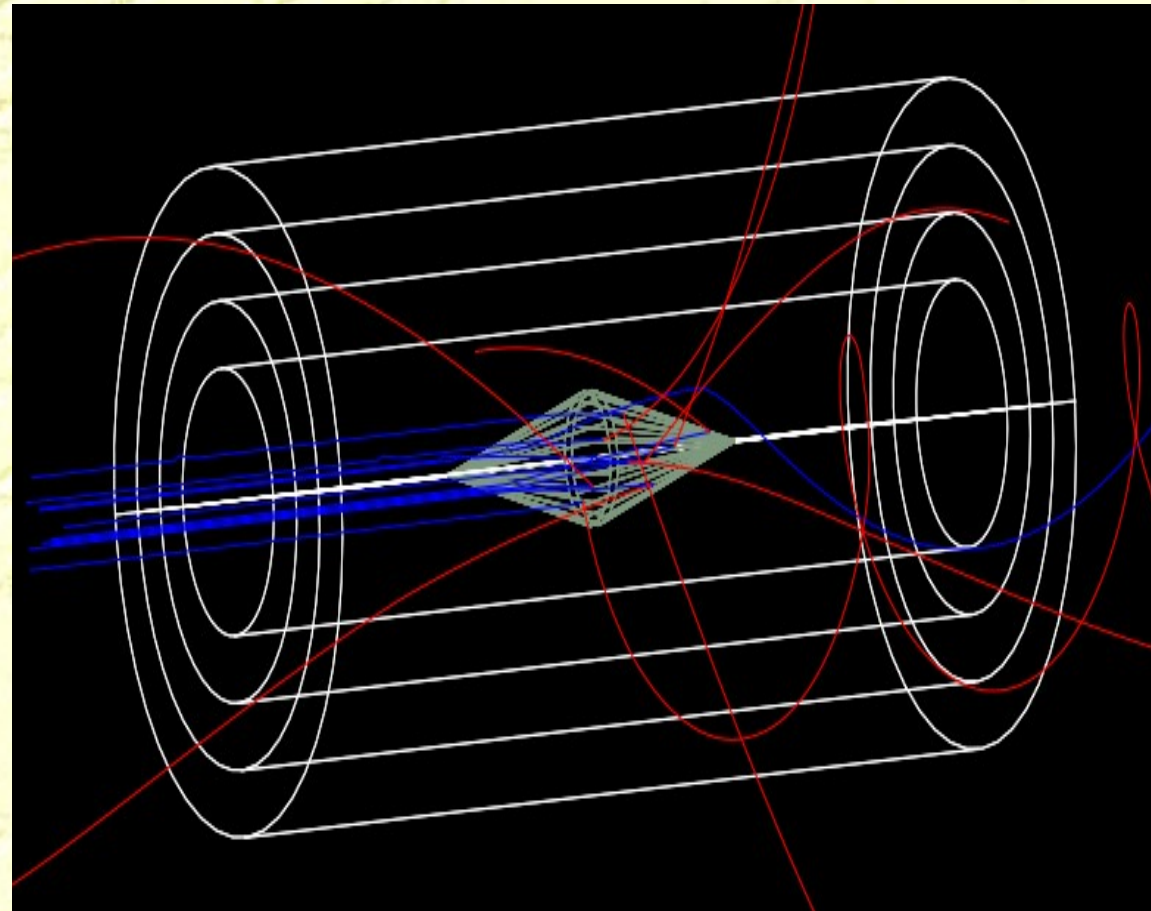
# Target and Vertex Resolution

## Sindrum-like Hollow Double Cone Target:

- total length of target:  $\sim 7$  cm
- diameter: 2 cm
- thickness of hollow cone  $\sim 60$   $\mu\text{m}$  (Al)
- **vertex resolution:  $\sim 150$   $\mu\text{m}$**

Simulation Model

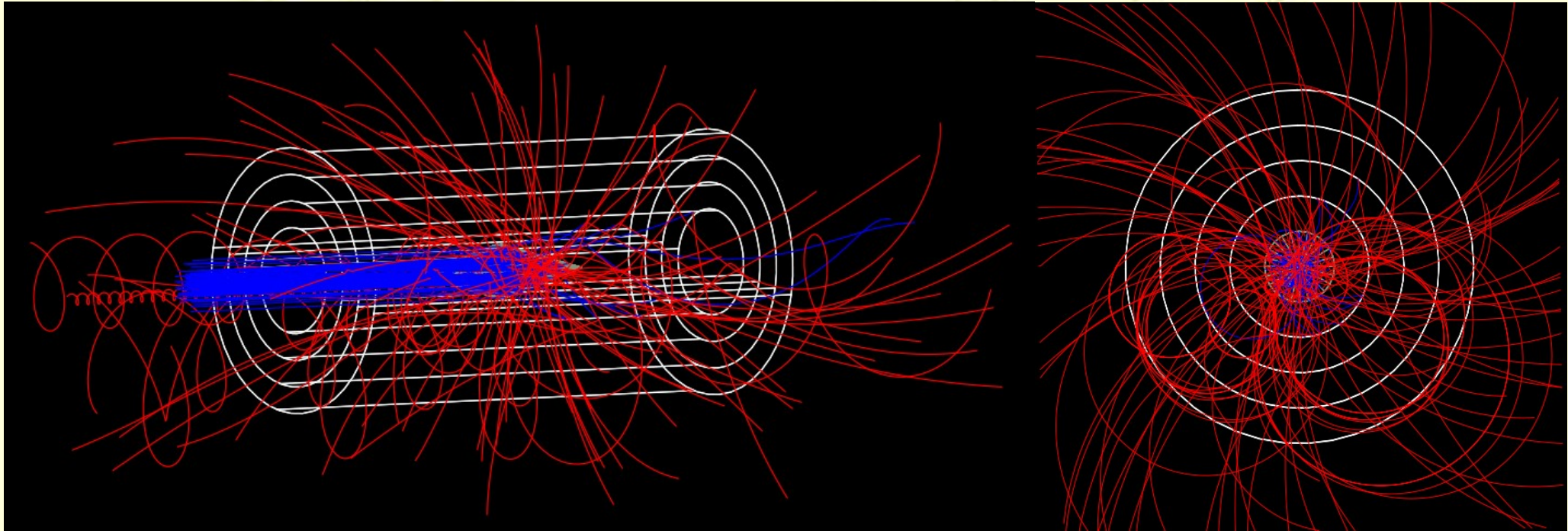
allows to suppress combinatorial BG  
by factor  $5 \cdot 10^{-5}$





# Timing Resolution

$\int dt = 100 \text{ ns}$ : 100 decays @  $10^9$  muon stops/s

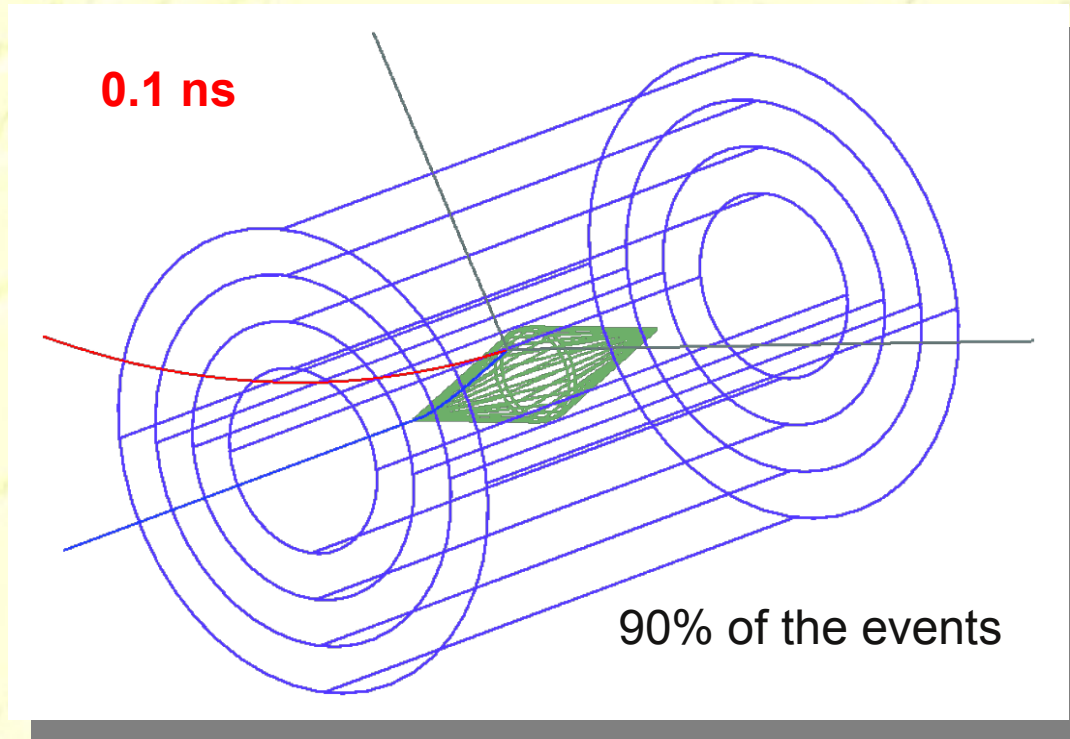


timing resolution silicon: 100 ns



# Timing Resolution

$\int dt = 0.1 \text{ ns}$ :  $<1$  decay @  $10^9$  muon stops/s



timing resolution silicon: 100 ns

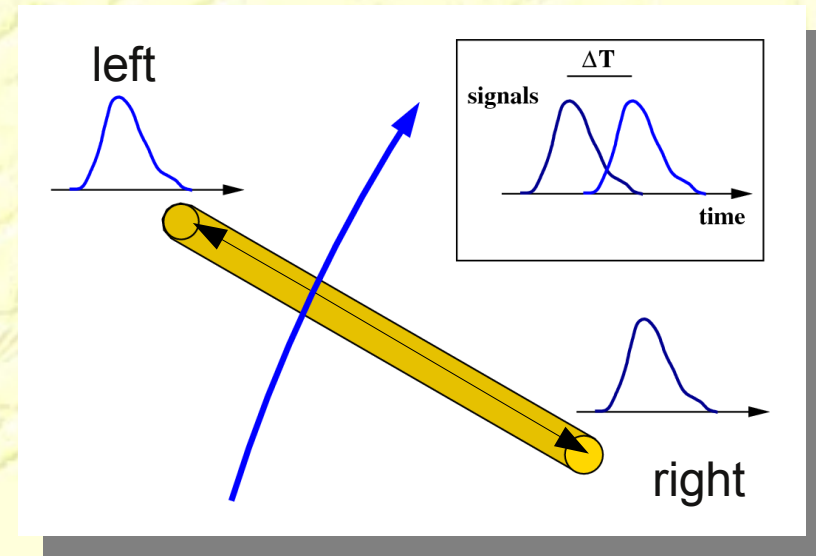
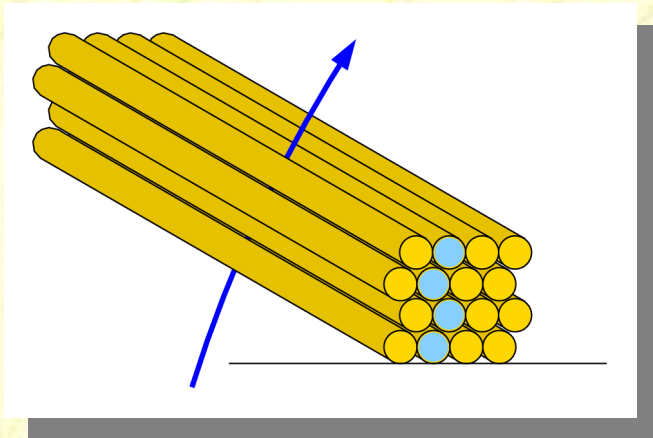
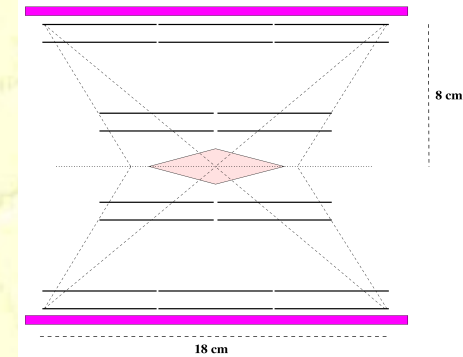
timing resolution fiber tracker:  $\sim 0.1 \text{ ns}$

→ allows to suppress combinatorial BG by **factor 1000**

# Scintillating Fiber Tracker

## Purpose:

- Measure timing of tracks precisely:  $\sigma_t = 50\text{-}100$  ps
- Allows for unambiguous silicon hit assignment
- x-y plane:  $\varnothing = 0.25\text{-}1.0$  mm fibers
- z-position: relative time difference both ends (precision 1-2 cm)



time difference between both ends

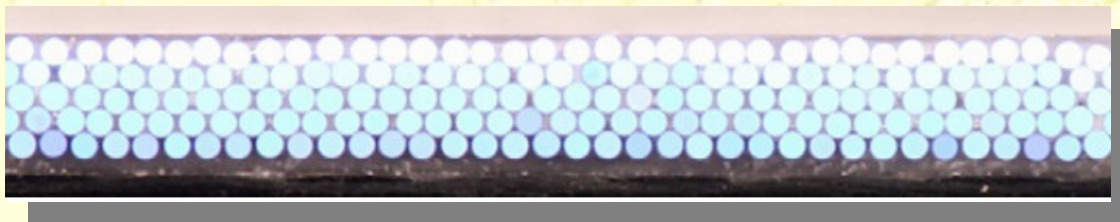
- Photodetector: SiPM

# Silicon Photomultipliers

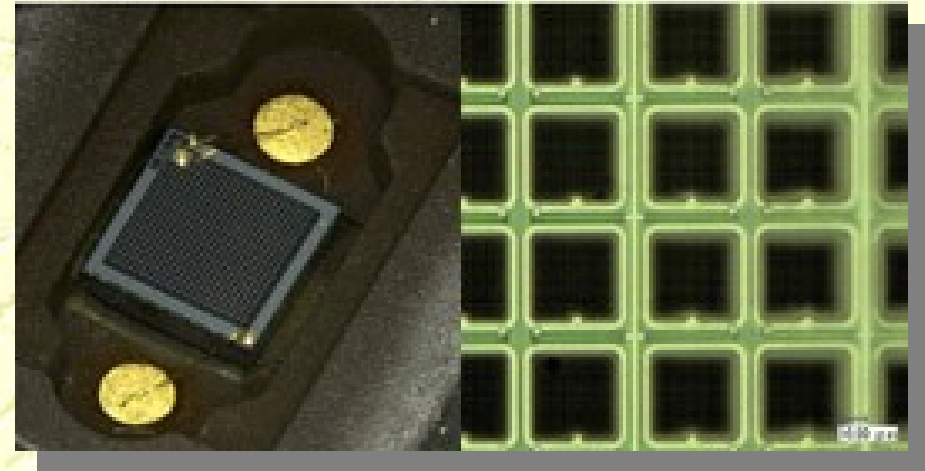
- compact
- fast  $\Delta t < 100\text{ps}$ ,  $f_{\text{max}} = 1\text{-}10\text{ MHz}$
- high gain  $1\text{e}5\text{-}1\text{e}6$
- high efficiency
- radiation hard
- insensitive to magnetic fields

used in various experiments:

- KEK T2K INGRID (photon detection)
- PEPS balloon-borne detector (scintillating fiber tracker)

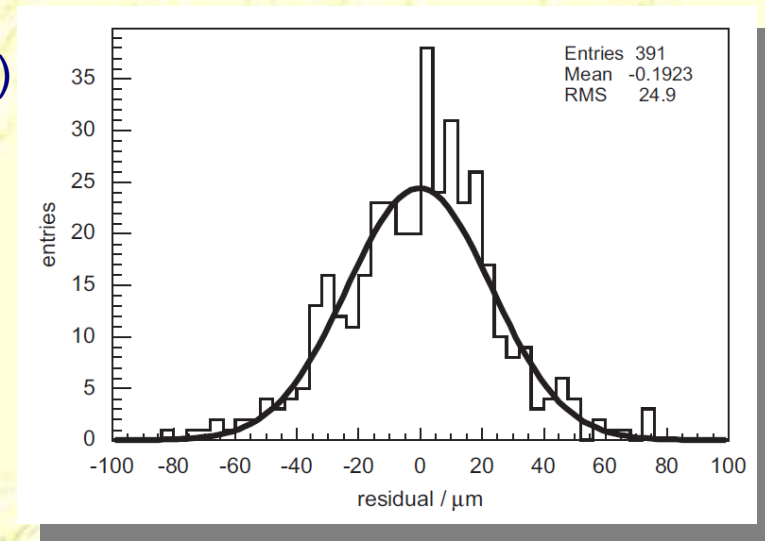


5 layers of scintillating fibers 250 $\mu\text{m}$  diameter



pixel array of avalanche photo diodes

Beischer et al., NIM A622(2010)542



spatial resolution 25  $\mu\text{m}$



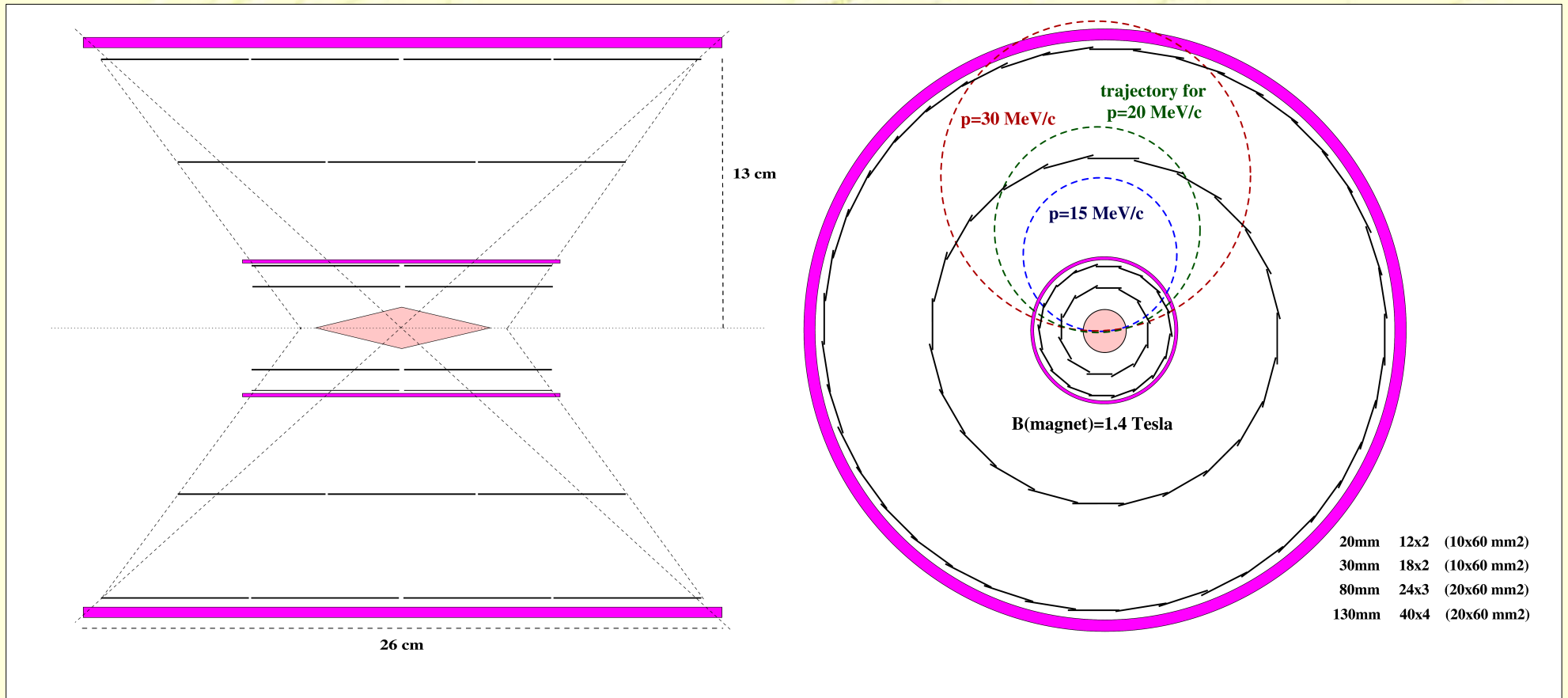
# “Big Barrel” Design

momentum resolution:  
(half-circle fit)

$$20 \text{ MeV/c: } \sigma_p/p=2.3\% \rightarrow \sigma_p=0.46 \text{ MeV/c}$$

$$35 \text{ MeV/c: } \sigma_p/p=1.3\% \rightarrow \sigma_p=0.45 \text{ MeV/c}$$

$$50 \text{ MeV/c: } \sigma_p/p=1.3\% \rightarrow \sigma_p=0.65 \text{ MeV/c}$$



precise timing information for all tracks by second **fiber tracker**



# Simulation Studies

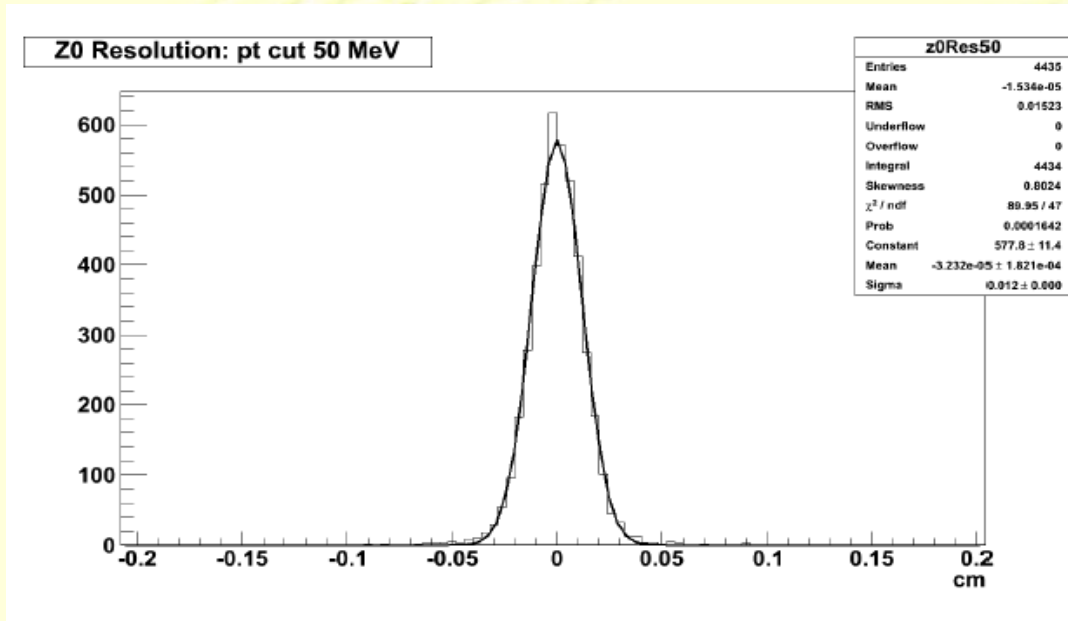
# Tracking Resolutions Studies

(R.Narayan)

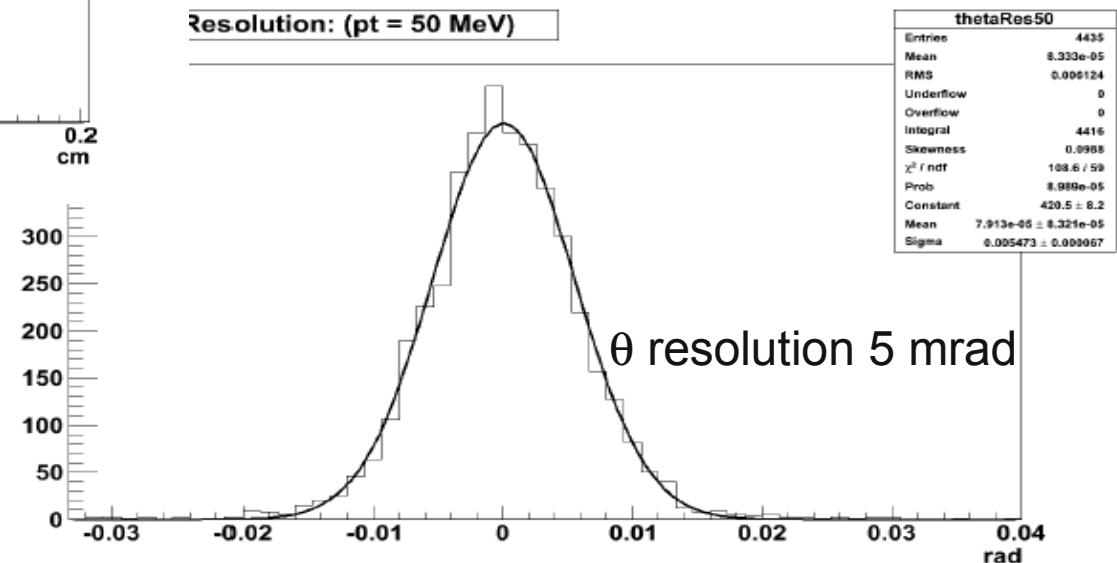
- Preliminary results obtained using Geant4 by simulating a small scale detector (radial layers at 2, 3, 4, 5 cm)



results are from preliminary studies.  
work in progress!



$Z_0$  (vertex) resolution 120  $\mu\text{m}$



$\theta$  resolution 5 mrad



# Possible Improvements

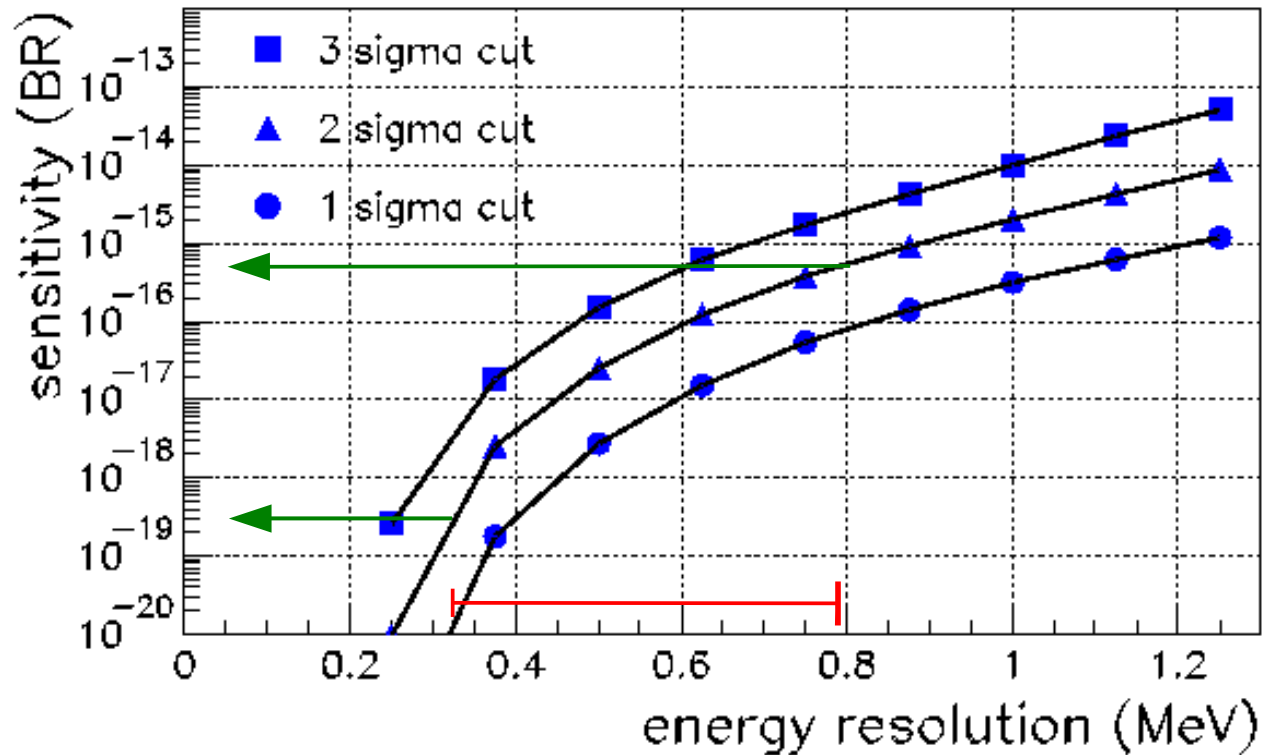
## Momentum resolution

- factor  $\sim 0.7$  fitting second track half
- factor  $\sim 0.8$  primary vertex fit (3 tracks)
- factor  $\sim 0.8$  from improved fitting (broken line fit)?
- factor  $\sim 0.9$  no inner scintillating fiber tracker

$$\rightarrow \sigma_E = 0.78-0.91 \text{ MeV} \rightarrow \sigma_E = 0.32-0.36 \text{ MeV}$$

# Simulated Sensitivity

Rate of  $\mu \rightarrow eee\nu$  as function of the energy resolution:



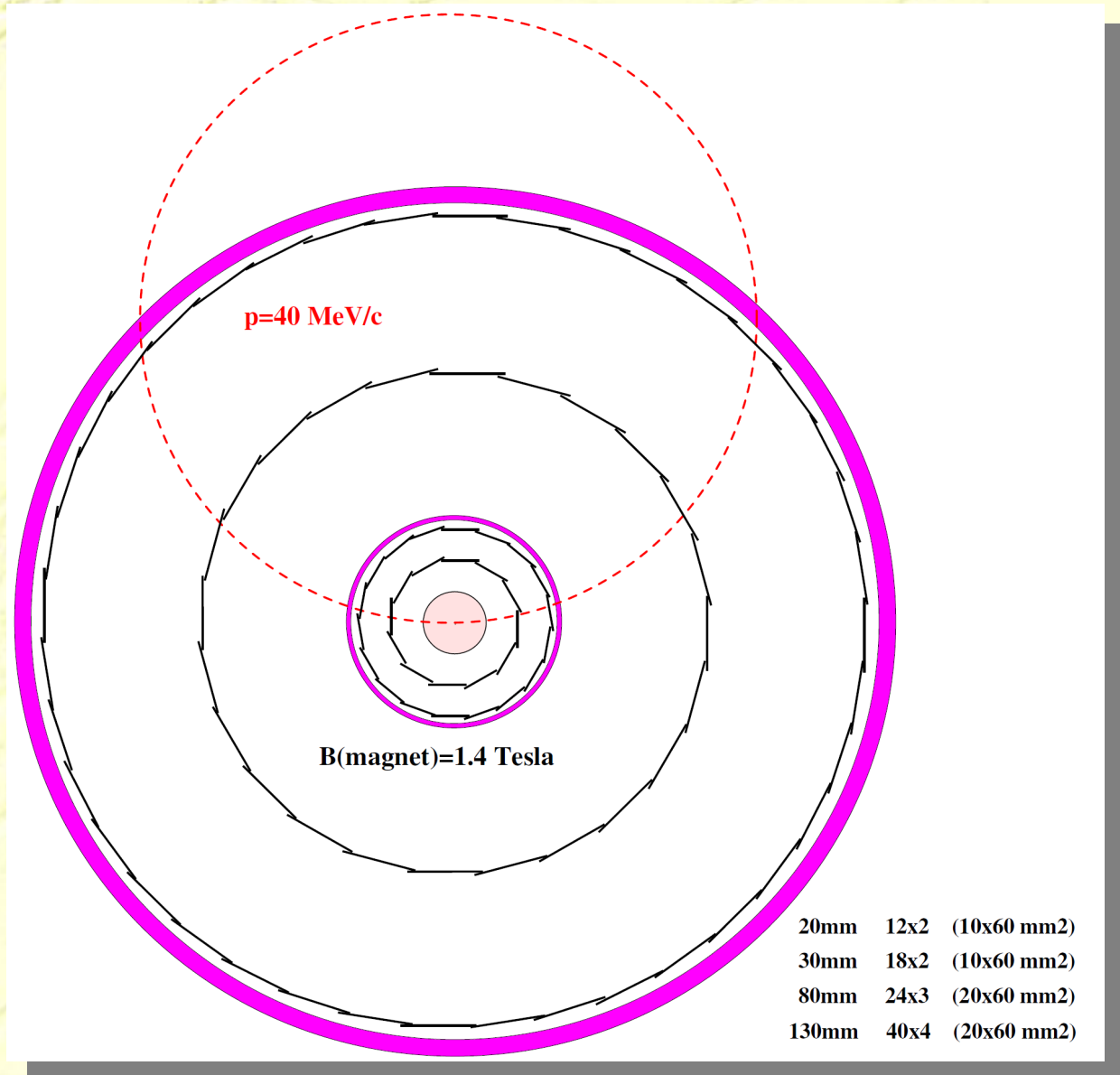
sensitivity  $\equiv$   
background

- good energy resolution suppresses  $\mu \rightarrow eee\nu$  BG effectively
- for  $\sigma_E = 0.3-0.6$  MeV sensitivity even below  $10^{-16}$

# Further Improvements?

Fit Recurling Track:

$$\sigma_E \leq 0.1 \text{ MeV ?}$$





# Mu3e Project

## Status of Project

- **interesting new ideas**
- no name, looking for collaborators

## Interested groups:

- Uni Zürich, ETH Zürich?
- Rome “La Sapienza”
- Paul Scherrer Institute
- Geneva
- Heidelberg (+ZITI Mannheim)

## Status of Activities (Heidelberg / Mannheim)

- **Tracker: Mechanical Stability / Construction studies**
- **Cooling studies**
- **MAPS HV CMOS design**  
first funding (50k€) for sensor prototype submission
- **Broken Line Fits and Fast Online Track Reconstruction**

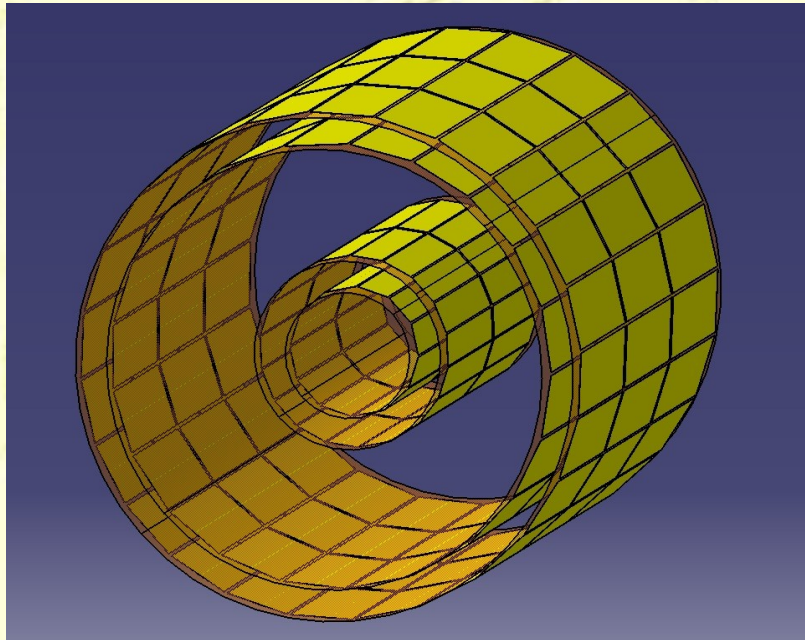
# Summary

- Novel detector concept for  $\mu \rightarrow eee$  experiment
- Technologies: **Silicon Pixel** and **Scintillating Fibers Trackers**
- sensitivity  **$BR(\mu \rightarrow eee) < 10^{-16}$**  seems feasible  
but more detailed simulations are required
- first pixel tracker prototype for 2012?
- could replace completed MEG experiment (in 2-3 years)
- later go to an upgraded high intensity beamline



# Conclusion

After more than 20 years time has come to repeat a search for  $\mu \rightarrow eee$  and to repeat very a successful experiment (Sindrum)



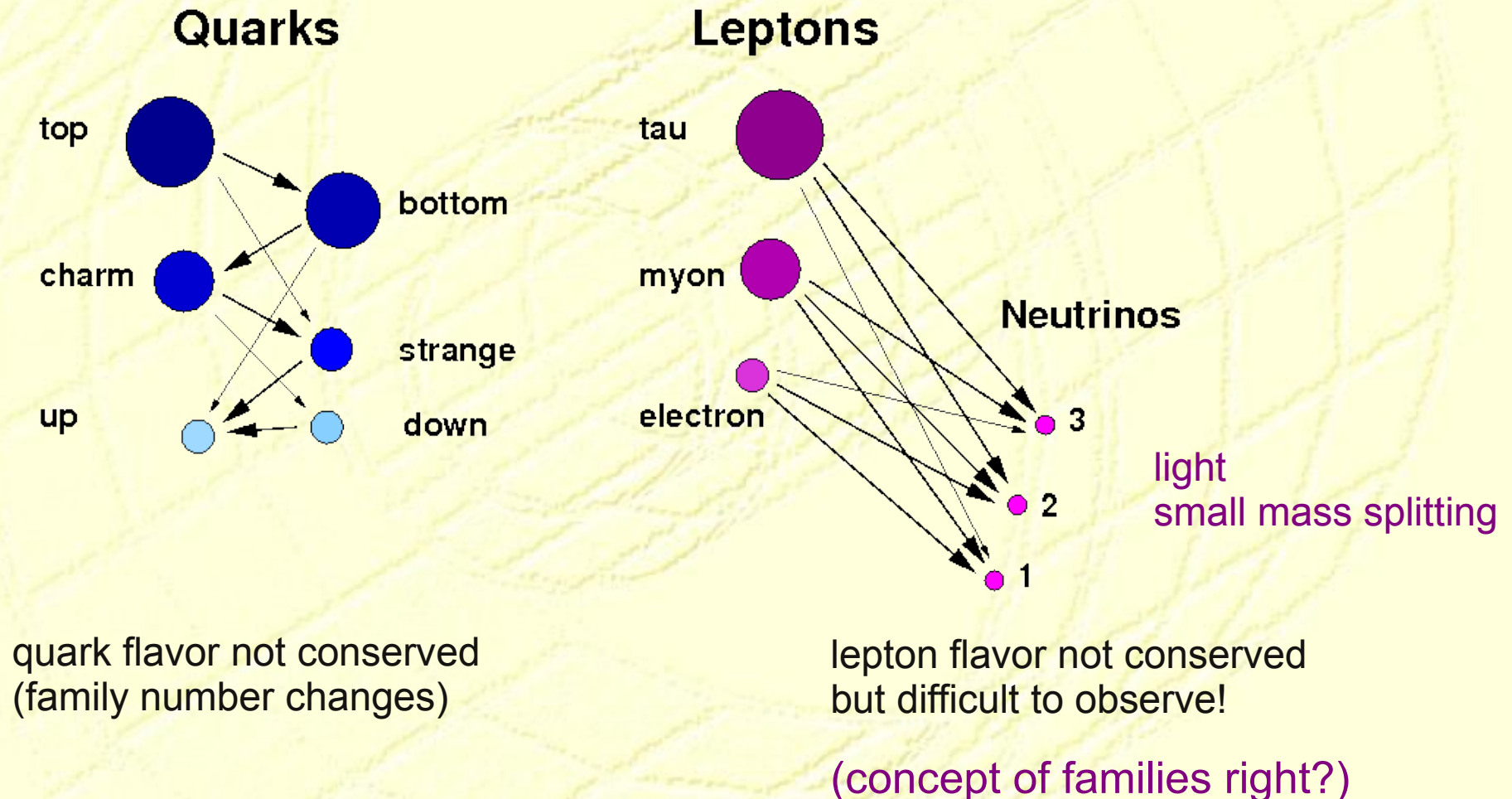
**A good detector is needed to resolve mysteries!**



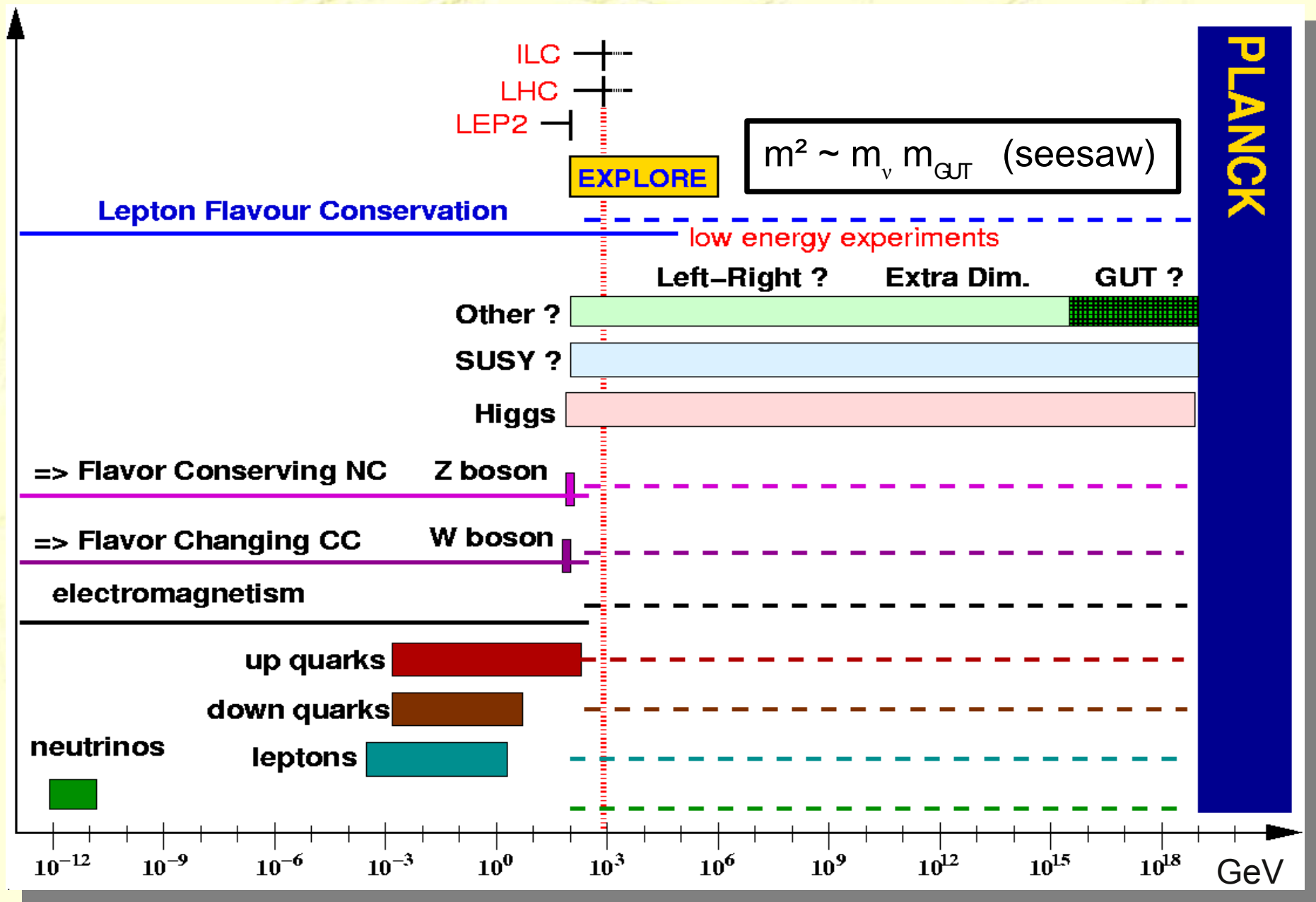
# Backup

# Family Number Violation

- Lepton Flavor Number in Charged Currents is an “ad hoc” concept

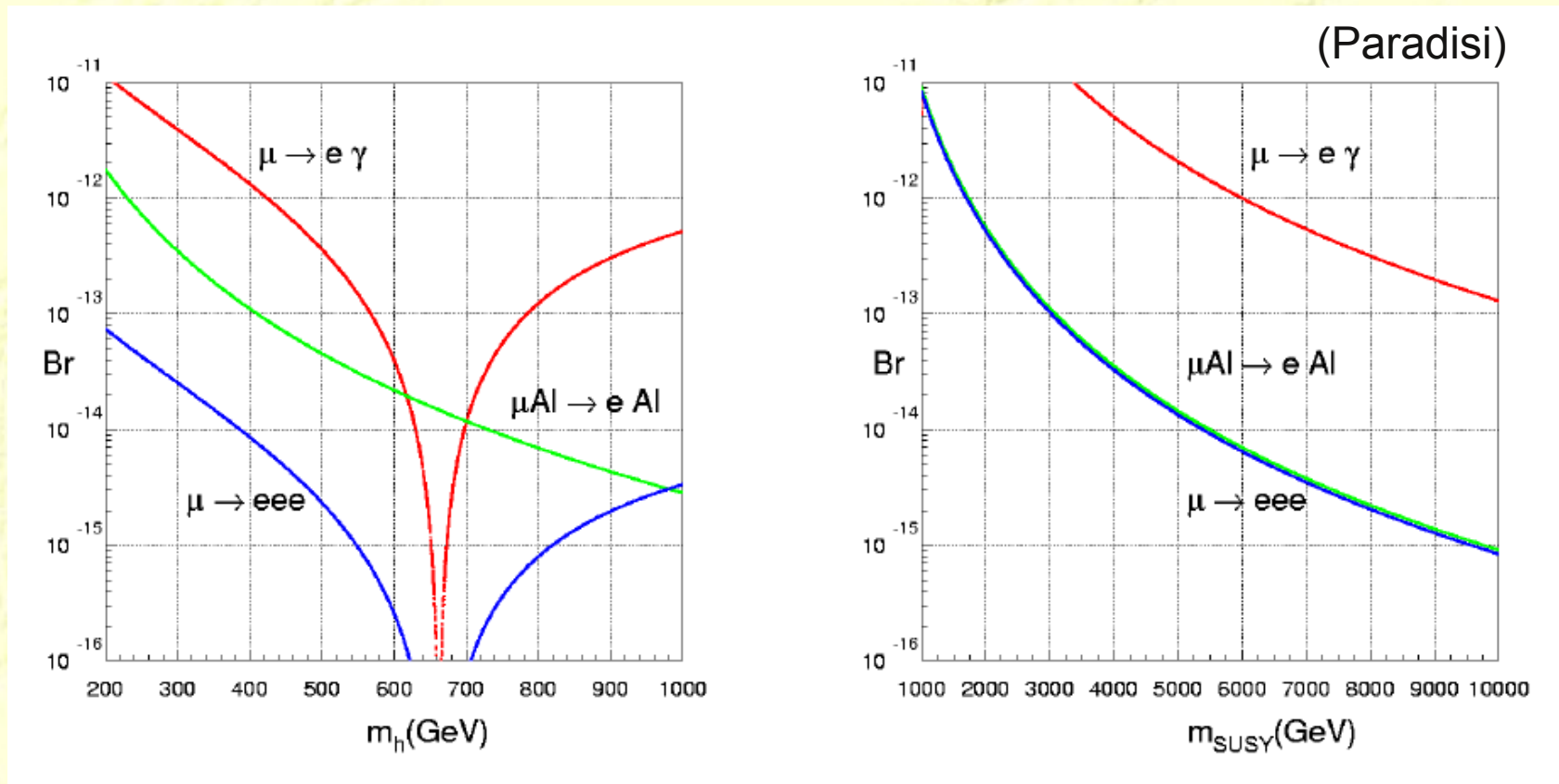


# Landscape of Mass Scales





# SUSY Higgs mediated LFV



# Leptogenesis

## Matter–anti matter asymmetry in the universe requires:

- Baryogenesis (Sacharov)

- baryon number violation
- CP (T) violation
- non equilibrium process

(measured but small)

- Leptogenesis (alternative)

- lepton number violation
- CP phase in lepton matrix
- non equilibrium process

(not observed)

(might be measured by  $\nu$  oscillation)

→ baryogenesis (sphaleron process)

- lepton flavor violation is a consequence of lepton number violation and CP phases



# Optimum Momentum Resolution

- minimum three layers → six coordinates
- momentum resolution multiple scattering dominated:

3 layers equidistant:

$$\frac{\sigma_p}{p} = 2 \frac{b}{BL}$$

4 layers equidistant:

$$\frac{\sigma_p}{p} = \frac{3}{\sqrt{2}} \frac{b}{BL} \approx 2.12 \frac{b}{BL}$$

$b \sim 0.001 T_m$   
(for 40 $\mu\text{m}$  Silicon)

>4 equidistant layers:

$$\frac{\sigma_p}{p} = \frac{N-3}{\sqrt{N-2}} \frac{b}{BL} \approx \sqrt{N} \frac{b}{BL}$$

- resolution is given by  $1/BL$ 
  - but minimum momentum given by  $p_{\min} \sim BL$



# Detector Acceptance $\mu^+ \rightarrow e^+e^+e^-$

## Model Dependence:

$$\frac{dB(\mu \rightarrow eee)}{dx_1 dx_2 d\cos\theta d\phi} = \sum_{k=1}^5 c_k \alpha_k(x_1, x_2)$$

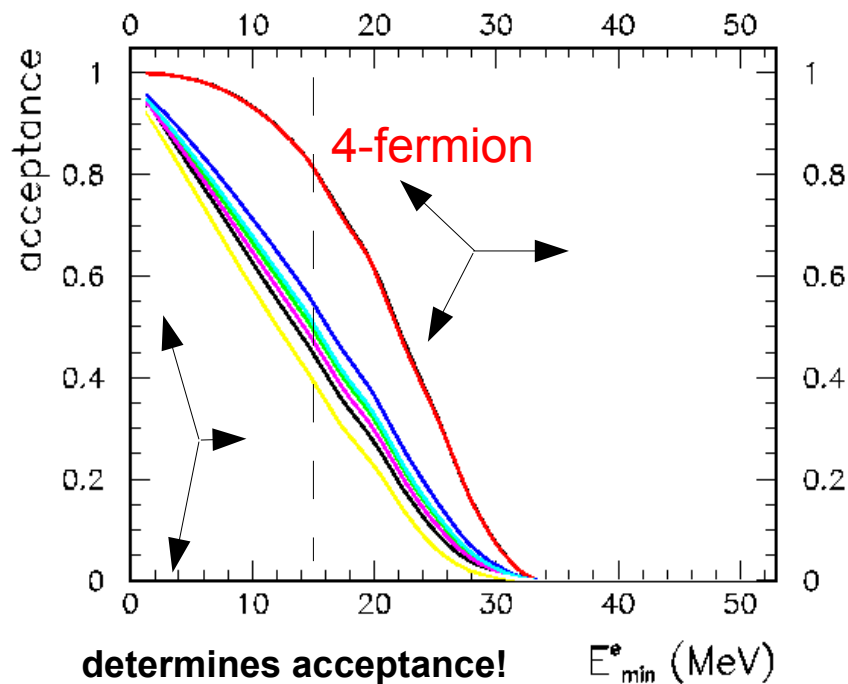
four  
fermion

photon  
penguin

$$\begin{aligned} c_1 &= \frac{g_1^2 + g_2^2}{16} + g_{34}^2 && \text{acc} \sim 80\% \\ c_2 &= g_{56}^2 && \\ c_3 &= e A^2 && \\ c_4 &= e A g_{34} \eta && \text{acc} \sim 40\% \\ c_5 &= e A g_{56} \eta' && \end{aligned}$$

T-odd

## Minimum electron energy:



measure momenta  
in range:  $p=15-53$  MeV/c

# DAQ

- Number of (zero suppressed) channels in Silicon ~10-20 million
- Number of channels in Fiber Tracker 5-10k
- What matters is the events rate of  $\sim 10^9$ 
  - data rate ~ 16 Gbyte/s
  - triggerless readout (software filter only)

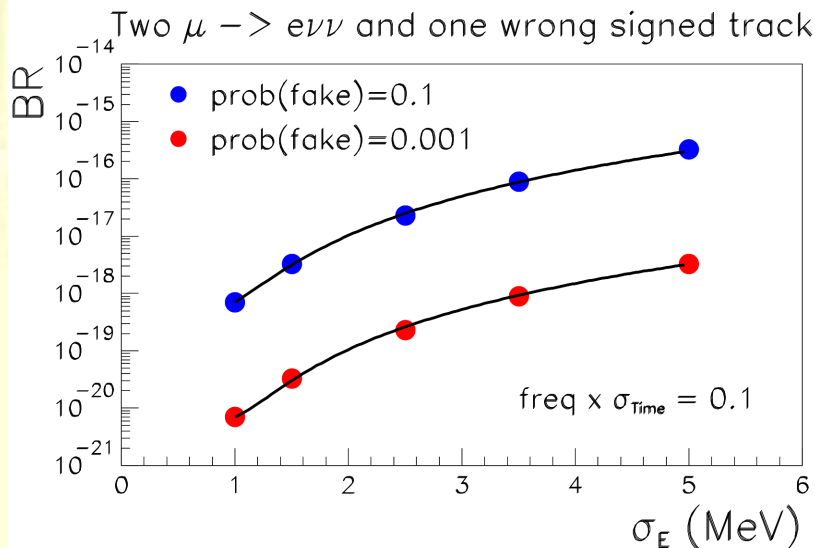
# Combinatorial Background

## Design Parameters:

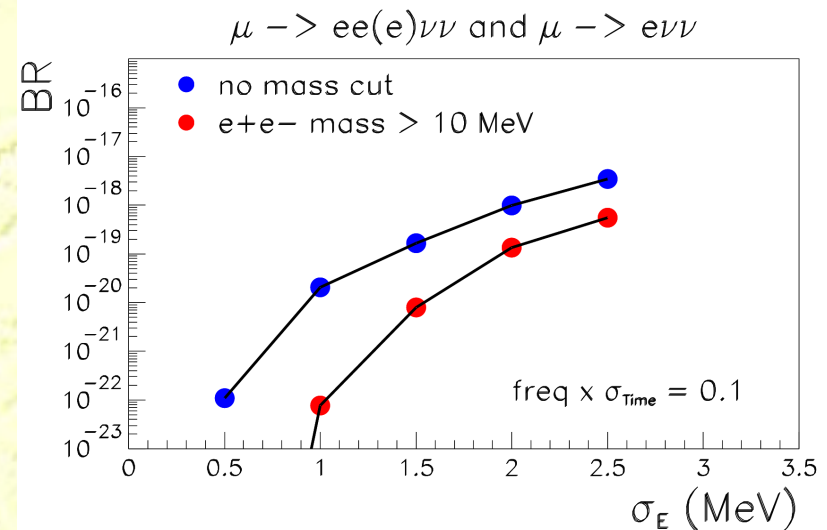
- prob (coincidence vertex) =  $5 \cdot 10^{-5}$
- prob (coincidence time) = 0.1

## BG as function of $E_{\text{tot}}$

### fake track and two muon decays



### internal conversion and muon decay



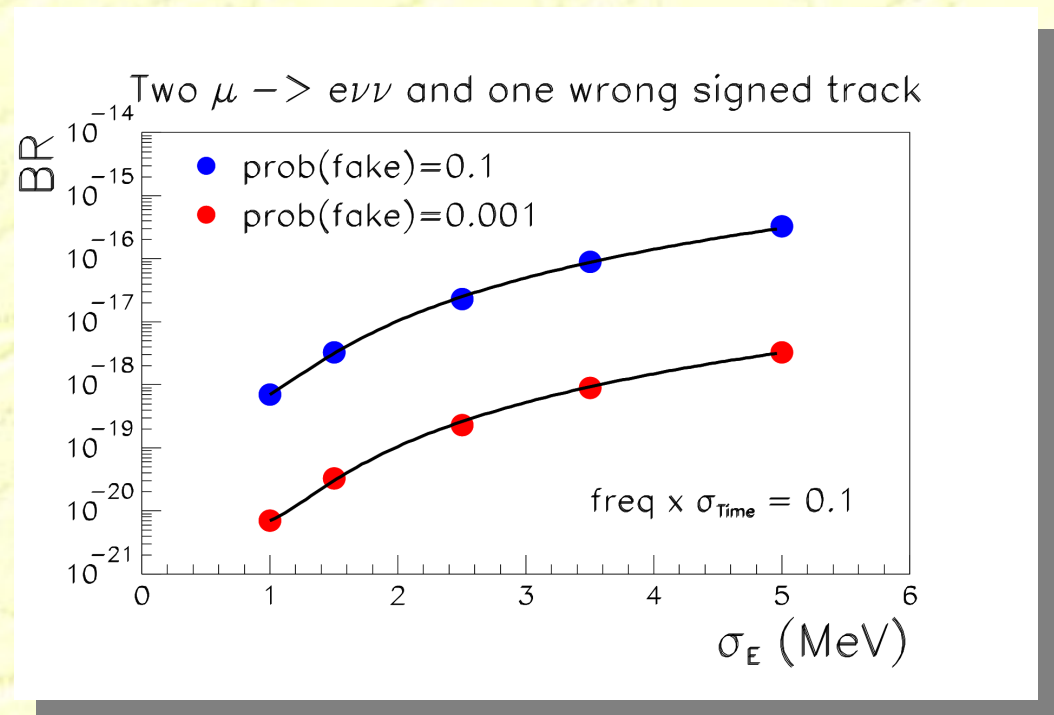
**combinatorial BG can be ignored already for moderate energy resolution  $\sigma_E < 3$  MeV**



# Maximum Muon Beam Intensity?

- **Combinatorial Background increases!**
- **The maximum tolerable muon intensity depends mainly on vertex, timing, and tracking resolution (also fake rate).**
- **assuming that the fake track reconstruction rate is small (0.001) a sensitivity of  $10^{-17}$  could be achieved with beam intensities of  $3 \cdot 10^{10}$  muon stops/s**

BG  $\sim$  rate<sup>2</sup>



# A new Silicon Detector for MEG?

Expected performance for electron  $p=53 \text{ MeV}/c$ :

$$\sigma_p = 0.3\text{-}0.6 \text{ MeV}/c \quad (\text{MEG } 0.7 \text{ MeV}/c)$$

$$\sigma_\theta \sim 5 \text{ mrad} \quad (\text{MEG } 8 \text{ mrad})$$

$$\sigma_{\text{vtx}} \sim 0.15 \text{ mm} \quad (\text{MEG } 1.4\text{-}2.5 \text{ mm})$$

momentum resolution could be further improved by increasing the lever arm:  
e.g.  $13 \text{ cm} \rightarrow 20 - 25 \text{ cm}$